

# MSSM with Seesaw I

Superpotential, Rotations and Interactions for eigenstates 'EWSB'  
including Renormalization Group Equations  
including one-loop Self-Energies

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References: arXiv: [1309.7223](#) , Comput.Phys.Commun.[184:1792-1809,2011](#) ([1207.0906](#)) , Comput.Phys.Commun.[182:833,2011](#) ([1002.0840](#)) , Comput.Phys.Commun.[181:1077-1086,2010](#) ([0909.2863](#)) , arXiv: [0806.0538](#)

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# Contents

<b>1 Superfields</b>	<b>3</b>
1.1 Vector Superfields . . . . .	3
1.2 Chiral Superfields . . . . .	3
<b>2 Superpotential and Lagrangian</b>	<b>3</b>
2.1 Superpotential . . . . .	3
2.2 Softbreaking terms . . . . .	3
2.3 Gauge fixing terms . . . . .	4
2.3.1 Gauge fixing terms for eigenstates 'GaugeES' . . . . .	4
2.3.2 Gauge fixing terms for eigenstates 'EWSB' . . . . .	4
2.4 Fields integrated out . . . . .	4
<b>3 Renormalization Group Equations</b>	<b>4</b>
3.1 Anomalous Dimensions . . . . .	4
3.2 Gauge Couplings . . . . .	5
3.3 Gaugino Mass Parameters . . . . .	6
3.4 Trilinear Superpotential Parameters . . . . .	6
3.5 Bilinear Superpotential Parameters . . . . .	7
3.6 Trilinear Soft-Breaking Parameters . . . . .	8
3.7 Bilinear Soft-Breaking Parameters . . . . .	10
3.8 Soft-Breaking Scalar Masses . . . . .	11
3.9 Vacuum expectation values . . . . .	18
<b>4 Field Rotations</b>	<b>19</b>
4.1 Rotations in gauge sector for eigenstates 'EWSB' . . . . .	19
4.2 Rotations in Mass sector for eigenstates 'EWSB' . . . . .	20
4.2.1 Mass Matrices for Scalars . . . . .	20
4.2.2 Mass Matrices for Fermions . . . . .	23
<b>5 Vacuum Expectation Values</b>	<b>25</b>
<b>6 Tadpole Equations</b>	<b>25</b>
<b>7 Particle content for eigenstates 'EWSB'</b>	<b>25</b>
<b>8 One Loop Self-Energy and One Loop Tadpoles for eigenstates 'EWSB'</b>	<b>26</b>
8.1 One Loop Self-Energy . . . . .	26
8.2 Tadpoles . . . . .	49
<b>9 Interactions for eigenstates 'EWSB'</b>	<b>49</b>
9.1 Three Scalar-Interaction . . . . .	49
9.2 Two Scalar-One Vector Boson-Interaction . . . . .	64
9.3 One Scalar-Two Vector Boson-Interaction . . . . .	72
9.4 Two Fermion-One Vector Boson-Interaction . . . . .	74
9.5 Two Fermion-One Scalar Boson-Interaction . . . . .	80

9.6	Three Vector Boson-Interaction . . . . .	96
9.7	Four Scalar-Interaction . . . . .	97
9.8	Two Scalar-Two Vector Boson-Interaction . . . . .	147
9.9	Four Vector Boson-Interaction . . . . .	165
9.10	Two Ghosts-One Vector Boson-Interaction . . . . .	167
9.11	Two Ghosts-One Scalar-Interaction . . . . .	171
<b>10</b>	<b>Clebsch-Gordan Coefficients</b>	<b>175</b>

# 1 Superfields

## 1.1 Vector Superfields

SF	Spin $\frac{1}{2}$	Spin 1	$SU(N)$	Coupling	Name
$\hat{B}$	$\lambda_{\tilde{B}}$	$B$	$U(1)$	$g_1$	hypercharge
$\hat{W}$	$\lambda_{\tilde{W}}$	$W$	$SU(2)$	$g_2$	left
$\hat{g}$	$\lambda_{\tilde{g}}$	$g$	$SU(3)$	$g_3$	color

## 1.2 Chiral Superfields

SF	Spin 0	Spin $\frac{1}{2}$	Generations	$(U(1) \otimes SU(2) \otimes SU(3))$
$\hat{q}$	$\tilde{q}$	$q$	3	$(\frac{1}{6}, \mathbf{2}, \mathbf{3})$
$\hat{l}$	$\tilde{l}$	$l$	3	$(-\frac{1}{2}, \mathbf{2}, \mathbf{1})$
$\hat{H}_d$	$H_d$	$\tilde{H}_d$	1	$(-\frac{1}{2}, \mathbf{2}, \mathbf{1})$
$\hat{H}_u$	$H_u$	$\tilde{H}_u$	1	$(\frac{1}{2}, \mathbf{2}, \mathbf{1})$
$\hat{d}$	$\tilde{d}_R^*$	$d_R^*$	3	$(\frac{1}{3}, \mathbf{1}, \bar{\mathbf{3}})$
$\hat{u}$	$\tilde{u}_R^*$	$u_R^*$	3	$(-\frac{2}{3}, \mathbf{1}, \bar{\mathbf{3}})$
$\hat{e}$	$\tilde{e}_R^*$	$e_R^*$	3	$(1, \mathbf{1}, \mathbf{1})$
$\hat{\nu}$	$\tilde{\nu}_R$	$\nu_R$	3	$(0, \mathbf{1}, \mathbf{1})$

# 2 Superpotential and Lagrangian

## 2.1 Superpotential

$$W = \mu \hat{H}_u \hat{H}_d + \frac{1}{2} M_v \hat{\nu} \hat{\nu} - Y_d \hat{d} \hat{q} \hat{H}_d - Y_e \hat{e} \hat{l} \hat{H}_d + Y_u \hat{u} \hat{q} \hat{H}_u + Y_\nu \hat{\nu} \hat{l} \hat{H}_u + \frac{1}{2} \kappa_\nu \hat{l} \hat{H}_u \hat{l} \hat{H}_u \quad (1)$$

## 2.2 Softbreaking terms

$$\begin{aligned} -L_{SB,W} = & -H_d^0 H_u^0 B_\mu + H_d^- H_u^+ B_\mu + \frac{1}{2} \tilde{\nu}_{R,i} \tilde{\nu}_{R,j} B_{v,ij} \\ & + \frac{1}{2} \left( H_u^{0,2} \tilde{\nu}_{L,i} \tilde{\nu}_{L,k} Q_{\nu,ik} - H_u^0 H_u^+ \tilde{e}_{L,i} \tilde{\nu}_{L,k} Q_{\nu,ik} - H_u^0 H_u^+ \tilde{e}_{L,k} \tilde{\nu}_{L,i} Q_{\nu,ik} + H_u^{+,2} \tilde{e}_{L,i} \tilde{e}_{L,k} Q_{\nu,ik} \right) \\ & + H_d^0 \tilde{d}_{R,i\alpha}^* \delta_{\alpha\beta} \tilde{d}_{L,j\beta} T_{d,ij} - H_d^- \tilde{d}_{R,i\alpha}^* \delta_{\alpha\beta} \tilde{u}_{L,j\beta} T_{d,ij} + H_d^0 \tilde{e}_{R,i}^* \tilde{e}_{L,j} T_{e,ij} - H_d^- \tilde{e}_{R,i}^* \tilde{\nu}_{L,j} T_{e,ij} \\ & - H_u^+ \tilde{u}_{R,i\alpha}^* \delta_{\alpha\beta} \tilde{d}_{L,j\beta} T_{u,ij} + H_u^0 \tilde{u}_{R,i\alpha}^* \delta_{\alpha\beta} \tilde{u}_{L,j\beta} T_{u,ij} - H_u^+ \tilde{e}_{L,j} \tilde{\nu}_{R,i} T_{\nu,ij} + H_u^0 \tilde{\nu}_{L,j} \tilde{\nu}_{R,i} T_{\nu,ij} + \text{h.c.} \end{aligned} \quad (2)$$

$$\begin{aligned} -L_{SB,\phi} = & +m_{H_d}^2 |H_d^0|^2 + m_{H_d}^2 |H_d^-|^2 + m_{H_u}^2 |H_u^0|^2 + m_{H_u}^2 |H_u^+|^2 + \tilde{d}_{L,i\alpha}^* \delta_{\alpha\beta} m_{q,ij}^2 \tilde{d}_{L,j\beta} \\ & + \tilde{d}_{R,i\alpha}^* \delta_{\alpha\beta} m_{d,ij}^2 \tilde{d}_{R,j\beta} + \tilde{e}_{L,i}^* m_{l,ij}^2 \tilde{e}_{L,j} + \tilde{e}_{R,i}^* m_{e,ij}^2 \tilde{e}_{R,j} + \tilde{u}_{L,i\alpha}^* \delta_{\alpha\beta} m_{q,ij}^2 \tilde{u}_{L,j\beta} \\ & + \tilde{u}_{R,i\alpha}^* \delta_{\alpha\beta} m_{u,ij}^2 \tilde{u}_{R,j\beta} + \tilde{\nu}_{L,i}^* m_{l,ij}^2 \tilde{\nu}_{L,j} + \tilde{\nu}_{R,i}^* m_{\nu,ij}^2 \tilde{\nu}_{R,j} \end{aligned} \quad (3)$$

$$-L_{SB,\lambda} = \frac{1}{2} \left( \lambda_{\tilde{B}}^2 M_1 \delta_{ij} + M_2 \delta_{ij} \lambda_{\tilde{W},i} \lambda_{\tilde{W},j} + M_3 \delta_{ij} \lambda_{\tilde{g},\alpha} \lambda_{\tilde{g},\beta} + \text{h.c.} \right) \quad (4)$$

## 2.3 Gauge fixing terms

### 2.3.1 Gauge fixing terms for eigenstates 'GaugeES'

$$L_{GF} = -\frac{1}{2} |\partial_\mu B|^2 \xi_B^{-1} - \frac{1}{2} |\partial_\mu g|^2 \xi_g^{-1} - \frac{1}{2} |\partial_\mu W|^2 \xi_W^{-1} \quad (5)$$

### 2.3.2 Gauge fixing terms for eigenstates 'EWSB'

$$\begin{aligned} L_{GF} = & -\frac{1}{2} |\partial_\mu g|^2 \xi_g^{-1} - \frac{1}{2} |\partial_\mu \gamma|^2 \xi_\gamma^{-1} - | - \frac{i}{2} g_2 \left( H_d^- v_d - v_u H_u^{+,*} \right) \xi_{W^-} + \partial_\mu W^-|^2 \xi_{W^-}^{-1} \\ & - \frac{1}{2} \frac{1}{2} \left( 2 \partial_\mu Z + \left( \sigma_d v_d - \sigma_u v_u \right) \xi_Z \left( g_1 \sin \Theta_W + g_2 \cos \Theta_W \right) \right)^2 \xi_Z^{-1} \end{aligned} \quad (6)$$

## 2.4 Fields integrated out

1.  $\hat{\nu}$

## 3 Renormalization Group Equations

### 3.1 Anomalous Dimensions

$$\gamma_{\hat{q}}^{(1)} = -\frac{1}{30} \left( 45g_2^2 + 80g_3^2 + g_1^2 \right) \mathbf{1} + Y_d^\dagger Y_d + Y_u^\dagger Y_u \quad (7)$$

$$\begin{aligned} \gamma_{\hat{q}}^{(2)} = & + \left( 8g_2^2 g_3^2 + \frac{15}{4} g_2^4 + \frac{1}{90} g_1^2 \left( 16g_3^2 + 9g_2^2 \right) + \frac{199}{900} g_1^4 - \frac{8}{9} g_3^4 \right) \mathbf{1} + \frac{4}{5} g_1^2 Y_u^\dagger Y_u - 2Y_d^\dagger Y_d Y_d^\dagger Y_d \\ & - 2Y_u^\dagger Y_u Y_u^\dagger Y_u + Y_d^\dagger Y_d \left( -3 \text{Tr} \left( Y_d Y_d^\dagger \right) + \frac{2}{5} g_1^2 - \text{Tr} \left( Y_e Y_e^\dagger \right) \right) - 3Y_u^\dagger Y_u \text{Tr} \left( Y_u Y_u^\dagger \right) \\ & - Y_u^\dagger Y_u \text{Tr} \left( Y_\nu Y_\nu^\dagger \right) \end{aligned} \quad (8)$$

$$\gamma_{\hat{l}}^{(1)} = -\frac{3}{10} \left( 5g_2^2 + g_1^2 \right) \mathbf{1} + Y_e^\dagger Y_e + Y_\nu^\dagger Y_\nu \quad (9)$$

$$\begin{aligned} \gamma_{\hat{l}}^{(2)} = & + \frac{3}{100} \left( 125g_2^4 + 30g_1^2 g_2^2 + 69g_1^4 \right) \mathbf{1} - 2Y_e^\dagger Y_e Y_e^\dagger Y_e - 2Y_\nu^\dagger Y_\nu Y_\nu^\dagger Y_\nu \\ & + Y_e^\dagger Y_e \left( -3 \text{Tr} \left( Y_d Y_d^\dagger \right) + \frac{6}{5} g_1^2 - \text{Tr} \left( Y_e Y_e^\dagger \right) \right) - 3Y_\nu^\dagger Y_\nu \text{Tr} \left( Y_u Y_u^\dagger \right) \\ & - Y_\nu^\dagger Y_\nu \text{Tr} \left( Y_\nu Y_\nu^\dagger \right) \end{aligned} \quad (10)$$

$$\gamma_{\hat{H}_d}^{(1)} = 3 \text{Tr} \left( Y_d Y_d^\dagger \right) - \frac{3}{10} \left( 5g_2^2 + g_1^2 \right) + \text{Tr} \left( Y_e Y_e^\dagger \right) \quad (11)$$

$$\begin{aligned} \gamma_{\hat{H}_d}^{(2)} = & + \frac{207}{100} g_1^4 + \frac{9}{10} g_1^2 g_2^2 + \frac{15}{4} g_2^4 - \frac{2}{5} \left( -40g_3^2 + g_1^2 \right) \text{Tr} \left( Y_d Y_d^\dagger \right) + \frac{6}{5} g_1^2 \text{Tr} \left( Y_e Y_e^\dagger \right) - 9 \text{Tr} \left( Y_d Y_d^\dagger Y_d Y_d^\dagger \right) \\ & - 3 \text{Tr} \left( Y_d Y_u^\dagger Y_u Y_d^\dagger \right) - 3 \text{Tr} \left( Y_e Y_e^\dagger Y_e Y_e^\dagger \right) - \text{Tr} \left( Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger \right) \end{aligned} \quad (12)$$

$$\gamma_{\hat{H}_u}^{(1)} = 3\text{Tr}\left(Y_u Y_u^\dagger\right) - \frac{3}{10}\left(5g_2^2 + g_1^2\right) + \text{Tr}\left(Y_\nu Y_\nu^\dagger\right) \quad (13)$$

$$\begin{aligned} \gamma_{\hat{H}_u}^{(2)} = & +\frac{207}{100}g_1^4 + \frac{9}{10}g_1^2g_2^2 + \frac{15}{4}g_2^4 + \frac{4}{5}\left(20g_3^2 + g_1^2\right)\text{Tr}\left(Y_u Y_u^\dagger\right) - 3\text{Tr}\left(Y_d Y_u^\dagger Y_u Y_d^\dagger\right) \\ & - \text{Tr}\left(Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger\right) - 9\text{Tr}\left(Y_u Y_u^\dagger Y_u Y_u^\dagger\right) - 3\text{Tr}\left(Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger\right) \end{aligned} \quad (14)$$

$$\gamma_{\hat{d}}^{(1)} = 2Y_d^* Y_d^T - \frac{2}{15}\left(20g_3^2 + g_1^2\right)\mathbf{1} \quad (15)$$

$$\begin{aligned} \gamma_{\hat{d}}^{(2)} = & +\frac{2}{225}\left(-100g_3^4 + 101g_1^4 + 80g_1^2g_3^2\right)\mathbf{1} - 2\left(Y_d^* Y_d^T Y_d^* Y_d^T + Y_d^* Y_u^T Y_u^* Y_d^T\right) \\ & + Y_d^* Y_d^T \left(-2\text{Tr}\left(Y_e Y_e^\dagger\right) + 6g_2^2 - 6\text{Tr}\left(Y_d Y_d^\dagger\right) + \frac{2}{5}g_1^2\right) \end{aligned} \quad (16)$$

$$\gamma_{\hat{u}}^{(1)} = 2Y_u^* Y_u^T - \frac{8}{15}\left(5g_3^2 + g_1^2\right)\mathbf{1} \quad (17)$$

$$\begin{aligned} \gamma_{\hat{u}}^{(2)} = & +\frac{8}{225}\left(107g_1^4 - 25g_3^4 + 80g_1^2g_3^2\right)\mathbf{1} \\ & - \frac{2}{5}\left(5\left(Y_u^* Y_d^T Y_d^* Y_u^T + Y_u^* Y_u^T Y_u^* Y_u^T\right) + Y_u^* Y_u^T \left(-15g_2^2 + 15\text{Tr}\left(Y_u Y_u^\dagger\right) + 5\text{Tr}\left(Y_\nu Y_\nu^\dagger\right) + g_1^2\right)\right) \end{aligned} \quad (18)$$

$$\gamma_{\hat{e}}^{(1)} = 2Y_e^* Y_e^T - \frac{6}{5}g_1^2\mathbf{1} \quad (19)$$

$$\begin{aligned} \gamma_{\hat{e}}^{(2)} = & +\frac{234}{25}g_1^4\mathbf{1} - 2\left(Y_e^* Y_e^T Y_e^* Y_e^T + Y_e^* Y_\nu^T Y_\nu^* Y_e^T\right) \\ & + Y_e^* Y_e^T \left(-2\text{Tr}\left(Y_e Y_e^\dagger\right) + 6g_2^2 - 6\text{Tr}\left(Y_d Y_d^\dagger\right) - \frac{6}{5}g_1^2\right) \end{aligned} \quad (20)$$

$$\gamma_{\hat{\nu}}^{(1)} = 2Y_\nu^* Y_\nu^T \quad (21)$$

$$\gamma_{\hat{\nu}}^{(2)} = -2\left(Y_\nu^* Y_e^T Y_e^* Y_\nu^T + Y_\nu^* Y_\nu^T Y_\nu^* Y_\nu^T\right) + Y_\nu^* Y_\nu^T \left(-2\text{Tr}\left(Y_\nu Y_\nu^\dagger\right) + 6g_2^2 - 6\text{Tr}\left(Y_u Y_u^\dagger\right) + \frac{6}{5}g_1^2\right) \quad (22)$$

### 3.2 Gauge Couplings

$$\beta_{g_1}^{(1)} = \frac{33}{5}g_1^3 \quad (23)$$

$$\beta_{g_1}^{(2)} = \frac{1}{25}g_1^3 \left(-130\text{Tr}\left(Y_u Y_u^\dagger\right) + 135g_2^2 + 199g_1^2 - 30\text{Tr}\left(Y_\nu Y_\nu^\dagger\right) + 440g_3^2 - 70\text{Tr}\left(Y_d Y_d^\dagger\right) - 90\text{Tr}\left(Y_e Y_e^\dagger\right)\right) \quad (24)$$

$$\beta_{g_2}^{(1)} = g_2^3 \quad (25)$$

$$\beta_{g_2}^{(2)} = \frac{1}{5}g_2^3 \left(-10\text{Tr}\left(Y_e Y_e^\dagger\right) - 10\text{Tr}\left(Y_\nu Y_\nu^\dagger\right) + 120g_3^2 + 125g_2^2 - 30\text{Tr}\left(Y_d Y_d^\dagger\right) - 30\text{Tr}\left(Y_u Y_u^\dagger\right) + 9g_1^2\right) \quad (26)$$

$$\beta_{g_3}^{(1)} = -3g_3^3 \quad (27)$$

$$\beta_{g_3}^{(2)} = \frac{1}{5}g_3^3 \left(11g_1^2 - 20\text{Tr}\left(Y_d Y_d^\dagger\right) - 20\text{Tr}\left(Y_u Y_u^\dagger\right) + 45g_2^2 + 70g_3^2\right) \quad (28)$$

### 3.3 Gaugino Mass Parameters

$$\beta_{M_1}^{(1)} = \frac{66}{5} g_1^2 M_1 \quad (29)$$

$$\begin{aligned} \beta_{M_1}^{(2)} = & \frac{2}{25} g_1^2 \left( 398g_1^2 M_1 + 135g_2^2 M_1 + 440g_3^2 M_1 + 440g_3^2 M_3 + 135g_2^2 M_2 - 70M_1 \text{Tr}(Y_d Y_d^\dagger) - 90M_1 \text{Tr}(Y_e Y_e^\dagger) \right. \\ & \left. - 130M_1 \text{Tr}(Y_u Y_u^\dagger) - 30M_1 \text{Tr}(Y_\nu Y_\nu^\dagger) + 70 \text{Tr}(Y_d^\dagger T_d) + 90 \text{Tr}(Y_e^\dagger T_e) + 130 \text{Tr}(Y_u^\dagger T_u) + 30 \text{Tr}(Y_\nu^\dagger T_\nu) \right) \end{aligned} \quad (30)$$

$$\beta_{M_2}^{(1)} = 2g_2^2 M_2 \quad (31)$$

$$\begin{aligned} \beta_{M_2}^{(2)} = & \frac{2}{5} g_2^2 \left( 9g_1^2 M_1 + 120g_3^2 M_3 + 9g_1^2 M_2 + 250g_2^2 M_2 + 120g_3^2 M_2 - 30M_2 \text{Tr}(Y_d Y_d^\dagger) - 10M_2 \text{Tr}(Y_e Y_e^\dagger) \right. \\ & \left. - 30M_2 \text{Tr}(Y_u Y_u^\dagger) - 10M_2 \text{Tr}(Y_\nu Y_\nu^\dagger) + 30 \text{Tr}(Y_d^\dagger T_d) + 10 \text{Tr}(Y_e^\dagger T_e) + 30 \text{Tr}(Y_u^\dagger T_u) + 10 \text{Tr}(Y_\nu^\dagger T_\nu) \right) \end{aligned} \quad (32)$$

$$\beta_{M_3}^{(1)} = -6g_3^2 M_3 \quad (33)$$

$$\begin{aligned} \beta_{M_3}^{(2)} = & \frac{2}{5} g_3^2 \left( 11g_1^2 M_1 + 11g_1^2 M_3 + 45g_2^2 M_3 + 140g_3^2 M_3 + 45g_2^2 M_2 - 20M_3 \text{Tr}(Y_d Y_d^\dagger) - 20M_3 \text{Tr}(Y_u Y_u^\dagger) \right. \\ & \left. + 20 \text{Tr}(Y_d^\dagger T_d) + 20 \text{Tr}(Y_u^\dagger T_u) \right) \end{aligned} \quad (34)$$

### 3.4 Trilinear Superpotential Parameters

$$\beta_{Y_d}^{(1)} = 3Y_d Y_d^\dagger Y_d + Y_d \left( -3g_2^2 + 3 \text{Tr}(Y_d Y_d^\dagger) - \frac{16}{3} g_3^2 - \frac{7}{15} g_1^2 + \text{Tr}(Y_e Y_e^\dagger) \right) + Y_d Y_u^\dagger Y_u \quad (35)$$

$$\begin{aligned} \beta_{Y_d}^{(2)} = & +\frac{4}{5} g_1^2 Y_d Y_u^\dagger Y_u - 4Y_d Y_d^\dagger Y_d Y_d^\dagger Y_d - 2Y_d Y_u^\dagger Y_u Y_d^\dagger Y_d - 2Y_d Y_u^\dagger Y_u Y_u^\dagger Y_u \\ & + Y_d Y_d^\dagger Y_d \left( -3 \text{Tr}(Y_e Y_e^\dagger) + 6g_2^2 - 9 \text{Tr}(Y_d Y_d^\dagger) + \frac{4}{5} g_1^2 \right) - 3Y_d Y_u^\dagger Y_u \text{Tr}(Y_u Y_u^\dagger) \\ & - Y_d Y_u^\dagger Y_u \text{Tr}(Y_\nu Y_\nu^\dagger) \\ & + Y_d \left( \frac{287}{90} g_1^4 + g_1^2 g_2^2 + \frac{15}{2} g_2^4 + \frac{8}{9} g_1^2 g_3^2 + 8g_2^2 g_3^2 - \frac{16}{9} g_3^4 - \frac{2}{5} (-40g_3^2 + g_1^2) \text{Tr}(Y_d Y_d^\dagger) \right. \\ & \left. + \frac{6}{5} g_1^2 \text{Tr}(Y_e Y_e^\dagger) - 9 \text{Tr}(Y_d Y_d^\dagger Y_d Y_d^\dagger) - 3 \text{Tr}(Y_d Y_u^\dagger Y_u Y_d^\dagger) - 3 \text{Tr}(Y_e Y_e^\dagger Y_e Y_e^\dagger) \right. \\ & \left. - \text{Tr}(Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger) \right) \end{aligned} \quad (36)$$

$$\beta_{Y_e}^{(1)} = 3Y_e Y_e^\dagger Y_e + Y_e \left( -3g_2^2 + 3 \text{Tr}(Y_d Y_d^\dagger) - \frac{9}{5} g_1^2 + \text{Tr}(Y_e Y_e^\dagger) \right) + Y_e Y_\nu^\dagger Y_\nu \quad (37)$$

$$\begin{aligned} \beta_{Y_e}^{(2)} = & -4Y_e Y_e^\dagger Y_e Y_e^\dagger Y_e - 2Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger Y_e - 2Y_e Y_\nu^\dagger Y_\nu Y_\nu^\dagger Y_\nu \\ & + Y_e Y_e^\dagger Y_e \left( -3 \text{Tr}(Y_e Y_e^\dagger) + 6g_2^2 - 9 \text{Tr}(Y_d Y_d^\dagger) \right) - 3Y_e Y_\nu^\dagger Y_\nu \text{Tr}(Y_u Y_u^\dagger) \\ & - Y_e Y_\nu^\dagger Y_\nu \text{Tr}(Y_\nu Y_\nu^\dagger) \\ & + \frac{1}{10} Y_e \left( 135g_1^4 + 18g_1^2 g_2^2 + 75g_2^4 - 4(-40g_3^2 + g_1^2) \text{Tr}(Y_d Y_d^\dagger) + 12g_1^2 \text{Tr}(Y_e Y_e^\dagger) - 90 \text{Tr}(Y_d Y_d^\dagger Y_d Y_d^\dagger) \right) \end{aligned}$$

$$- 30\text{Tr}\left(Y_d Y_u^\dagger Y_u Y_d^\dagger\right) - 30\text{Tr}\left(Y_e Y_e^\dagger Y_e Y_e^\dagger\right) - 10\text{Tr}\left(Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger\right) \quad (38)$$

$$\beta_{Y_u}^{(1)} = 3Y_u Y_u^\dagger Y_u + Y_u \left( -3g_2^2 + 3\text{Tr}\left(Y_u Y_u^\dagger\right) - \frac{13}{15}g_1^2 - \frac{16}{3}g_3^2 + \text{Tr}\left(Y_\nu Y_\nu^\dagger\right) \right) + Y_u Y_d^\dagger Y_d \quad (39)$$

$$\begin{aligned} \beta_{Y_u}^{(2)} = & +\frac{2}{5}g_1^2 Y_u Y_u^\dagger Y_u + 6g_2^2 Y_u Y_u^\dagger Y_u - 2Y_u Y_d^\dagger Y_d Y_d^\dagger Y_d - 2Y_u Y_d^\dagger Y_d Y_u^\dagger Y_u \\ & - 4Y_u Y_u^\dagger Y_u Y_u^\dagger Y_u + Y_u Y_d^\dagger Y_d \left( -3\text{Tr}\left(Y_d Y_d^\dagger\right) + \frac{2}{5}g_1^2 - \text{Tr}\left(Y_e Y_e^\dagger\right) \right) - 9Y_u Y_u^\dagger Y_u \text{Tr}\left(Y_u Y_u^\dagger\right) \\ & - 3Y_u Y_u^\dagger Y_u \text{Tr}\left(Y_\nu Y_\nu^\dagger\right) \\ & + Y_u \left( \frac{2743}{450}g_1^4 + g_1^2 g_2^2 + \frac{15}{2}g_2^4 + \frac{136}{45}g_1^2 g_3^2 + 8g_2^2 g_3^2 - \frac{16}{9}g_3^4 + \frac{4}{5}(20g_3^2 + g_1^2)\text{Tr}\left(Y_u Y_u^\dagger\right) \right. \\ & \left. - 3\text{Tr}\left(Y_d Y_u^\dagger Y_u Y_d^\dagger\right) - \text{Tr}\left(Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger\right) - 9\text{Tr}\left(Y_u Y_u^\dagger Y_u Y_u^\dagger\right) - 3\text{Tr}\left(Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger\right) \right) \end{aligned} \quad (40)$$

$$\beta_{Y_\nu}^{(1)} = 3Y_\nu Y_\nu^\dagger Y_\nu + Y_\nu \left( -3g_2^2 + 3\text{Tr}\left(Y_u Y_u^\dagger\right) - \frac{3}{5}g_1^2 + \text{Tr}\left(Y_\nu Y_\nu^\dagger\right) \right) + Y_\nu Y_e^\dagger Y_e \quad (41)$$

$$\begin{aligned} \beta_{Y_\nu}^{(2)} = & +\frac{6}{5}g_1^2 Y_\nu Y_\nu^\dagger Y_\nu + 6g_2^2 Y_\nu Y_\nu^\dagger Y_\nu - 2Y_\nu Y_e^\dagger Y_e Y_e^\dagger Y_e - 2Y_\nu Y_e^\dagger Y_e Y_\nu^\dagger Y_\nu \\ & - 4Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger Y_\nu + Y_\nu Y_e^\dagger Y_e \left( -3\text{Tr}\left(Y_d Y_d^\dagger\right) + \frac{6}{5}g_1^2 - \text{Tr}\left(Y_e Y_e^\dagger\right) \right) - 9Y_\nu Y_\nu^\dagger Y_\nu \text{Tr}\left(Y_u Y_u^\dagger\right) \\ & - 3Y_\nu Y_\nu^\dagger Y_\nu \text{Tr}\left(Y_\nu Y_\nu^\dagger\right) \\ & + Y_\nu \left( \frac{207}{50}g_1^4 + \frac{9}{5}g_1^2 g_2^2 + \frac{15}{2}g_2^4 + \frac{4}{5}(20g_3^2 + g_1^2)\text{Tr}\left(Y_u Y_u^\dagger\right) - 3\text{Tr}\left(Y_d Y_u^\dagger Y_u Y_d^\dagger\right) \right. \\ & \left. - \text{Tr}\left(Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger\right) - 9\text{Tr}\left(Y_u Y_u^\dagger Y_u Y_u^\dagger\right) - 3\text{Tr}\left(Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger\right) \right) \end{aligned} \quad (42)$$

### 3.5 Bilinear Superpotential Parameters

$$\beta_\mu^{(1)} = -3g_2^2 \mu + 3\mu \text{Tr}\left(Y_d Y_d^\dagger\right) + 3\mu \text{Tr}\left(Y_u Y_u^\dagger\right) - \frac{3}{5}g_1^2 \mu + \mu \text{Tr}\left(Y_e Y_e^\dagger\right) + \mu \text{Tr}\left(Y_\nu Y_\nu^\dagger\right) \quad (43)$$

$$\begin{aligned} \beta_\mu^{(2)} = & \frac{1}{50}\mu \left( 207g_1^4 + 90g_1^2 g_2^2 + 375g_2^4 - 20(-40g_3^2 + g_1^2)\text{Tr}\left(Y_d Y_d^\dagger\right) + 60g_1^2 \text{Tr}\left(Y_e Y_e^\dagger\right) + 40g_1^2 \text{Tr}\left(Y_u Y_u^\dagger\right) \right. \\ & + 800g_3^2 \text{Tr}\left(Y_u Y_u^\dagger\right) - 450\text{Tr}\left(Y_d Y_d^\dagger Y_d Y_d^\dagger\right) - 300\text{Tr}\left(Y_d Y_u^\dagger Y_u Y_d^\dagger\right) - 150\text{Tr}\left(Y_e Y_e^\dagger Y_e Y_e^\dagger\right) \\ & \left. - 100\text{Tr}\left(Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger\right) - 450\text{Tr}\left(Y_u Y_u^\dagger Y_u Y_u^\dagger\right) - 150\text{Tr}\left(Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger\right) \right) \end{aligned} \quad (44)$$

$$\beta_{M_v}^{(1)} = 2 \left( M_v Y_\nu^* Y_\nu^T + Y_\nu Y_\nu^\dagger M_v \right) \quad (45)$$

$$\begin{aligned} \beta_{M_v}^{(2)} = & -2 \left( M_v Y_\nu^* Y_e^T Y_e^* Y_\nu^T + M_v Y_\nu^* Y_\nu^T Y_\nu^* Y_\nu^T + Y_\nu Y_e^\dagger Y_e Y_\nu^\dagger M_v + Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger M_v \right) \\ & + M_v Y_\nu^* Y_\nu^T \left( -2\text{Tr}\left(Y_\nu Y_\nu^\dagger\right) + 6g_2^2 - 6\text{Tr}\left(Y_u Y_u^\dagger\right) + \frac{6}{5}g_1^2 \right) \\ & + Y_\nu Y_\nu^\dagger M_v \left( -2\text{Tr}\left(Y_\nu Y_\nu^\dagger\right) + 6g_2^2 - 6\text{Tr}\left(Y_u Y_u^\dagger\right) + \frac{6}{5}g_1^2 \right) \end{aligned} \quad (46)$$

### 3.6 Trilinear Soft-Breaking Parameters

$$\begin{aligned} \beta_{T_d}^{(1)} = & +4Y_d Y_d^\dagger T_d + 2Y_d Y_u^\dagger T_u + 5T_d Y_d^\dagger Y_d + T_d Y_u^\dagger Y_u - \frac{7}{15}g_1^2 T_d - 3g_2^2 T_d - \frac{16}{3}g_3^2 T_d \\ & + 3T_d \text{Tr}(Y_d Y_d^\dagger) + T_d \text{Tr}(Y_e Y_e^\dagger) + Y_d (2\text{Tr}(Y_e^\dagger T_e) + 6g_2^2 M_2 + 6\text{Tr}(Y_d^\dagger T_d) + \frac{14}{15}g_1^2 M_1 + \frac{32}{3}g_3^2 M_3) \end{aligned} \quad (47)$$

$$\begin{aligned} \beta_{T_d}^{(2)} = & +\frac{6}{5}g_1^2 Y_d Y_d^\dagger T_d + 6g_2^2 Y_d Y_d^\dagger T_d - \frac{8}{5}g_1^2 M_1 Y_d Y_u^\dagger Y_u + \frac{8}{5}g_1^2 Y_d Y_u^\dagger T_u \\ & + \frac{6}{5}g_1^2 T_d Y_d^\dagger Y_d + 12g_2^2 T_d Y_d^\dagger Y_d + \frac{4}{5}g_1^2 T_d Y_u^\dagger Y_u - 6Y_d Y_d^\dagger Y_d Y_d^\dagger T_d \\ & - 8Y_d Y_d^\dagger T_d Y_d^\dagger Y_d - 2Y_d Y_u^\dagger Y_u Y_d^\dagger T_d - 4Y_d Y_u^\dagger Y_u Y_u^\dagger T_u - 4Y_d Y_u^\dagger T_u Y_d^\dagger Y_d \\ & - 4Y_d Y_u^\dagger T_u Y_u^\dagger Y_u - 6T_d Y_d^\dagger Y_d Y_d^\dagger Y_d - 4T_d Y_u^\dagger Y_u Y_d^\dagger Y_d - 2T_d Y_u^\dagger Y_u Y_u^\dagger Y_u \\ & + \frac{287}{90}g_1^4 T_d + g_1^2 g_2^2 T_d + \frac{15}{2}g_2^4 T_d + \frac{8}{9}g_1^2 g_3^2 T_d + 8g_2^2 g_3^2 T_d - \frac{16}{9}g_3^4 T_d \\ & - 12Y_d Y_d^\dagger T_d \text{Tr}(Y_d Y_d^\dagger) - 15T_d Y_d^\dagger Y_d \text{Tr}(Y_d Y_d^\dagger) - \frac{2}{5}g_1^2 T_d \text{Tr}(Y_d Y_d^\dagger) \\ & + 16g_3^2 T_d \text{Tr}(Y_d Y_d^\dagger) - 4Y_d Y_d^\dagger T_d \text{Tr}(Y_e Y_e^\dagger) - 5T_d Y_d^\dagger Y_d \text{Tr}(Y_e Y_e^\dagger) \\ & + \frac{6}{5}g_1^2 T_d \text{Tr}(Y_e Y_e^\dagger) - 6Y_d Y_u^\dagger T_u \text{Tr}(Y_u Y_u^\dagger) - 3T_d Y_u^\dagger Y_u \text{Tr}(Y_u Y_u^\dagger) \\ & - 2Y_d Y_u^\dagger T_u \text{Tr}(Y_\nu Y_\nu^\dagger) - T_d Y_u^\dagger Y_u \text{Tr}(Y_\nu Y_\nu^\dagger) \\ & - \frac{2}{5}Y_d Y_d^\dagger Y_d (15\text{Tr}(Y_e^\dagger T_e) + 30g_2^2 M_2 + 45\text{Tr}(Y_d^\dagger T_d) + 4g_1^2 M_1) - 6Y_d Y_u^\dagger Y_u \text{Tr}(Y_u^\dagger T_u) \\ & - 2Y_d Y_u^\dagger Y_u \text{Tr}(Y_\nu^\dagger T_\nu) - 9T_d \text{Tr}(Y_d Y_d^\dagger Y_d Y_d^\dagger) - 3T_d \text{Tr}(Y_d Y_u^\dagger Y_u Y_d^\dagger) \\ & - 3T_d \text{Tr}(Y_e Y_e^\dagger Y_e Y_e^\dagger) - T_d \text{Tr}(Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger) \\ & - \frac{2}{45}Y_d (287g_1^4 M_1 + 45g_1^2 g_2^2 M_1 + 40g_1^2 g_3^2 M_1 + 40g_1^2 g_3^2 M_3 + 360g_2^2 g_3^2 M_3 - 160g_3^4 M_3 \\ & + 45g_1^2 g_2^2 M_2 + 675g_2^4 M_2 + 360g_2^2 g_3^2 M_2 - 18(-40g_3^2 M_3 + g_1^2 M_1) \text{Tr}(Y_d Y_d^\dagger) \\ & + 54g_1^2 M_1 \text{Tr}(Y_e Y_e^\dagger) + 18g_1^2 \text{Tr}(Y_d^\dagger T_d) - 720g_3^2 \text{Tr}(Y_d^\dagger T_d) - 54g_1^2 \text{Tr}(Y_e^\dagger T_e) \\ & + 810\text{Tr}(Y_d Y_d^\dagger T_d Y_d^\dagger) + 135\text{Tr}(Y_d Y_u^\dagger T_u Y_d^\dagger) + 270\text{Tr}(Y_e Y_e^\dagger T_e Y_e^\dagger) + 45\text{Tr}(Y_e Y_\nu^\dagger T_\nu Y_e^\dagger) \\ & + 135\text{Tr}(Y_u Y_d^\dagger T_d Y_u^\dagger) + 45\text{Tr}(Y_\nu Y_e^\dagger T_e Y_\nu^\dagger)) \end{aligned} \quad (48)$$

$$\begin{aligned} \beta_{T_e}^{(1)} = & +4Y_e Y_e^\dagger T_e + 2Y_e Y_\nu^\dagger T_\nu + 5T_e Y_e^\dagger Y_e + T_e Y_\nu^\dagger Y_\nu - \frac{9}{5}g_1^2 T_e - 3g_2^2 T_e \\ & + 3T_e \text{Tr}(Y_d Y_d^\dagger) + T_e \text{Tr}(Y_e Y_e^\dagger) + Y_e (2\text{Tr}(Y_e^\dagger T_e) + 6g_2^2 M_2 + 6\text{Tr}(Y_d^\dagger T_d) + \frac{18}{5}g_1^2 M_1) \end{aligned} \quad (49)$$

$$\begin{aligned} \beta_{T_e}^{(2)} = & +\frac{6}{5}g_1^2 Y_e Y_e^\dagger T_e + 6g_2^2 Y_e Y_e^\dagger T_e - \frac{6}{5}g_1^2 T_e Y_e^\dagger Y_e + 12g_2^2 T_e Y_e^\dagger Y_e \\ & - 6Y_e Y_e^\dagger Y_e^\dagger T_e - 8Y_e Y_e^\dagger T_e Y_e^\dagger Y_e - 2Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger T_e - 4Y_e Y_\nu^\dagger Y_\nu Y_\nu^\dagger T_\nu \\ & - 4Y_e Y_\nu^\dagger T_\nu Y_e^\dagger Y_e - 4Y_e Y_\nu^\dagger T_\nu Y_\nu^\dagger Y_\nu - 6T_e Y_e^\dagger Y_e Y_e^\dagger Y_e - 4T_e Y_\nu^\dagger Y_\nu Y_e^\dagger Y_e \end{aligned}$$

$$\begin{aligned}
& -2T_e Y_\nu^\dagger Y_\nu Y_\nu^\dagger Y_\nu + \frac{27}{2} g_1^4 T_e + \frac{9}{5} g_1^2 g_2^2 T_e + \frac{15}{2} g_2^4 T_e - 12Y_e Y_e^\dagger T_e \text{Tr}(Y_d Y_d^\dagger) \\
& - 15T_e Y_e^\dagger Y_e \text{Tr}(Y_d Y_d^\dagger) - \frac{2}{5} g_1^2 T_e \text{Tr}(Y_d Y_d^\dagger) + 16g_3^2 T_e \text{Tr}(Y_d Y_d^\dagger) \\
& - 4Y_e Y_e^\dagger T_e \text{Tr}(Y_e Y_e^\dagger) - 5T_e Y_e^\dagger Y_e \text{Tr}(Y_e Y_e^\dagger) + \frac{6}{5} g_1^2 T_e \text{Tr}(Y_e Y_e^\dagger) \\
& - 6Y_e Y_\nu^\dagger T_\nu \text{Tr}(Y_u Y_u^\dagger) - 3T_e Y_\nu^\dagger Y_\nu \text{Tr}(Y_u Y_u^\dagger) - 2Y_e Y_\nu^\dagger T_\nu \text{Tr}(Y_\nu Y_\nu^\dagger) \\
& - T_e Y_\nu^\dagger Y_\nu \text{Tr}(Y_\nu Y_\nu^\dagger) - 6Y_e Y_e^\dagger Y_e (2g_2^2 M_2 + 3\text{Tr}(Y_d^\dagger T_d) + \text{Tr}(Y_e^\dagger T_e)) \\
& - 6Y_e Y_\nu^\dagger Y_\nu \text{Tr}(Y_u^\dagger T_u) - 2Y_e Y_\nu^\dagger Y_\nu \text{Tr}(Y_\nu^\dagger T_\nu) - 9T_e \text{Tr}(Y_d Y_d^\dagger Y_d Y_d^\dagger) \\
& - 3T_e \text{Tr}(Y_d Y_u^\dagger Y_u Y_d^\dagger) - 3T_e \text{Tr}(Y_e Y_e^\dagger Y_e Y_e^\dagger) - T_e \text{Tr}(Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger) \\
& - \frac{2}{5} Y_e (135g_1^4 M_1 + 9g_1^2 g_2^2 M_1 + 9g_1^2 g_2^2 M_2 + 75g_2^4 M_2 + (-2g_1^2 M_1 + 80g_3^2 M_3) \text{Tr}(Y_d Y_d^\dagger) \\
& + 6g_1^2 M_1 \text{Tr}(Y_e Y_e^\dagger) + 2g_1^2 \text{Tr}(Y_d^\dagger T_d) - 80g_3^2 \text{Tr}(Y_d^\dagger T_d) - 6g_1^2 \text{Tr}(Y_e^\dagger T_e) \\
& + 90\text{Tr}(Y_d Y_d^\dagger T_d Y_d^\dagger) + 15\text{Tr}(Y_d Y_u^\dagger T_u Y_d^\dagger) + 30\text{Tr}(Y_e Y_e^\dagger T_e Y_e^\dagger) + 5\text{Tr}(Y_e Y_\nu^\dagger T_\nu Y_e^\dagger) \\
& + 15\text{Tr}(Y_u Y_d^\dagger T_d Y_u^\dagger) + 5\text{Tr}(Y_\nu Y_e^\dagger T_e Y_\nu^\dagger)) \tag{50}
\end{aligned}$$

$$\begin{aligned}
\beta_{T_u}^{(1)} & = +2Y_u Y_d^\dagger T_d + 4Y_u Y_u^\dagger T_u + T_u Y_d^\dagger Y_d + 5T_u Y_u^\dagger Y_u - \frac{13}{15} g_1^2 T_u - 3g_2^2 T_u - \frac{16}{3} g_3^2 T_u \\
& + 3T_u \text{Tr}(Y_u Y_u^\dagger) + T_u \text{Tr}(Y_\nu Y_\nu^\dagger) + Y_u (2\text{Tr}(Y_\nu^\dagger T_\nu) + 6g_2^2 M_2 + 6\text{Tr}(Y_u^\dagger T_u) + \frac{26}{15} g_1^2 M_1 + \frac{32}{3} g_3^2 M_3) \tag{51}
\end{aligned}$$

$$\begin{aligned}
\beta_{T_u}^{(2)} & = +\frac{4}{5} g_1^2 Y_u Y_d^\dagger T_d - \frac{4}{5} g_1^2 M_1 Y_u Y_u^\dagger Y_u - 12g_2^2 M_2 Y_u Y_u^\dagger Y_u + \frac{6}{5} g_1^2 Y_u Y_u^\dagger T_u \\
& + 6g_2^2 Y_u Y_u^\dagger T_u + \frac{2}{5} g_1^2 T_u Y_d^\dagger Y_d + 12g_2^2 T_u Y_u^\dagger Y_u - 4Y_u Y_d^\dagger Y_d Y_d^\dagger T_d \\
& - 2Y_u Y_d^\dagger Y_d Y_u^\dagger T_u - 4Y_u Y_d^\dagger T_d Y_d^\dagger Y_d - 4Y_u Y_d^\dagger T_d Y_u^\dagger Y_u - 6Y_u Y_u^\dagger Y_u Y_u^\dagger T_u \\
& - 8Y_u Y_u^\dagger T_u Y_u^\dagger Y_u - 2T_u Y_d^\dagger Y_d Y_d^\dagger Y_d - 4T_u Y_d^\dagger Y_d Y_u^\dagger Y_u - 6T_u Y_u^\dagger Y_u Y_u^\dagger Y_u + \frac{2743}{450} g_1^4 T_u \\
& + g_1^2 g_2^2 T_u + \frac{15}{2} g_2^4 T_u + \frac{136}{45} g_1^2 g_3^2 T_u + 8g_2^2 g_3^2 T_u - \frac{16}{9} g_3^4 T_u - 6Y_u Y_d^\dagger T_d \text{Tr}(Y_d Y_d^\dagger) \\
& - 3T_u Y_d^\dagger Y_d \text{Tr}(Y_d Y_d^\dagger) - 2Y_u Y_d^\dagger T_d \text{Tr}(Y_e Y_e^\dagger) - T_u Y_d^\dagger Y_d \text{Tr}(Y_e Y_e^\dagger) \\
& - 12Y_u Y_u^\dagger T_u \text{Tr}(Y_u Y_u^\dagger) - 15T_u Y_u^\dagger Y_u \text{Tr}(Y_u Y_u^\dagger) + \frac{4}{5} g_1^2 T_u \text{Tr}(Y_u Y_u^\dagger) \\
& + 16g_3^2 T_u \text{Tr}(Y_u Y_u^\dagger) - 4Y_u Y_u^\dagger T_u \text{Tr}(Y_\nu Y_\nu^\dagger) - 5T_u Y_u^\dagger Y_u \text{Tr}(Y_\nu Y_\nu^\dagger) \\
& - \frac{2}{5} Y_u Y_d^\dagger Y_d (15\text{Tr}(Y_d^\dagger T_d) + 2g_1^2 M_1 + 5\text{Tr}(Y_e^\dagger T_e)) - 18Y_u Y_u^\dagger Y_u \text{Tr}(Y_u^\dagger T_u) \\
& - 6Y_u Y_u^\dagger Y_u \text{Tr}(Y_\nu^\dagger T_\nu) - 3T_u \text{Tr}(Y_d Y_u^\dagger Y_u Y_d^\dagger) - T_u \text{Tr}(Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger) \\
& - 9T_u \text{Tr}(Y_u Y_u^\dagger Y_u Y_u^\dagger) - 3T_u \text{Tr}(Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger)
\end{aligned}$$

$$\begin{aligned}
& + Y_u \left( -\frac{5486}{225} g_1^4 M_1 - 2g_1^2 g_2^2 M_1 - \frac{272}{45} g_1^2 g_3^2 M_1 - \frac{272}{45} g_1^2 g_3^2 M_3 - 16g_2^2 g_3^2 M_3 + \frac{64}{9} g_3^4 M_3 \right. \\
& \left. - 2g_1^2 g_2^2 M_2 - 30g_2^4 M_2 - 16g_2^2 g_3^2 M_2 - \frac{8}{5} (20g_3^2 M_3 + g_1^2 M_1) \text{Tr}(Y_u Y_u^\dagger) \right. \\
& \left. + \frac{8}{5} (20g_3^2 + g_1^2) \text{Tr}(Y_u^\dagger T_u) - 6 \text{Tr}(Y_d Y_u^\dagger T_u Y_d^\dagger) - 2 \text{Tr}(Y_e Y_e^\dagger T_\nu Y_e^\dagger) - 6 \text{Tr}(Y_u Y_d^\dagger T_d Y_u^\dagger) \right. \\
& \left. - 36 \text{Tr}(Y_u Y_u^\dagger T_u Y_u^\dagger) - 2 \text{Tr}(Y_\nu Y_e^\dagger T_e Y_\nu^\dagger) - 12 \text{Tr}(Y_\nu Y_\nu^\dagger T_\nu Y_\nu^\dagger) \right) \tag{52}
\end{aligned}$$

$$\begin{aligned}
\beta_{T_\nu}^{(1)} = & +2Y_\nu Y_e^\dagger T_e + 4Y_\nu Y_\nu^\dagger T_\nu + T_\nu Y_e^\dagger Y_e + 5T_\nu Y_\nu^\dagger Y_\nu - \frac{3}{5} g_1^2 T_\nu - 3g_2^2 T_\nu \\
& + 3T_\nu \text{Tr}(Y_u Y_u^\dagger) + T_\nu \text{Tr}(Y_\nu Y_\nu^\dagger) + Y_\nu \left( 2 \text{Tr}(Y_\nu^\dagger T_\nu) + 6g_2^2 M_2 + 6 \text{Tr}(Y_u^\dagger T_u) + \frac{6}{5} g_1^2 M_1 \right) \tag{53}
\end{aligned}$$

$$\begin{aligned}
\beta_{T_\nu}^{(2)} = & +\frac{12}{5} g_1^2 Y_\nu Y_e^\dagger T_e - \frac{12}{5} g_1^2 M_1 Y_\nu Y_\nu^\dagger Y_\nu - 12g_2^2 M_2 Y_\nu Y_\nu^\dagger Y_\nu + \frac{6}{5} g_1^2 Y_\nu Y_\nu^\dagger T_\nu \\
& + 6g_2^2 Y_\nu Y_\nu^\dagger T_\nu + \frac{6}{5} g_1^2 T_\nu Y_e^\dagger Y_e + \frac{12}{5} g_1^2 T_\nu Y_\nu^\dagger Y_\nu + 12g_2^2 T_\nu Y_\nu^\dagger Y_\nu \\
& - 4Y_\nu Y_e^\dagger Y_e Y_e^\dagger T_e - 2Y_\nu Y_e^\dagger Y_e Y_\nu^\dagger T_\nu - 4Y_\nu Y_e^\dagger T_e Y_e^\dagger Y_e - 4Y_\nu Y_e^\dagger T_e Y_\nu^\dagger Y_\nu \\
& - 6Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger T_\nu - 8Y_\nu Y_\nu^\dagger T_\nu Y_\nu^\dagger Y_\nu - 2T_\nu Y_e^\dagger Y_e Y_e^\dagger Y_e - 4T_\nu Y_e^\dagger Y_e Y_\nu^\dagger Y_\nu \\
& - 6T_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger Y_\nu + \frac{207}{50} g_1^4 T_\nu + \frac{9}{5} g_1^2 g_2^2 T_\nu + \frac{15}{2} g_2^4 T_\nu - 6Y_\nu Y_e^\dagger T_e \text{Tr}(Y_d Y_d^\dagger) \\
& - 3T_\nu Y_e^\dagger Y_e \text{Tr}(Y_d Y_d^\dagger) - 2Y_\nu Y_e^\dagger T_e \text{Tr}(Y_e Y_e^\dagger) - T_\nu Y_e^\dagger Y_e \text{Tr}(Y_e Y_e^\dagger) \\
& - 12Y_\nu Y_\nu^\dagger T_\nu \text{Tr}(Y_u Y_u^\dagger) - 15T_\nu Y_\nu^\dagger Y_\nu \text{Tr}(Y_u Y_u^\dagger) + \frac{4}{5} g_1^2 T_\nu \text{Tr}(Y_u Y_u^\dagger) \\
& + 16g_3^2 T_\nu \text{Tr}(Y_u Y_u^\dagger) - 4Y_\nu Y_\nu^\dagger T_\nu \text{Tr}(Y_\nu Y_\nu^\dagger) - 5T_\nu Y_\nu^\dagger Y_\nu \text{Tr}(Y_\nu Y_\nu^\dagger) \\
& - \frac{2}{5} Y_\nu Y_e^\dagger Y_e \left( 15 \text{Tr}(Y_d^\dagger T_d) + 5 \text{Tr}(Y_e^\dagger T_e) + 6g_1^2 M_1 \right) - 18Y_\nu Y_\nu^\dagger Y_\nu \text{Tr}(Y_u^\dagger T_u) \\
& - 6Y_\nu Y_\nu^\dagger Y_\nu \text{Tr}(Y_\nu^\dagger T_\nu) - 3T_\nu \text{Tr}(Y_d Y_u^\dagger Y_u Y_d^\dagger) - T_\nu \text{Tr}(Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger) \\
& - 9T_\nu \text{Tr}(Y_u Y_u^\dagger Y_u Y_u^\dagger) - 3T_\nu \text{Tr}(Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger) \\
& - \frac{2}{25} Y_\nu \left( 207g_1^4 M_1 + 45g_1^2 g_2^2 M_1 + 45g_1^2 g_2^2 M_2 + 375g_2^4 M_2 + 20(20g_3^2 M_3 + g_1^2 M_1) \text{Tr}(Y_u Y_u^\dagger) \right. \\
& \left. - 20(20g_3^2 + g_1^2) \text{Tr}(Y_u^\dagger T_u) + 75 \text{Tr}(Y_d Y_u^\dagger T_u Y_d^\dagger) + 25 \text{Tr}(Y_e Y_e^\dagger T_\nu Y_e^\dagger) \right. \\
& \left. + 75 \text{Tr}(Y_u Y_d^\dagger T_d Y_u^\dagger) + 450 \text{Tr}(Y_u Y_u^\dagger T_u Y_u^\dagger) + 25 \text{Tr}(Y_\nu Y_e^\dagger T_e Y_\nu^\dagger) + 150 \text{Tr}(Y_\nu Y_\nu^\dagger T_\nu Y_\nu^\dagger) \right) \tag{54}
\end{aligned}$$

### 3.7 Bilinear Soft-Breaking Parameters

$$\begin{aligned}
\beta_{B_\mu}^{(1)} = & +B_\mu \left( -3g_2^2 + 3 \text{Tr}(Y_d Y_d^\dagger) + 3 \text{Tr}(Y_u Y_u^\dagger) - \frac{3}{5} g_1^2 + \text{Tr}(Y_e Y_e^\dagger) + \text{Tr}(Y_\nu Y_\nu^\dagger) \right) \\
& + \frac{2}{5} \mu \left( 15g_2^2 M_2 + 15 \text{Tr}(Y_d^\dagger T_d) + 15 \text{Tr}(Y_u^\dagger T_u) + 3g_1^2 M_1 + 5 \text{Tr}(Y_e^\dagger T_e) + 5 \text{Tr}(Y_\nu^\dagger T_\nu) \right) \tag{55}
\end{aligned}$$

$$\begin{aligned}
\beta_{B_\mu}^{(2)} = & +B_\mu \left( \frac{207}{50} g_1^4 + \frac{9}{5} g_1^2 g_2^2 + \frac{15}{2} g_2^4 - \frac{2}{5} (-40g_3^2 + g_1^2) \text{Tr}(Y_d Y_d^\dagger) + \frac{6}{5} g_1^2 \text{Tr}(Y_e Y_e^\dagger) + \frac{4}{5} g_1^2 \text{Tr}(Y_u Y_u^\dagger) \right. \\
& + 16g_3^2 \text{Tr}(Y_u Y_u^\dagger) - 9 \text{Tr}(Y_d Y_d^\dagger Y_d Y_d^\dagger) - 6 \text{Tr}(Y_d Y_u^\dagger Y_u Y_d^\dagger) - 3 \text{Tr}(Y_e Y_e^\dagger Y_e Y_e^\dagger) \\
& - 2 \text{Tr}(Y_e Y_e^\dagger Y_\nu Y_\nu^\dagger) - 9 \text{Tr}(Y_u Y_u^\dagger Y_u Y_u^\dagger) - 3 \text{Tr}(Y_e Y_\nu^\dagger Y_\nu Y_\nu^\dagger) \\
& - \frac{2}{25} \mu \left( 207g_1^4 M_1 + 45g_1^2 g_2^2 M_1 + 45g_1^2 g_2^2 M_2 + 375g_2^4 M_2 - 10(-40g_3^2 M_3 + g_1^2 M_1) \right) \text{Tr}(Y_d Y_d^\dagger) \\
& + 30g_1^2 M_1 \text{Tr}(Y_e Y_e^\dagger) + 20g_1^2 M_1 \text{Tr}(Y_u Y_u^\dagger) + 400g_3^2 M_3 \text{Tr}(Y_u Y_u^\dagger) + 10g_1^2 \text{Tr}(Y_d^\dagger T_d) \\
& - 400g_3^2 \text{Tr}(Y_d^\dagger T_d) - 30g_1^2 \text{Tr}(Y_e^\dagger T_e) - 20g_1^2 \text{Tr}(Y_u^\dagger T_u) - 400g_3^2 \text{Tr}(Y_u^\dagger T_u) \\
& + 450 \text{Tr}(Y_d Y_d^\dagger T_d Y_d^\dagger) + 150 \text{Tr}(Y_d Y_u^\dagger T_u Y_d^\dagger) + 150 \text{Tr}(Y_e Y_e^\dagger T_e Y_e^\dagger) + 50 \text{Tr}(Y_e Y_\nu^\dagger T_\nu Y_e^\dagger) \\
& \left. + 150 \text{Tr}(Y_u Y_d^\dagger T_d Y_u^\dagger) + 450 \text{Tr}(Y_u Y_u^\dagger T_u Y_u^\dagger) + 50 \text{Tr}(Y_\nu Y_e^\dagger T_e Y_\nu^\dagger) + 150 \text{Tr}(Y_\nu Y_\nu^\dagger T_\nu Y_\nu^\dagger) \right) \quad (56)
\end{aligned}$$

$$\beta_{B_v}^{(1)} = 2 \left( 2M_v Y_\nu^* T_\nu^T + 2T_\nu Y_\nu^\dagger M_v + Y_\nu Y_\nu^\dagger B_v + B_v Y_\nu^* Y_\nu^T \right) \quad (57)$$

$$\begin{aligned}
\beta_{B_v}^{(2)} = & -\frac{2}{5} \left( 6g_1^2 M_1 Y_\nu Y_\nu^\dagger M_v + 30g_2^2 M_2 Y_\nu Y_\nu^\dagger M_v - 3g_1^2 Y_\nu Y_\nu^\dagger B_v - 15g_2^2 Y_\nu Y_\nu^\dagger B_v \right. \\
& - 3g_1^2 B_v Y_\nu^* Y_\nu^T - 15g_2^2 B_v Y_\nu^* Y_\nu^T - 6g_1^2 T_\nu Y_\nu^\dagger M_v - 30g_2^2 T_\nu Y_\nu^\dagger M_v \\
& + 10M_v Y_\nu^* Y_e^T Y_e^* T_\nu^T + 10M_v Y_\nu^* Y_\nu^T Y_e^* T_\nu^T + 10M_v Y_\nu^* T_e^T Y_e^* Y_\nu^T \\
& + 10M_v Y_\nu^* T_\nu^T Y_\nu^* Y_\nu^T + 5Y_\nu Y_e^\dagger Y_e Y_\nu^\dagger B_v + 10Y_\nu Y_e^\dagger T_e Y_\nu^\dagger M_v + 5Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger B_v \\
& + 10Y_\nu Y_\nu^\dagger T_\nu Y_\nu^\dagger M_v + 5B_v Y_\nu^* Y_e^T Y_e^* Y_\nu^T + 5B_v Y_\nu^* Y_\nu^T Y_e^* Y_\nu^T + 10T_\nu Y_e^\dagger Y_e Y_\nu^\dagger M_v \\
& + 10T_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger M_v + 15Y_\nu Y_\nu^\dagger B_v \text{Tr}(Y_u Y_u^\dagger) + 15B_v Y_\nu^* Y_\nu^T \text{Tr}(Y_u Y_u^\dagger) \\
& + 30T_\nu Y_\nu^\dagger M_v \text{Tr}(Y_u Y_u^\dagger) + 5Y_\nu Y_\nu^\dagger B_v \text{Tr}(Y_\nu Y_\nu^\dagger) + 5B_v Y_\nu^* Y_\nu^T \text{Tr}(Y_\nu Y_\nu^\dagger) \\
& + 10T_\nu Y_\nu^\dagger M_v \text{Tr}(Y_\nu Y_\nu^\dagger) + M_v Y_\nu^* T_\nu^T \left( 10 \text{Tr}(Y_\nu Y_\nu^\dagger) + 30 \text{Tr}(Y_u Y_u^\dagger) - 6(5g_2^2 + g_1^2) \right) \\
& + 30Y_\nu Y_\nu^\dagger M_v \text{Tr}(Y_u^\dagger T_u) + 10Y_\nu Y_\nu^\dagger M_v \text{Tr}(Y_\nu^\dagger T_\nu) \\
& \left. + 2M_v Y_\nu^* Y_\nu^T \left( 15g_2^2 M_2 + 15 \text{Tr}(Y_u^\dagger T_u) + 3g_1^2 M_1 + 5 \text{Tr}(Y_\nu^\dagger T_\nu) \right) \right) \quad (58)
\end{aligned}$$

### 3.8 Soft-Breaking Scalar Masses

$$\sigma_{1,1} = \sqrt{\frac{3}{5}} g_1 \left( -2 \text{Tr}(m_u^2) - \text{Tr}(m_l^2) - m_{H_d}^2 + m_{H_u}^2 + \text{Tr}(m_d^2) + \text{Tr}(m_e^2) + \text{Tr}(m_q^2) \right) \quad (59)$$

$$\sigma_{2,11} = \frac{1}{10} g_1^2 \left( 2 \text{Tr}(m_d^2) + 3 \text{Tr}(m_l^2) + 3m_{H_d}^2 + 3m_{H_u}^2 + 6 \text{Tr}(m_e^2) + 8 \text{Tr}(m_u^2) + \text{Tr}(m_q^2) \right) \quad (60)$$

$$\begin{aligned}
\sigma_{3,1} = & \frac{1}{20} \frac{1}{\sqrt{15}} g_1 \left( -9g_1^2 m_{H_d}^2 - 45g_2^2 m_{H_d}^2 + 9g_1^2 m_{H_u}^2 + 45g_2^2 m_{H_u}^2 + 4(20g_3^2 + g_1^2) \text{Tr}(m_d^2) + 36g_1^2 \text{Tr}(m_e^2) \right. \\
& - 9g_1^2 \text{Tr}(m_l^2) - 45g_2^2 \text{Tr}(m_l^2) + g_1^2 \text{Tr}(m_q^2) + 45g_2^2 \text{Tr}(m_q^2) + 80g_3^2 \text{Tr}(m_q^2) - 32g_1^2 \text{Tr}(m_u^2) \\
& \left. - 15g_2^2 \text{Tr}(m_u^2) + 15g_3^2 \text{Tr}(m_u^2) \right) \quad (61)
\end{aligned}$$

$$\begin{aligned}
& - 160g_3^2 \text{Tr}(m_u^2) + 90m_{H_d}^2 \text{Tr}(Y_d Y_d^\dagger) + 30m_{H_d}^2 \text{Tr}(Y_e Y_e^\dagger) - 90m_{H_u}^2 \text{Tr}(Y_u Y_u^\dagger) - 30m_{H_u}^2 \text{Tr}(Y_\nu Y_\nu^\dagger) \\
& - 60 \text{Tr}(Y_d Y_d^\dagger m_d^{2*}) - 30 \text{Tr}(Y_d m_q^{2*} Y_d^\dagger) - 60 \text{Tr}(Y_e Y_e^\dagger m_e^{2*}) + 30 \text{Tr}(Y_e m_l^{2*} Y_e^\dagger) \\
& + 120 \text{Tr}(Y_u Y_u^\dagger m_u^{2*}) - 30 \text{Tr}(Y_u m_q^{2*} Y_u^\dagger) + 30 \text{Tr}(Y_\nu m_l^{2*} Y_\nu^\dagger)
\end{aligned} \tag{61}$$

$$\sigma_{2,2} = \frac{1}{2} \left( 3 \text{Tr}(m_q^2) + m_{H_d}^2 + m_{H_u}^2 + \text{Tr}(m_l^2) \right) \tag{62}$$

$$\sigma_{2,3} = \frac{1}{2} \left( 2 \text{Tr}(m_q^2) + \text{Tr}(m_d^2) + \text{Tr}(m_u^2) \right) \tag{63}$$

$$\begin{aligned}
\beta_{m_q^2}^{(1)} = & -\frac{2}{15} g_1^2 \mathbf{1} |M_1|^2 - \frac{32}{3} g_3^2 \mathbf{1} |M_3|^2 - 6g_2^2 \mathbf{1} |M_2|^2 + 2m_{H_d}^2 Y_d^\dagger Y_d + 2m_{H_u}^2 Y_u^\dagger Y_u + 2T_d^\dagger T_d \\
& + 2T_u^\dagger T_u + m_q^2 Y_d^\dagger Y_d + m_q^2 Y_u^\dagger Y_u + 2Y_d^\dagger m_d^2 Y_d + Y_d^\dagger Y_d m_q^2 + 2Y_u^\dagger m_u^2 Y_u \\
& + Y_u^\dagger Y_u m_q^2 + \frac{1}{\sqrt{15}} g_1 \mathbf{1} \sigma_{1,1}
\end{aligned} \tag{64}$$

$$\begin{aligned}
\beta_{m_q^2}^{(2)} = & +\frac{2}{5} g_1^2 g_2^2 \mathbf{1} |M_2|^2 + 33g_2^4 \mathbf{1} |M_2|^2 + 32g_2^2 g_3^2 \mathbf{1} |M_2|^2 \\
& + \frac{16}{45} g_3^2 \left( 15 \left( 3g_2^2 (2M_3 + M_2) - 8g_3^2 M_3 \right) + g_1^2 (2M_3 + M_1) \right) \mathbf{1} M_3^* + \frac{1}{5} g_1^2 g_2^2 M_1 \mathbf{1} M_2^* + 16g_2^2 g_3^2 M_3 \mathbf{1} M_2^* \\
& + \frac{4}{5} g_1^2 m_{H_d}^2 Y_d^\dagger Y_d + \frac{8}{5} g_1^2 m_{H_u}^2 Y_u^\dagger Y_u \\
& + \frac{1}{225} g_1^2 M_1^* \left( \left( 5 \left( 16g_3^2 (2M_1 + M_3) + 9g_2^2 (2M_1 + M_2) \right) + 597g_1^2 M_1 \right) \mathbf{1} \right. \\
& \left. + 180 \left( 2M_1 Y_d^\dagger Y_d - 2Y_u^\dagger T_u + 4M_1 Y_u^\dagger Y_u - Y_d^\dagger T_d \right) \right) \\
& - \frac{4}{5} g_1^2 M_1 T_d^\dagger Y_d + \frac{4}{5} g_1^2 T_d^\dagger T_d - \frac{8}{5} g_1^2 M_1 T_u^\dagger Y_u + \frac{8}{5} g_1^2 T_u^\dagger T_u \\
& + \frac{2}{5} g_1^2 m_q^2 Y_d^\dagger Y_d + \frac{4}{5} g_1^2 m_q^2 Y_u^\dagger Y_u + \frac{4}{5} g_1^2 Y_d^\dagger m_d^2 Y_d + \frac{2}{5} g_1^2 Y_d^\dagger Y_d m_q^2 \\
& + \frac{8}{5} g_1^2 Y_u^\dagger m_u^2 Y_u + \frac{4}{5} g_1^2 Y_u^\dagger Y_u m_q^2 - 8m_{H_d}^2 Y_d^\dagger Y_d Y_d^\dagger Y_d - 4Y_d^\dagger Y_d T_d^\dagger T_d \\
& - 4Y_d^\dagger T_d T_d^\dagger Y_d - 8m_{H_u}^2 Y_u^\dagger Y_u Y_u^\dagger Y_u - 4Y_u^\dagger Y_u T_u^\dagger T_u - 4Y_u^\dagger T_u T_u^\dagger Y_u \\
& - 4T_d^\dagger Y_d Y_d^\dagger T_d - 4T_d^\dagger T_d Y_d^\dagger Y_d - 4T_u^\dagger Y_u Y_u^\dagger T_u - 4T_u^\dagger T_u Y_u^\dagger Y_u \\
& - 2m_q^2 Y_d^\dagger Y_d Y_d^\dagger Y_d - 2m_q^2 Y_u^\dagger Y_u Y_u^\dagger Y_u - 4Y_d^\dagger m_d^2 Y_d Y_d^\dagger Y_d - 4Y_d^\dagger Y_d m_q^2 Y_d^\dagger Y_d \\
& - 4Y_d^\dagger Y_d Y_d^\dagger m_d^2 Y_d - 2Y_d^\dagger Y_d Y_d^\dagger Y_d m_q^2 - 4Y_u^\dagger m_u^2 Y_u Y_u^\dagger Y_u - 4Y_u^\dagger Y_u m_q^2 Y_u^\dagger Y_u \\
& - 4Y_u^\dagger Y_u m_u^2 Y_u - 2Y_u^\dagger Y_u Y_u^\dagger Y_u m_q^2 + 6g_2^4 \mathbf{1} \sigma_{2,2} + \frac{32}{3} g_3^4 \mathbf{1} \sigma_{2,3} + \frac{2}{15} g_1^2 \mathbf{1} \sigma_{2,11} + 4 \frac{1}{\sqrt{15}} g_1 \mathbf{1} \sigma_{3,1} \\
& - 12m_{H_d}^2 Y_d^\dagger Y_d \text{Tr}(Y_d Y_d^\dagger) - 6T_d^\dagger T_d \text{Tr}(Y_d Y_d^\dagger) - 3m_q^2 Y_d^\dagger Y_d \text{Tr}(Y_d Y_d^\dagger) \\
& - 6Y_d^\dagger m_d^2 Y_d \text{Tr}(Y_d Y_d^\dagger) - 3Y_d^\dagger Y_d m_q^2 \text{Tr}(Y_d Y_d^\dagger) - 4m_{H_d}^2 Y_d^\dagger Y_d \text{Tr}(Y_e Y_e^\dagger) \\
& - 2T_d^\dagger T_d \text{Tr}(Y_e Y_e^\dagger) - m_q^2 Y_d^\dagger Y_d \text{Tr}(Y_e Y_e^\dagger) - 2Y_d^\dagger m_d^2 Y_d \text{Tr}(Y_e Y_e^\dagger)
\end{aligned}$$

$$\begin{aligned}
& - Y_d^\dagger Y_d m_q^2 \text{Tr}(Y_e Y_e^\dagger) - 12m_{H_u}^2 Y_u^\dagger Y_u \text{Tr}(Y_u Y_u^\dagger) - 6T_u^\dagger T_u \text{Tr}(Y_u Y_u^\dagger) \\
& - 3m_q^2 Y_u^\dagger Y_u \text{Tr}(Y_u Y_u^\dagger) - 6Y_u^\dagger m_u^2 Y_u \text{Tr}(Y_u Y_u^\dagger) - 3Y_u^\dagger Y_u m_q^2 \text{Tr}(Y_u Y_u^\dagger) \\
& - 4m_{H_u}^2 Y_u^\dagger Y_u \text{Tr}(Y_\nu Y_\nu^\dagger) - 2T_u^\dagger T_u \text{Tr}(Y_\nu Y_\nu^\dagger) - m_q^2 Y_u^\dagger Y_u \text{Tr}(Y_\nu Y_\nu^\dagger) \\
& - 2Y_u^\dagger m_u^2 Y_u \text{Tr}(Y_\nu Y_\nu^\dagger) - Y_u^\dagger Y_u m_q^2 \text{Tr}(Y_\nu Y_\nu^\dagger) - 6T_d^\dagger Y_d \text{Tr}(Y_d^\dagger T_d) \\
& - 2T_d^\dagger Y_d \text{Tr}(Y_e^\dagger T_e) - 6T_u^\dagger Y_u \text{Tr}(Y_u^\dagger T_u) - 2T_u^\dagger Y_u \text{Tr}(Y_\nu^\dagger T_\nu) \\
& - 6Y_d^\dagger T_d \text{Tr}(T_d^* Y_d^T) - 6Y_d^\dagger Y_d \text{Tr}(T_d^* T_d^T) - 2Y_d^\dagger T_d \text{Tr}(T_e^* Y_e^T) \\
& - 2Y_d^\dagger Y_d \text{Tr}(T_e^* T_e^T) - 6Y_u^\dagger T_u \text{Tr}(T_u^* Y_u^T) - 6Y_u^\dagger Y_u \text{Tr}(T_u^* T_u^T) \\
& - 2Y_u^\dagger T_u \text{Tr}(T_\nu^* Y_\nu^T) - 2Y_u^\dagger Y_u \text{Tr}(T_\nu^* T_\nu^T) - 6Y_d^\dagger Y_d \text{Tr}(m_d^2 Y_d Y_d^\dagger) \\
& - 2Y_d^\dagger Y_d \text{Tr}(m_e^2 Y_e Y_e^\dagger) - 2Y_d^\dagger Y_d \text{Tr}(m_l^2 Y_e^\dagger Y_e) - 2Y_u^\dagger Y_u \text{Tr}(m_l^2 Y_\nu^\dagger Y_\nu) \\
& - 6Y_d^\dagger Y_d \text{Tr}(m_q^2 Y_d^\dagger Y_d) - 6Y_u^\dagger Y_u \text{Tr}(m_q^2 Y_u^\dagger Y_u) - 6Y_u^\dagger Y_u \text{Tr}(m_u^2 Y_u Y_u^\dagger) \\
& - 2Y_u^\dagger Y_u \text{Tr}(Y_\nu Y_\nu^\dagger m_\nu^{2*}) \tag{65}
\end{aligned}$$

$$\begin{aligned}
\beta_{m_l^2}^{(1)} = & -\frac{6}{5}g_1^2 \mathbf{1}|M_1|^2 - 6g_2^2 \mathbf{1}|M_2|^2 + 2m_{H_d}^2 Y_e^\dagger Y_e + 2m_{H_u}^2 Y_\nu^\dagger Y_\nu + 2T_e^\dagger T_e + 2T_\nu^\dagger T_\nu \\
& + m_l^2 Y_e^\dagger Y_e + m_l^2 Y_\nu^\dagger Y_\nu + 2Y_e^\dagger m_e^2 Y_e + Y_e^\dagger Y_e m_l^2 + Y_\nu^\dagger Y_\nu m_l^2 + 2Y_\nu^\dagger m_\nu^{2*} Y_\nu \\
& - \sqrt{\frac{3}{5}}g_1 \mathbf{1}\sigma_{1,1} \tag{66}
\end{aligned}$$

$$\begin{aligned}
\beta_{m_l^2}^{(2)} = & +\frac{3}{5}g_2^2 \left( 3g_1^2 (2M_2 + M_1) + 55g_2^2 M_2 \right) \mathbf{1}M_2^* + \frac{12}{5}g_1^2 m_{H_d}^2 Y_e^\dagger Y_e \\
& + \frac{3}{25}g_1^2 M_2^* \left( -20Y_e^\dagger T_e + 3(5g_2^2 (2M_1 + M_2) + 69g_1^2 M_1) \mathbf{1} + 40M_1 Y_e^\dagger Y_e \right) - \frac{12}{5}g_1^2 M_1 T_e^\dagger Y_e \\
& + \frac{12}{5}g_1^2 T_e^\dagger T_e + \frac{6}{5}g_1^2 m_l^2 Y_e^\dagger Y_e + \frac{12}{5}g_1^2 Y_e^\dagger m_e^2 Y_e + \frac{6}{5}g_1^2 Y_e^\dagger Y_e m_l^2 \\
& - 8m_{H_d}^2 Y_e^\dagger Y_e T_e^\dagger Y_e - 4Y_e^\dagger Y_e T_e^\dagger T_e - 4Y_e^\dagger T_e T_e^\dagger Y_e - 8m_{H_u}^2 Y_\nu^\dagger Y_\nu Y_\nu^\dagger Y_\nu \\
& - 4Y_\nu^\dagger Y_\nu T_\nu^\dagger T_\nu - 4Y_\nu^\dagger T_\nu T_\nu^\dagger Y_\nu - 4T_e^\dagger Y_e Y_e^\dagger T_e - 4T_e^\dagger T_e Y_e^\dagger Y_e \\
& - 4T_\nu^\dagger Y_\nu Y_\nu^\dagger T_\nu - 4T_\nu^\dagger T_\nu Y_\nu^\dagger Y_\nu - 2m_l^2 Y_e^\dagger Y_e Y_e^\dagger Y_e - 2m_l^2 Y_\nu^\dagger Y_\nu Y_\nu^\dagger Y_\nu \\
& - 4Y_e^\dagger m_e^2 Y_e^\dagger Y_e - 4Y_e^\dagger Y_e m_l^2 Y_e^\dagger Y_e - 4Y_e^\dagger Y_e Y_e^\dagger m_e^2 Y_e - 2Y_e^\dagger Y_e Y_e^\dagger Y_e m_l^2 \\
& - 4Y_\nu^\dagger Y_\nu m_l^2 Y_\nu^\dagger Y_\nu - 2Y_\nu^\dagger Y_\nu Y_\nu^\dagger Y_\nu m_l^2 - 4Y_\nu^\dagger Y_\nu Y_\nu^\dagger m_\nu^{2*} Y_\nu - 4Y_\nu^\dagger m_\nu^{2*} Y_\nu Y_\nu^\dagger Y_\nu + 6g_2^4 \mathbf{1}\sigma_{2,2} \\
& + \frac{6}{5}g_1^2 \mathbf{1}\sigma_{2,11} - 4\sqrt{\frac{3}{5}}g_1 \mathbf{1}\sigma_{3,1} - 12m_{H_d}^2 Y_e^\dagger Y_e \text{Tr}(Y_d Y_d^\dagger) - 6T_e^\dagger T_e \text{Tr}(Y_d Y_d^\dagger) \\
& - 3m_l^2 Y_e^\dagger Y_e \text{Tr}(Y_d Y_d^\dagger) - 6Y_e^\dagger m_e^2 Y_e \text{Tr}(Y_d Y_d^\dagger) - 3Y_e^\dagger Y_e m_l^2 \text{Tr}(Y_d Y_d^\dagger) \\
& - 4m_{H_d}^2 Y_e^\dagger Y_e \text{Tr}(Y_e Y_e^\dagger) - 2T_e^\dagger T_e \text{Tr}(Y_e Y_e^\dagger) - m_l^2 Y_e^\dagger Y_e \text{Tr}(Y_e Y_e^\dagger)
\end{aligned}$$

$$\begin{aligned}
& -2Y_e^\dagger m_e^2 Y_e \text{Tr}(Y_e Y_e^\dagger) - Y_e^\dagger Y_e m_l^2 \text{Tr}(Y_e Y_e^\dagger) - 12m_{H_u}^2 Y_\nu^\dagger Y_\nu \text{Tr}(Y_u Y_u^\dagger) \\
& - 6T_\nu^\dagger T_\nu \text{Tr}(Y_u Y_u^\dagger) - 3m_l^2 Y_\nu^\dagger Y_\nu \text{Tr}(Y_u Y_u^\dagger) - 3Y_\nu^\dagger Y_\nu m_l^2 \text{Tr}(Y_u Y_u^\dagger) \\
& - 6Y_\nu^\dagger m_\nu^{2*} Y_\nu \text{Tr}(Y_u Y_u^\dagger) - 4m_{H_u}^2 Y_\nu^\dagger Y_\nu \text{Tr}(Y_\nu Y_\nu^\dagger) - 2T_\nu^\dagger T_\nu \text{Tr}(Y_\nu Y_\nu^\dagger) \\
& - m_l^2 Y_\nu^\dagger Y_\nu \text{Tr}(Y_\nu Y_\nu^\dagger) - Y_\nu^\dagger Y_\nu m_l^2 \text{Tr}(Y_\nu Y_\nu^\dagger) - 2Y_\nu^\dagger m_\nu^{2*} Y_\nu \text{Tr}(Y_\nu Y_\nu^\dagger) \\
& - 6T_e^\dagger Y_e \text{Tr}(Y_d^\dagger T_d) - 2T_e^\dagger Y_e \text{Tr}(Y_e^\dagger T_e) - 6T_\nu^\dagger Y_\nu \text{Tr}(Y_u^\dagger T_u) \\
& - 2T_\nu^\dagger Y_\nu \text{Tr}(Y_\nu^\dagger T_\nu) - 6Y_e^\dagger T_e \text{Tr}(T_d^* Y_d^T) - 6Y_e^\dagger Y_e \text{Tr}(T_d^* T_d^T) \\
& - 2Y_e^\dagger T_e \text{Tr}(T_e^* Y_e^T) - 2Y_e^\dagger Y_e \text{Tr}(T_e^* T_e^T) - 6Y_\nu^\dagger T_\nu \text{Tr}(T_u^* Y_u^T) \\
& - 6Y_\nu^\dagger Y_\nu \text{Tr}(T_u^* T_u^T) - 2Y_\nu^\dagger T_\nu \text{Tr}(T_\nu^* Y_\nu^T) - 2Y_\nu^\dagger Y_\nu \text{Tr}(T_\nu^* T_\nu^T) \\
& - 6Y_e^\dagger Y_e \text{Tr}(m_d^2 Y_d Y_d^\dagger) - 2Y_e^\dagger Y_e \text{Tr}(m_e^2 Y_e Y_e^\dagger) - 2Y_e^\dagger Y_e \text{Tr}(m_l^2 Y_e^\dagger Y_e) \\
& - 2Y_\nu^\dagger Y_\nu \text{Tr}(m_l^2 Y_\nu^\dagger Y_\nu) - 6Y_e^\dagger Y_e \text{Tr}(m_q^2 Y_d^\dagger Y_d) - 6Y_\nu^\dagger Y_\nu \text{Tr}(m_q^2 Y_u^\dagger Y_u) \\
& - 6Y_\nu^\dagger Y_\nu \text{Tr}(m_u^2 Y_u Y_u^\dagger) - 2Y_\nu^\dagger Y_\nu \text{Tr}(Y_\nu Y_\nu^\dagger m_\nu^{2*}) \tag{67}
\end{aligned}$$

$$\begin{aligned}
\beta_{m_{H_d}^2}^{(1)} &= -\frac{6}{5}g_1^2|M_1|^2 - 6g_2^2|M_2|^2 - \sqrt{\frac{3}{5}}g_1\sigma_{1,1} + 6m_{H_d}^2 \text{Tr}(Y_d Y_d^\dagger) + 2m_{H_d}^2 \text{Tr}(Y_e Y_e^\dagger) + 6\text{Tr}(T_d^* T_d^T) \\
& + 2\text{Tr}(T_e^* T_e^T) + 6\text{Tr}(m_d^2 Y_d Y_d^\dagger) + 2\text{Tr}(m_e^2 Y_e Y_e^\dagger) + 2\text{Tr}(m_l^2 Y_e^\dagger Y_e) + 6\text{Tr}(m_q^2 Y_d^\dagger Y_d) \tag{68}
\end{aligned}$$

$$\begin{aligned}
\beta_{m_{H_d}^2}^{(2)} &= \frac{1}{25} \left( 15g_2^2 \left( 3g_1^2 (2M_2 + M_1) + 55g_2^2 M_2 \right) M_2^* \right. \\
& + g_1^2 M_1^* \left( 621g_1^2 M_1 + 90g_2^2 M_1 + 45g_2^2 M_2 - 40M_1 \text{Tr}(Y_d Y_d^\dagger) + 120M_1 \text{Tr}(Y_e Y_e^\dagger) + 20\text{Tr}(Y_d^\dagger T_d) \right. \\
& \left. \left. - 60\text{Tr}(Y_e^\dagger T_e) \right) \right) \\
& + 10 \left( 15g_2^4 \sigma_{2,2} + 3g_1^2 \sigma_{2,11} - 2\sqrt{15}g_1 \sigma_{3,1} + \left( 160g_3^2 |M_3|^2 - 2g_1^2 m_{H_d}^2 + 80g_3^2 m_{H_d}^2 \right) \text{Tr}(Y_d Y_d^\dagger) \right. \\
& + 6g_1^2 m_{H_d}^2 \text{Tr}(Y_e Y_e^\dagger) - 80g_3^2 M_3^* \text{Tr}(Y_d^\dagger T_d) + 2g_1^2 M_1 \text{Tr}(T_d^* Y_d^T) - 80g_3^2 M_3 \text{Tr}(T_d^* Y_d^T) \\
& - 2g_1^2 \text{Tr}(T_d^* T_d^T) + 80g_3^2 \text{Tr}(T_d^* T_d^T) - 6g_1^2 M_1 \text{Tr}(T_e^* Y_e^T) + 6g_1^2 \text{Tr}(T_e^* T_e^T) \\
& - 2g_1^2 \text{Tr}(m_d^2 Y_d Y_d^\dagger) + 80g_3^2 \text{Tr}(m_d^2 Y_d Y_d^\dagger) + 6g_1^2 \text{Tr}(m_e^2 Y_e Y_e^\dagger) + 6g_1^2 \text{Tr}(m_l^2 Y_e^\dagger Y_e) \\
& - 2g_1^2 \text{Tr}(m_q^2 Y_d^\dagger Y_d) + 80g_3^2 \text{Tr}(m_q^2 Y_d^\dagger Y_d) - 90m_{H_d}^2 \text{Tr}(Y_d Y_d^\dagger Y_d Y_d^\dagger) - 90\text{Tr}(Y_d Y_d^\dagger T_d T_d^\dagger) \\
& - 15m_{H_d}^2 \text{Tr}(Y_d Y_u^\dagger Y_u Y_d^\dagger) - 15m_{H_u}^2 \text{Tr}(Y_d Y_u^\dagger Y_u Y_d^\dagger) - 15\text{Tr}(Y_d Y_u^\dagger T_u T_d^\dagger) \\
& - 90\text{Tr}(Y_d T_d^\dagger T_d Y_d^\dagger) - 15\text{Tr}(Y_d T_u^\dagger T_u Y_d^\dagger) - 30m_{H_d}^2 \text{Tr}(Y_e Y_e^\dagger Y_e Y_e^\dagger) - 30\text{Tr}(Y_e Y_e^\dagger T_e T_e^\dagger) \\
& \left. - 5m_{H_d}^2 \text{Tr}(Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger) - 5m_{H_u}^2 \text{Tr}(Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger) - 5\text{Tr}(Y_e Y_\nu^\dagger T_\nu T_e^\dagger) \right)
\end{aligned}$$

$$\begin{aligned}
& -30\text{Tr}\left(Y_e T_e^\dagger T_e Y_e^\dagger\right) - 5\text{Tr}\left(Y_e T_\nu^\dagger T_\nu Y_e^\dagger\right) - 15\text{Tr}\left(Y_u Y_d^\dagger T_d T_u^\dagger\right) - 15\text{Tr}\left(Y_u T_d^\dagger T_d Y_u^\dagger\right) \\
& - 5\text{Tr}\left(Y_\nu Y_e^\dagger T_e T_\nu^\dagger\right) - 5\text{Tr}\left(Y_\nu T_e^\dagger T_e Y_\nu^\dagger\right) - 90\text{Tr}\left(m_d^2 Y_d Y_d^\dagger Y_d Y_d^\dagger\right) \\
& - 15\text{Tr}\left(m_d^2 Y_d Y_u^\dagger Y_u Y_d^\dagger\right) - 30\text{Tr}\left(m_e^2 Y_e Y_e^\dagger Y_e Y_e^\dagger\right) - 5\text{Tr}\left(m_e^2 Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger\right) \\
& - 30\text{Tr}\left(m_l^2 Y_e^\dagger Y_e Y_e^\dagger Y_e\right) - 5\text{Tr}\left(m_l^2 Y_e^\dagger Y_e Y_\nu^\dagger Y_\nu\right) - 5\text{Tr}\left(m_l^2 Y_\nu^\dagger Y_\nu Y_e^\dagger Y_e\right) \\
& - 90\text{Tr}\left(m_q^2 Y_d^\dagger Y_d Y_d^\dagger Y_d\right) - 15\text{Tr}\left(m_q^2 Y_d^\dagger Y_d Y_u^\dagger Y_u\right) - 15\text{Tr}\left(m_q^2 Y_u^\dagger Y_u Y_d^\dagger Y_d\right) \\
& - 15\text{Tr}\left(m_u^2 Y_u^\dagger Y_d Y_d^\dagger Y_u\right) - 5\text{Tr}\left(Y_e Y_\nu^\dagger m_\nu^{2*} Y_\nu Y_e^\dagger\right) \quad (69)
\end{aligned}$$

$$\begin{aligned}
\beta_{m_{H_u}^2}^{(1)} = & -\frac{6}{5}g_1^2|M_1|^2 - 6g_2^2|M_2|^2 + \sqrt{\frac{3}{5}}g_1\sigma_{1,1} + 6m_{H_u}^2\text{Tr}\left(Y_u Y_u^\dagger\right) + 2m_{H_u}^2\text{Tr}\left(Y_\nu Y_\nu^\dagger\right) + 6\text{Tr}\left(T_u^* T_u^T\right) \\
& + 2\text{Tr}\left(T_\nu^* T_\nu^T\right) + 2\text{Tr}\left(m_l^2 Y_\nu^\dagger Y_\nu\right) + 6\text{Tr}\left(m_q^2 Y_u^\dagger Y_u\right) + 6\text{Tr}\left(m_u^2 Y_u^\dagger Y_u\right) + 2\text{Tr}\left(Y_\nu Y_\nu^\dagger m_\nu^{2*}\right) \quad (70)
\end{aligned}$$

$$\begin{aligned}
\beta_{m_{H_u}^2}^{(2)} = & +\frac{3}{5}g_2^2\left(3g_1^2\left(2M_2 + M_1\right) + 55g_2^2M_2\right)M_2^* + 6g_2^4\sigma_{2,2} + \frac{6}{5}g_1^2\sigma_{2,11} + 4\sqrt{\frac{3}{5}}g_1\sigma_{3,1} + \frac{8}{5}g_1^2m_{H_u}^2\text{Tr}\left(Y_u Y_u^\dagger\right) \\
& + 32g_3^2m_{H_u}^2\text{Tr}\left(Y_u Y_u^\dagger\right) + 64g_3^2|M_3|^2\text{Tr}\left(Y_u Y_u^\dagger\right) \\
& + \frac{1}{25}g_1^2M_1^*\left(-40\text{Tr}\left(Y_u^\dagger T_u\right) + 45g_2^2M_2 + 621g_1^2M_1 + 80M_1\text{Tr}\left(Y_u Y_u^\dagger\right) + 90g_2^2M_1\right) \\
& - 32g_3^2M_3^*\text{Tr}\left(Y_u^\dagger T_u\right) - \frac{8}{5}g_1^2M_1\text{Tr}\left(T_u^* Y_u^T\right) - 32g_3^2M_3\text{Tr}\left(T_u^* Y_u^T\right) + \frac{8}{5}g_1^2\text{Tr}\left(T_u^* T_u^T\right) \\
& + 32g_3^2\text{Tr}\left(T_u^* T_u^T\right) + \frac{8}{5}g_1^2\text{Tr}\left(m_q^2 Y_u^\dagger Y_u\right) + 32g_3^2\text{Tr}\left(m_q^2 Y_u^\dagger Y_u\right) + \frac{8}{5}g_1^2\text{Tr}\left(m_u^2 Y_u^\dagger Y_u\right) \\
& + 32g_3^2\text{Tr}\left(m_u^2 Y_u^\dagger Y_u\right) - 6m_{H_d}^2\text{Tr}\left(Y_d Y_u^\dagger Y_u Y_d^\dagger\right) - 6m_{H_u}^2\text{Tr}\left(Y_d Y_u^\dagger Y_u Y_d^\dagger\right) \\
& - 6\text{Tr}\left(Y_d Y_u^\dagger T_u T_d^\dagger\right) - 6\text{Tr}\left(Y_d T_u^\dagger T_u Y_d^\dagger\right) - 2m_{H_d}^2\text{Tr}\left(Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger\right) \\
& - 2m_{H_u}^2\text{Tr}\left(Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger\right) - 2\text{Tr}\left(Y_e Y_\nu^\dagger T_\nu T_e^\dagger\right) - 2\text{Tr}\left(Y_e T_\nu^\dagger T_\nu Y_e^\dagger\right) \\
& - 6\text{Tr}\left(Y_u Y_d^\dagger T_d T_u^\dagger\right) - 36m_{H_u}^2\text{Tr}\left(Y_u Y_u^\dagger Y_u Y_u^\dagger\right) - 36\text{Tr}\left(Y_u Y_u^\dagger T_u T_u^\dagger\right) - 6\text{Tr}\left(Y_u T_d^\dagger T_d Y_u^\dagger\right) \\
& - 36\text{Tr}\left(Y_u T_u^\dagger T_u Y_u^\dagger\right) - 2\text{Tr}\left(Y_\nu Y_e^\dagger T_e T_\nu^\dagger\right) - 12m_{H_u}^2\text{Tr}\left(Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger\right) - 12\text{Tr}\left(Y_\nu Y_\nu^\dagger T_\nu T_\nu^\dagger\right) \\
& - 2\text{Tr}\left(Y_\nu T_e^\dagger T_e Y_\nu^\dagger\right) - 12\text{Tr}\left(Y_\nu T_\nu^\dagger T_\nu Y_\nu^\dagger\right) - 6\text{Tr}\left(m_d^2 Y_d Y_u^\dagger Y_u Y_d^\dagger\right) \\
& - 2\text{Tr}\left(m_e^2 Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger\right) - 2\text{Tr}\left(m_l^2 Y_e^\dagger Y_e Y_\nu^\dagger Y_\nu\right) - 2\text{Tr}\left(m_l^2 Y_\nu^\dagger Y_\nu Y_e^\dagger Y_e\right) \\
& - 12\text{Tr}\left(m_l^2 Y_\nu^\dagger Y_\nu Y_\nu^\dagger Y_\nu\right) - 6\text{Tr}\left(m_q^2 Y_d^\dagger Y_d Y_u^\dagger Y_u\right) - 6\text{Tr}\left(m_q^2 Y_u^\dagger Y_u Y_d^\dagger Y_d\right) \\
& - 36\text{Tr}\left(m_q^2 Y_u^\dagger Y_u Y_u^\dagger Y_u\right) - 6\text{Tr}\left(m_u^2 Y_u Y_d^\dagger Y_d Y_u^\dagger\right) - 36\text{Tr}\left(m_u^2 Y_u Y_u^\dagger Y_u Y_u^\dagger\right) \\
& - 2\text{Tr}\left(Y_e Y_\nu^\dagger m_\nu^{2*} Y_\nu Y_e^\dagger\right) - 6\text{Tr}\left(Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger m_\nu^{2*}\right) - 6\text{Tr}\left(Y_\nu Y_\nu^\dagger m_\nu^{2*} Y_\nu Y_\nu^\dagger\right) \quad (71)
\end{aligned}$$

$$\beta_{m_d^2}^{(1)} = -\frac{8}{15}g_1^2\mathbf{1}|M_1|^2 - \frac{32}{3}g_3^2\mathbf{1}|M_3|^2 + 4m_{H_d}^2 Y_d Y_d^\dagger + 4T_d T_d^\dagger + 2m_d^2 Y_d Y_d^\dagger + 4Y_d m_q^2 Y_d^\dagger$$

$$+ 2Y_d Y_d^\dagger m_d^2 + 2 \frac{1}{\sqrt{15}} g_1 \mathbf{1} \sigma_{1,1} \quad (72)$$

$$\begin{aligned} \beta_{m_d^2}^{(2)} = & + \frac{64}{45} g_3^2 \left( -30g_3^2 M_3 + g_1^2 (2M_3 + M_1) \right) \mathbf{1} M_3^* + \frac{4}{5} g_1^2 m_{H_d}^2 Y_d Y_d^\dagger + 12g_2^2 m_{H_d}^2 Y_d Y_d^\dagger \\ & + 24g_2^2 |M_2|^2 Y_d Y_d^\dagger - \frac{4}{5} g_1^2 M_1 Y_d T_d^\dagger - 12g_2^2 M_2 Y_d T_d^\dagger \\ & + \frac{4}{225} g_1^2 M_1^* \left( 2(303g_1^2 M_1 + 40g_3^2 (2M_1 + M_3)) \mathbf{1} - 45T_d Y_d^\dagger + 90M_1 Y_d Y_d^\dagger \right) - 12g_2^2 M_2^* T_d Y_d^\dagger \\ & + \frac{4}{5} g_1^2 T_d T_d^\dagger + 12g_2^2 T_d T_d^\dagger + \frac{2}{5} g_1^2 m_d^2 Y_d Y_d^\dagger + 6g_2^2 m_d^2 Y_d Y_d^\dagger \\ & + \frac{4}{5} g_1^2 Y_d m_q^2 Y_d^\dagger + 12g_2^2 Y_d m_q^2 Y_d^\dagger + \frac{2}{5} g_1^2 Y_d Y_d^\dagger m_d^2 + 6g_2^2 Y_d Y_d^\dagger m_d^2 \\ & - 8m_{H_d}^2 Y_d Y_d^\dagger Y_d Y_d^\dagger - 4Y_d Y_d^\dagger T_d T_d^\dagger - 4m_{H_d}^2 Y_d Y_u^\dagger Y_u Y_d^\dagger \\ & - 4m_{H_u}^2 Y_d Y_u^\dagger Y_u Y_d^\dagger - 4Y_d Y_u^\dagger T_u T_d^\dagger - 4Y_d T_d^\dagger T_d Y_d^\dagger - 4Y_d T_u^\dagger T_u Y_d^\dagger \\ & - 4T_d Y_d^\dagger Y_d T_d^\dagger - 4T_d Y_u^\dagger Y_u T_d^\dagger - 4T_d T_d^\dagger Y_d Y_d^\dagger - 4T_d T_u^\dagger Y_u Y_d^\dagger \\ & - 2m_d^2 Y_d Y_d^\dagger Y_d Y_d^\dagger - 2m_d^2 Y_d Y_u^\dagger Y_u Y_d^\dagger - 4Y_d m_q^2 Y_d^\dagger Y_d Y_d^\dagger - 4Y_d m_q^2 Y_u^\dagger Y_u Y_d^\dagger \\ & - 4Y_d Y_d^\dagger m_d^2 Y_d Y_d^\dagger - 4Y_d Y_d^\dagger Y_d m_q^2 Y_d^\dagger - 2Y_d Y_d^\dagger Y_d Y_d^\dagger m_d^2 - 4Y_d Y_u^\dagger m_u^2 Y_u Y_d^\dagger \\ & - 4Y_d Y_u^\dagger m_q^2 Y_d^\dagger - 2Y_d Y_u^\dagger Y_u T_d^\dagger m_d^2 + \frac{32}{3} g_3^4 \mathbf{1} \sigma_{2,3} + \frac{8}{15} g_1^2 \mathbf{1} \sigma_{2,11} + 8 \frac{1}{\sqrt{15}} g_1 \mathbf{1} \sigma_{3,1} \\ & - 24m_{H_d}^2 Y_d Y_d^\dagger \text{Tr}(Y_d Y_d^\dagger) - 12T_d T_d^\dagger \text{Tr}(Y_d Y_d^\dagger) - 6m_d^2 Y_d Y_d^\dagger \text{Tr}(Y_d Y_d^\dagger) \\ & - 12Y_d m_q^2 Y_d^\dagger \text{Tr}(Y_d Y_d^\dagger) - 6Y_d Y_d^\dagger m_d^2 \text{Tr}(Y_d Y_d^\dagger) - 8m_{H_d}^2 Y_d Y_d^\dagger \text{Tr}(Y_e Y_e^\dagger) \\ & - 4T_d T_d^\dagger \text{Tr}(Y_e Y_e^\dagger) - 2m_d^2 Y_d Y_d^\dagger \text{Tr}(Y_e Y_e^\dagger) - 4Y_d m_q^2 Y_d^\dagger \text{Tr}(Y_e Y_e^\dagger) \\ & - 2Y_d Y_d^\dagger m_d^2 \text{Tr}(Y_e Y_e^\dagger) - 12Y_d T_d^\dagger \text{Tr}(Y_d^\dagger T_d) - 4Y_d T_d^\dagger \text{Tr}(Y_e^\dagger T_e) \\ & - 12T_d Y_d^\dagger \text{Tr}(T_d^* Y_d^T) - 12Y_d Y_d^\dagger \text{Tr}(T_d^* T_d^T) - 4T_d Y_d^\dagger \text{Tr}(T_e^* Y_e^T) \\ & - 4Y_d Y_d^\dagger \text{Tr}(T_e^* T_e^T) - 12Y_d Y_d^\dagger \text{Tr}(m_d^2 Y_d Y_d^\dagger) - 4Y_d Y_d^\dagger \text{Tr}(m_e^2 Y_e Y_e^\dagger) \\ & - 4Y_d Y_d^\dagger \text{Tr}(m_l^2 Y_e^\dagger Y_e) - 12Y_d Y_d^\dagger \text{Tr}(m_q^2 Y_d^\dagger Y_d) \end{aligned} \quad (73)$$

$$\begin{aligned} \beta_{m_u^2}^{(1)} = & - \frac{32}{15} g_1^2 \mathbf{1} |M_1|^2 - \frac{32}{3} g_3^2 \mathbf{1} |M_3|^2 + 4m_{H_u}^2 Y_u Y_u^\dagger + 4T_u T_u^\dagger + 2m_u^2 Y_u Y_u^\dagger + 4Y_u m_q^2 Y_u^\dagger \\ & + 2Y_u Y_u^\dagger m_u^2 - 4 \frac{1}{\sqrt{15}} g_1 \mathbf{1} \sigma_{1,1} \end{aligned} \quad (74)$$

$$\begin{aligned} \beta_{m_u^2}^{(2)} = & - \frac{128}{45} g_3^2 \left( 15g_3^2 M_3 - 2g_1^2 (2M_3 + M_1) \right) \mathbf{1} M_3^* - \frac{4}{5} g_1^2 m_{H_u}^2 Y_u Y_u^\dagger + 12g_2^2 m_{H_u}^2 Y_u Y_u^\dagger \\ & + 24g_2^2 |M_2|^2 Y_u Y_u^\dagger + \frac{4}{5} g_1^2 M_1 Y_u T_u^\dagger - 12g_2^2 M_2 Y_u T_u^\dagger - 12g_2^2 M_2^* T_u Y_u^\dagger \\ & + \frac{4}{225} g_1^2 M_1^* \left( 45 \left( -2M_1 Y_u Y_u^\dagger + T_u Y_u^\dagger \right) + 8 \left( 321g_1^2 M_1 + 40g_3^2 (2M_1 + M_3) \right) \mathbf{1} \right) - \frac{4}{5} g_1^2 T_u T_u^\dagger \end{aligned}$$

$$\begin{aligned}
& + 12g_2^2 T_u T_u^\dagger - \frac{2}{5} g_1^2 m_u^2 Y_u Y_u^\dagger + 6g_2^2 m_u^2 Y_u Y_u^\dagger - \frac{4}{5} g_1^2 Y_u m_q^2 Y_u^\dagger \\
& + 12g_2^2 Y_u m_q^2 Y_u^\dagger - \frac{2}{5} g_1^2 Y_u Y_u^\dagger m_u^2 + 6g_2^2 Y_u Y_u^\dagger m_u^2 - 4m_{H_d}^2 Y_u Y_d^\dagger Y_d Y_u^\dagger \\
& - 4m_{H_u}^2 Y_u Y_d^\dagger Y_d Y_u^\dagger - 4Y_u Y_d^\dagger T_d T_u^\dagger - 8m_{H_u}^2 Y_u Y_u^\dagger Y_u Y_u^\dagger - 4Y_u Y_u^\dagger T_u T_u^\dagger \\
& - 4Y_u T_d^\dagger T_d Y_u^\dagger - 4Y_u T_u^\dagger T_u Y_u^\dagger - 4T_u Y_d^\dagger Y_d T_u^\dagger - 4T_u Y_u^\dagger Y_u T_u^\dagger \\
& - 4T_u T_d^\dagger Y_d Y_u^\dagger - 4T_u T_u^\dagger Y_u Y_u^\dagger - 2m_u^2 Y_u Y_d^\dagger Y_d Y_u^\dagger - 2m_u^2 Y_u Y_u^\dagger Y_u Y_u^\dagger \\
& - 4Y_u m_q^2 Y_d Y_u^\dagger - 4Y_u m_q^2 Y_u^\dagger Y_u Y_u^\dagger - 4Y_u Y_d^\dagger m_d^2 Y_d Y_u^\dagger \\
& - 4Y_u Y_d^\dagger Y_d m_q^2 Y_u^\dagger - 2Y_u Y_d^\dagger Y_d Y_u^\dagger m_u^2 - 4Y_u Y_u^\dagger m_u^2 Y_u Y_u^\dagger - 4Y_u Y_u^\dagger Y_u m_q^2 Y_u^\dagger \\
& - 2Y_u Y_u^\dagger Y_u Y_u^\dagger m_u^2 + \frac{32}{3} g_3^4 \mathbf{1}\sigma_{2,3} + \frac{32}{15} g_1^2 \mathbf{1}\sigma_{2,11} - 16 \frac{1}{\sqrt{15}} g_1 \mathbf{1}\sigma_{3,1} - 24m_{H_u}^2 Y_u Y_u^\dagger \text{Tr}(Y_u Y_u^\dagger) \\
& - 12T_u T_u^\dagger \text{Tr}(Y_u Y_u^\dagger) - 6m_u^2 Y_u Y_u^\dagger \text{Tr}(Y_u Y_u^\dagger) - 12Y_u m_q^2 Y_u^\dagger \text{Tr}(Y_u Y_u^\dagger) \\
& - 6Y_u Y_u^\dagger m_u^2 \text{Tr}(Y_u Y_u^\dagger) - 8m_{H_u}^2 Y_u Y_u^\dagger \text{Tr}(Y_u Y_u^\dagger) - 4T_u T_u^\dagger \text{Tr}(Y_u Y_u^\dagger) \\
& - 2m_u^2 Y_u Y_u^\dagger \text{Tr}(Y_u Y_u^\dagger) - 4Y_u m_q^2 Y_u^\dagger \text{Tr}(Y_u Y_u^\dagger) - 2Y_u Y_u^\dagger m_u^2 \text{Tr}(Y_u Y_u^\dagger) \\
& - 12Y_u T_u^\dagger \text{Tr}(Y_u^\dagger T_u) - 4Y_u T_u^\dagger \text{Tr}(Y_u^\dagger T_u) - 12T_u Y_u^\dagger \text{Tr}(T_u^* Y_u^T) \\
& - 12Y_u Y_u^\dagger \text{Tr}(T_u^* Y_u^T) - 4T_u Y_u^\dagger \text{Tr}(T_u^* Y_u^T) - 4Y_u Y_u^\dagger \text{Tr}(T_u^* Y_u^T) \\
& - 4Y_u Y_u^\dagger \text{Tr}(m_l^2 Y_u^\dagger Y_u) - 12Y_u Y_u^\dagger \text{Tr}(m_q^2 Y_u^\dagger Y_u) - 12Y_u Y_u^\dagger \text{Tr}(m_u^2 Y_u Y_u^\dagger) \\
& - 4Y_u Y_u^\dagger \text{Tr}(Y_u Y_u^\dagger m_{\nu}^{2*}) \tag{75}
\end{aligned}$$

$$\begin{aligned}
\beta_{m_e^2}^{(1)} = & -\frac{24}{5} g_1^2 \mathbf{1}|M_1|^2 + 2 \left( 2m_{H_d}^2 Y_e Y_e^\dagger + 2T_e T_e^\dagger + 2Y_e m_l^2 Y_e^\dagger + m_e^2 Y_e Y_e^\dagger + Y_e Y_e^\dagger m_e^2 \right) \\
& + 2\sqrt{\frac{3}{5}} g_1 \mathbf{1}\sigma_{1,1} \tag{76}
\end{aligned}$$

$$\begin{aligned}
\beta_{m_e^2}^{(2)} = & \frac{2}{25} \left( 6g_1^2 M_1^* \left( 234g_1^2 M_1 \mathbf{1} + 5 \left( -2M_1 Y_e Y_e^\dagger + T_e Y_e^\dagger \right) \right) + 20g_1 \mathbf{1} \left( 3g_1 \sigma_{2,11} + \sqrt{15} \sigma_{3,1} \right) \right. \\
& - 5 \left( 30g_2^2 M_2^* T_e Y_e^\dagger + 6g_1^2 T_e T_e^\dagger - 30g_2^2 T_e T_e^\dagger + 3g_1^2 m_e^2 Y_e Y_e^\dagger \right. \\
& - 15g_2^2 m_e^2 Y_e Y_e^\dagger + 6g_1^2 Y_e m_l^2 Y_e^\dagger - 30g_2^2 Y_e m_l^2 Y_e^\dagger + 3g_1^2 Y_e Y_e^\dagger m_e^2 \\
& - 15g_2^2 Y_e Y_e^\dagger m_e^2 + 20m_{H_d}^2 Y_e Y_e^\dagger Y_e Y_e^\dagger + 10Y_e Y_e^\dagger T_e T_e^\dagger + 10m_{H_d}^2 Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger \\
& + 10m_{H_u}^2 Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger + 10Y_e Y_\nu^\dagger T_\nu T_e^\dagger + 10Y_e T_e^\dagger T_e Y_e^\dagger + 10Y_e T_\nu^\dagger T_\nu Y_e^\dagger \\
& + 10T_e Y_e^\dagger Y_e T_e^\dagger + 10T_e Y_\nu^\dagger Y_\nu T_e^\dagger + 10T_e T_e^\dagger Y_e Y_e^\dagger + 10T_e T_\nu^\dagger Y_\nu Y_e^\dagger \\
& + 5m_e^2 Y_e Y_e^\dagger Y_e Y_e^\dagger + 5m_e^2 Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger + 10Y_e m_l^2 Y_e^\dagger Y_e Y_e^\dagger + 10Y_e m_l^2 Y_\nu^\dagger Y_\nu Y_e^\dagger \\
& + 10Y_e Y_e^\dagger m_e^2 Y_e Y_e^\dagger + 10Y_e Y_e^\dagger Y_e m_l^2 Y_e^\dagger + 5Y_e Y_e^\dagger Y_e Y_e^\dagger m_e^2 + 10Y_e Y_\nu^\dagger Y_\nu m_l^2 Y_e^\dagger \\
& + 5Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger m_e^2 + 10Y_e Y_\nu^\dagger m_{\nu}^{2*} Y_\nu Y_e^\dagger + 30T_e T_e^\dagger \text{Tr}(Y_d Y_d^\dagger) \\
& \left. + 15m_e^2 Y_e Y_e^\dagger \text{Tr}(Y_d Y_d^\dagger) + 30Y_e m_l^2 Y_e^\dagger \text{Tr}(Y_d Y_d^\dagger) + 15Y_e Y_e^\dagger m_e^2 \text{Tr}(Y_d Y_d^\dagger) \right)
\end{aligned}$$

$$\begin{aligned}
& + 10T_e T_e^\dagger \text{Tr}(Y_e Y_e^\dagger) + 5m_e^2 Y_e Y_e^\dagger \text{Tr}(Y_e Y_e^\dagger) + 10Y_e m_l^2 Y_e^\dagger \text{Tr}(Y_e Y_e^\dagger) \\
& + 5Y_e Y_e^\dagger m_e^2 \text{Tr}(Y_e Y_e^\dagger) + Y_e T_e^\dagger (10 \text{Tr}(Y_e^\dagger T_e) + 30g_2^2 M_2 + 30 \text{Tr}(Y_d^\dagger T_d) - 6g_1^2 M_1) \\
& + 30T_e Y_e^\dagger \text{Tr}(T_d^* Y_d^T) + 10T_e Y_e^\dagger \text{Tr}(T_e^* Y_e^T) \\
& + 2Y_e Y_e^\dagger (3g_1^2 m_{H_d}^2 - 15g_2^2 m_{H_d}^2 - 30g_2^2 |M_2|^2 + 30m_{H_d}^2 \text{Tr}(Y_d Y_d^\dagger) + 10m_{H_d}^2 \text{Tr}(Y_e Y_e^\dagger) + 15 \text{Tr}(T_d^* T_d^T) \\
& + 5 \text{Tr}(T_e^* T_e^T) + 15 \text{Tr}(m_d^2 Y_d Y_d^\dagger) + 5 \text{Tr}(m_e^2 Y_e Y_e^\dagger) + 5 \text{Tr}(m_l^2 Y_e^\dagger Y_e) + 15 \text{Tr}(m_q^2 Y_d^\dagger Y_d)) \quad (77)
\end{aligned}$$

$$\beta_{m_\nu^2}^{(1)} = 2 \left( 2m_{H_u}^2 Y_\nu^* Y_\nu^T + 2T_\nu^* T_\nu^T + 2Y_\nu^* m_l^2 Y_\nu^T + m_\nu^2 Y_\nu^* Y_\nu^T + Y_\nu^* Y_\nu^T m_\nu^2 \right) \quad (78)$$

$$\begin{aligned}
\beta_{m_\nu^2}^{(2)} = & -\frac{2}{5} \left( 6g_1^2 M_1^* Y_\nu^* T_\nu^T + 30g_2^2 M_2^* Y_\nu^* T_\nu^T + 6g_1^2 M_1 T_\nu^* Y_\nu^T + 30g_2^2 M_2 T_\nu^* Y_\nu^T \right. \\
& - 6g_1^2 T_\nu^* T_\nu^T - 30g_2^2 T_\nu^* T_\nu^T - 3g_1^2 m_\nu^2 Y_\nu^* Y_\nu^T - 15g_2^2 m_\nu^2 Y_\nu^* Y_\nu^T \\
& - 6g_1^2 Y_\nu^* m_l^2 Y_\nu^T - 30g_2^2 Y_\nu^* m_l^2 Y_\nu^T - 3g_1^2 Y_\nu^* Y_\nu^T m_\nu^2 - 15g_2^2 Y_\nu^* Y_\nu^T m_\nu^2 \\
& + 10m_{H_d}^2 Y_\nu^* Y_e^T Y_e^* Y_\nu^T + 10m_{H_u}^2 Y_\nu^* Y_e^T Y_e^* Y_\nu^T + 10Y_\nu^* Y_e^T T_e^* T_\nu^T \\
& + 20m_{H_u}^2 Y_\nu^* Y_\nu^T Y_\nu^* Y_\nu^T + 10Y_\nu^* Y_\nu^T T_\nu^* T_\nu^T + 10Y_\nu^* T_e^* T_e^* Y_\nu^T + 10Y_\nu^* T_\nu^* T_\nu^* Y_\nu^T \\
& + 10T_\nu^* Y_e^T Y_e^* T_\nu^T + 10T_\nu^* Y_\nu^* T_\nu^* T_\nu^T + 10T_\nu^* T_e^* Y_e^* Y_\nu^T + 10T_\nu^* T_\nu^* Y_\nu^* Y_\nu^T \\
& + 5m_\nu^2 Y_\nu^* Y_e^T Y_e^* Y_\nu^T + 5m_\nu^2 Y_\nu^* Y_\nu^T Y_\nu^* Y_\nu^T + 10Y_\nu^* m_l^2 Y_e^T Y_e^* Y_\nu^T + 10Y_\nu^* m_l^2 Y_\nu^T Y_\nu^* Y_\nu^T \\
& + 10Y_\nu^* Y_e^T m_e^2 Y_e^* Y_\nu^T + 10Y_\nu^* Y_e^T Y_e^* m_l^2 Y_\nu^T + 5Y_\nu^* Y_e^T Y_e^* Y_\nu^T m_\nu^2 \\
& + 10Y_\nu^* Y_\nu^T m_\nu^2 Y_\nu^* Y_\nu^T + 10Y_\nu^* Y_\nu^T Y_\nu^* m_l^2 Y_\nu^T + 5Y_\nu^* Y_\nu^T Y_\nu^* Y_\nu^T m_\nu^2 + 30T_\nu^* T_\nu^T \text{Tr}(Y_u Y_u^\dagger) \\
& + 15m_\nu^2 Y_\nu^* Y_\nu^T \text{Tr}(Y_u Y_u^\dagger) + 30Y_\nu^* m_l^2 Y_\nu^T \text{Tr}(Y_u Y_u^\dagger) + 15Y_\nu^* Y_\nu^T m_\nu^2 \text{Tr}(Y_u Y_u^\dagger) \\
& + 10T_\nu^* T_\nu^T \text{Tr}(Y_\nu Y_\nu^\dagger) + 5m_\nu^2 Y_\nu^* Y_\nu^T \text{Tr}(Y_\nu Y_\nu^\dagger) + 10Y_\nu^* m_l^2 Y_\nu^T \text{Tr}(Y_\nu Y_\nu^\dagger) \\
& + 5Y_\nu^* Y_\nu^T m_\nu^2 \text{Tr}(Y_\nu Y_\nu^\dagger) + 30T_\nu^* Y_\nu^T \text{Tr}(Y_u^\dagger T_u) + 10T_\nu^* Y_\nu^T \text{Tr}(Y_\nu^\dagger T_\nu) \\
& + 30Y_\nu^* T_\nu^T \text{Tr}(T_u^* Y_u^T) + 10Y_\nu^* T_\nu^T \text{Tr}(T_\nu^* Y_\nu^T) \Big) \\
& + \frac{4}{5} Y_\nu^* Y_\nu^T (3g_1^2 m_{H_u}^2 + 15g_2^2 m_{H_u}^2 + 6g_1^2 |M_1|^2 + 30g_2^2 |M_2|^2 - 30m_{H_u}^2 \text{Tr}(Y_u Y_u^\dagger) - 10m_{H_u}^2 \text{Tr}(Y_\nu Y_\nu^\dagger) \\
& - 15 \text{Tr}(T_u^* T_u^T) - 5 \text{Tr}(T_\nu^* T_\nu^T) - 5 \text{Tr}(m_l^2 Y_\nu^\dagger Y_\nu) - 15 \text{Tr}(m_q^2 Y_u^\dagger Y_u) - 15 \text{Tr}(m_u^2 Y_u Y_u^\dagger) \\
& - 5 \text{Tr}(Y_\nu Y_\nu^\dagger m_\nu^{2*}) \Big) \quad (79)
\end{aligned}$$

### 3.9 Vacuum expectation values

$$\begin{aligned}
\beta_{v_d}^{(1)} &= \frac{1}{20} v_d \left( -20 \text{Tr}(Y_e Y_e^\dagger) + 3(5g_2^2 + g_1^2)(1 + \text{Xi}) - 60 \text{Tr}(Y_d Y_d^\dagger) \right) \quad (80) \\
\beta_{v_d}^{(2)} &= \frac{1}{400} v_d \left( -414g_1^4 - 180g_1^2 g_2^2 - 1200g_2^4 - 9g_1^4 \text{Xi} - 90g_1^2 g_2^2 \text{Xi} + 875g_2^4 \text{Xi} + 9g_1^4 \text{Xi}^2 + 90g_1^2 g_2^2 \text{Xi}^2 \right)
\end{aligned}$$

$$\begin{aligned}
& -225g_2^4Xi^2 - 40\left(5\left(32g_3^2 + 9g_2^2Xi\right) + g_1^2\left(9Xi - 4\right)\right)\text{Tr}\left(Y_dY_d^\dagger\right) - 120\left(5g_2^2Xi + g_1^2\left(4 + Xi\right)\right)\text{Tr}\left(Y_eY_e^\dagger\right) \\
& + 3600\text{Tr}\left(Y_dY_d^\dagger Y_dY_d^\dagger\right) + 1200\text{Tr}\left(Y_dY_u^\dagger Y_uY_d^\dagger\right) + 1200\text{Tr}\left(Y_eY_e^\dagger Y_eY_e^\dagger\right) + 400\text{Tr}\left(Y_eY_\nu^\dagger Y_\nu Y_e^\dagger\right)
\end{aligned} \tag{81}$$

$$\beta_{v_u}^{(1)} = \frac{1}{20}v_u\left(-20\text{Tr}\left(Y_\nu Y_\nu^\dagger\right) + 3\left(5g_2^2 + g_1^2\right)\left(1 + Xi\right) - 60\text{Tr}\left(Y_u Y_u^\dagger\right)\right) \tag{82}$$

$$\begin{aligned}
\beta_{v_u}^{(2)} = & \frac{1}{400}v_u\left(-414g_1^4 - 180g_1^2g_2^2 - 1200g_2^4 - 9g_1^4Xi - 90g_1^2g_2^2Xi + 875g_2^4Xi + 9g_1^4Xi^2 + 90g_1^2g_2^2Xi^2\right. \\
& - 225g_2^4Xi^2 - 40\left(5\left(32g_3^2 + 9g_2^2Xi\right) + g_1^2\left(9Xi + 8\right)\right)\text{Tr}\left(Y_u Y_u^\dagger\right) - 120\left(5g_2^2 + g_1^2\right)Xi\text{Tr}\left(Y_\nu Y_\nu^\dagger\right) \\
& \left.+ 1200\text{Tr}\left(Y_d Y_u^\dagger Y_u Y_d^\dagger\right) + 400\text{Tr}\left(Y_e Y_\nu^\dagger Y_\nu Y_e^\dagger\right) + 3600\text{Tr}\left(Y_u Y_u^\dagger Y_u Y_u^\dagger\right) + 1200\text{Tr}\left(Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger\right)\right)
\end{aligned} \tag{83}$$

## 4 Field Rotations

### 4.1 Rotations in gauge sector for eigenstates 'EWSB'

$$\begin{pmatrix} B_\rho \\ W_{3\rho} \end{pmatrix} = Z^{\gamma Z} \begin{pmatrix} \gamma_\rho \\ Z_\rho \end{pmatrix} \tag{84}$$

$$\begin{pmatrix} W_{1\rho} \\ W_{2\rho} \end{pmatrix} = Z^W \begin{pmatrix} W_\rho^- \\ W_\rho^- \end{pmatrix} \tag{85}$$

$$\begin{pmatrix} \lambda_{\tilde{W},1} \\ \lambda_{\tilde{W},2} \\ \lambda_{\tilde{W},3} \end{pmatrix} = Z^{\tilde{W}} \begin{pmatrix} \tilde{W}^- \\ \tilde{W}^+ \\ \tilde{W}^0 \end{pmatrix} \tag{86}$$

(87)

The mixing matrices are parametrized by

$$Z^{\gamma Z} = \begin{pmatrix} \cos \Theta_W & -\sin \Theta_W \\ \sin \Theta_W & \cos \Theta_W \end{pmatrix} \tag{88}$$

$$Z^W = \begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ -i\frac{1}{\sqrt{2}} & i\frac{1}{\sqrt{2}} \end{pmatrix} \tag{89}$$

$$Z^{\tilde{W}} = \begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} & 0 \\ -i\frac{1}{\sqrt{2}} & i\frac{1}{\sqrt{2}} & 0 \\ 0 & 0 & 1 \end{pmatrix} \tag{90}$$

(91)

## 4.2 Rotations in Mass sector for eigenstates 'EWSB'

### 4.2.1 Mass Matrices for Scalars

- **Mass matrix for Down-Squarks**, Basis:  $(\tilde{d}_{L,\alpha_1}, \tilde{d}_{R,\alpha_2}), (\tilde{d}_{L,\beta_1}^*, \tilde{d}_{R,\beta_2}^*)$

$$m_{\tilde{d}}^2 = \begin{pmatrix} m_{\tilde{d}_L \tilde{d}_L^*} & \frac{1}{\sqrt{2}}(v_d T_d^\dagger - v_u \mu Y_d^\dagger) \delta_{\alpha_1 \beta_2} \\ \frac{1}{\sqrt{2}} \delta_{\alpha_2 \beta_1} (v_d T_d - v_u Y_d \mu^*) & m_{\tilde{d}_R \tilde{d}_R^*} \end{pmatrix} \quad (92)$$

$$m_{\tilde{d}_L \tilde{d}_L^*} = -\frac{1}{24} (3g_2^2 + g_1^2) \mathbf{1} (-v_u^2 + v_d^2) \delta_{\alpha_1 \beta_1} + \frac{1}{2} \delta_{\alpha_1 \beta_1} (2m_q^2 + v_d^2 Y_d^\dagger Y_d) \quad (93)$$

$$m_{\tilde{d}_R \tilde{d}_R^*} = \frac{1}{12} g_1^2 \mathbf{1} (-v_d^2 + v_u^2) \delta_{\alpha_2 \beta_2} + \frac{1}{2} \delta_{\alpha_2 \beta_2} (2m_d^2 + v_d^2 Y_d Y_d^\dagger) \quad (94)$$

This matrix is diagonalized by  $Z^D$ :

$$Z^D m_{\tilde{d}}^2 Z^{D,\dagger} = m_{2,\tilde{d}}^{dia} \quad (95)$$

with

$$\tilde{d}_{L,i\alpha} = \sum_j Z_{ji}^{D,*} \tilde{d}_{j\alpha}, \quad \tilde{d}_{R,i\alpha} = \sum_j Z_{ji}^{D,*} \tilde{d}_{j\alpha} \quad (96)$$

- **Mass matrix for Up-Squarks**, Basis:  $(\tilde{u}_{L,\alpha_1}, \tilde{u}_{R,\alpha_2}), (\tilde{u}_{L,\beta_1}^*, \tilde{u}_{R,\beta_2}^*)$

$$m_{\tilde{u}}^2 = \begin{pmatrix} m_{\tilde{u}_L \tilde{u}_L^*} & \frac{1}{\sqrt{2}}(-v_d \mu Y_u^\dagger + v_u T_u^\dagger) \delta_{\alpha_1 \beta_2} \\ \frac{1}{\sqrt{2}} \delta_{\alpha_2 \beta_1} (-v_d Y_u \mu^* + v_u T_u) & m_{\tilde{u}_R \tilde{u}_R^*} \end{pmatrix} \quad (97)$$

$$m_{\tilde{u}_L \tilde{u}_L^*} = -\frac{1}{24} (-3g_2^2 + g_1^2) \mathbf{1} (-v_u^2 + v_d^2) \delta_{\alpha_1 \beta_1} + \frac{1}{2} \delta_{\alpha_1 \beta_1} (2m_q^2 + v_u^2 Y_u^\dagger Y_u) \quad (98)$$

$$m_{\tilde{u}_R \tilde{u}_R^*} = \frac{1}{2} \delta_{\alpha_2 \beta_2} (2m_u^2 + v_u^2 Y_u Y_u^\dagger) + \frac{1}{6} g_1^2 \mathbf{1} (-v_u^2 + v_d^2) \delta_{\alpha_2 \beta_2} \quad (99)$$

This matrix is diagonalized by  $Z^U$ :

$$Z^U m_{\tilde{u}}^2 Z^{U,\dagger} = m_{2,\tilde{u}}^{dia} \quad (100)$$

with

$$\tilde{u}_{L,i\alpha} = \sum_j Z_{ji}^{U,*} \tilde{u}_{j\alpha}, \quad \tilde{u}_{R,i\alpha} = \sum_j Z_{ji}^{U,*} \tilde{u}_{j\alpha} \quad (101)$$

- **Mass matrix for Sleptons**, Basis:  $(\tilde{e}_L, \tilde{e}_R), (\tilde{e}_L^*, \tilde{e}_R^*)$

$$m_{\tilde{e}}^2 = \begin{pmatrix} m_{\tilde{e}_L \tilde{e}_L^*} & \frac{1}{\sqrt{2}}(v_d T_e^\dagger - v_u \mu Y_e^\dagger) \\ \frac{1}{\sqrt{2}}(v_d T_e - v_u Y_e \mu^*) & m_{\tilde{e}_R \tilde{e}_R^*} \end{pmatrix} \quad (102)$$

$$m_{\tilde{e}_L \tilde{e}_L^*} = \frac{1}{2} v_d^2 Y_e^\dagger Y_e + \frac{1}{8} (-g_2^2 + g_1^2) \mathbf{1} (-v_u^2 + v_d^2) + m_l^2 \quad (103)$$

$$m_{\tilde{e}_R \tilde{e}_R^*} = \frac{1}{2} v_d^2 Y_e Y_e^\dagger + \frac{1}{4} g_1^2 \mathbf{1} (-v_d^2 + v_u^2) + m_e^2 \quad (104)$$

This matrix is diagonalized by  $Z^E$ :

$$Z^E m_{\tilde{e}}^2 Z^{E,\dagger} = m_{2,\tilde{e}}^{dia} \quad (105)$$

with

$$\tilde{e}_{L,i} = \sum_j Z_{ji}^{E,*} \tilde{e}_j, \quad \tilde{e}_{R,i} = \sum_j Z_{ji}^{E,*} \tilde{e}_j \quad (106)$$

- **Mass matrix for CP-odd Sneutrino**, Basis: (sigmaL), (sigmaL)

$$m_{\nu^i}^2 = \begin{pmatrix} & \\ m_{\text{sigmaLsigmaL}} & \end{pmatrix} \quad (107)$$

$$\begin{aligned} m_{\text{sigmaLsigmaL}} = & +\frac{1}{8} (g_1^2 + g_2^2) \mathbf{1} (-v_u^2 + v_d^2) \\ & + \frac{1}{32} (32 \Re(m_l^2) \\ & + v_u (v_u (16 \Re(Y_\nu^T Y_\nu^*) - 8 \Re(Q_\nu) - 8 \Re(Q_\nu^T) + v_u^2 (2 \Re(\kappa_\nu \kappa_\nu^*) + 2 \Re(\kappa_\nu \kappa_\nu^\dagger) + 2 \Re(\kappa_\nu^T \kappa_\nu^*) + 2 \Re(\kappa_\nu^T \kappa_\nu^\dagger))) \\ & + 4 v_d (2 \mu (\kappa_{\nu,o_1 1}^* + \kappa_{\nu,p_1 1}^*) + \mu^* (\kappa_\nu + \kappa_\nu^T + \kappa_{\nu,o_1 1} + \kappa_{\nu,p_1 1}))) \end{aligned} \quad (108)$$

This matrix is diagonalized by  $Z^i$ :

$$Z^i m_{\nu^i}^2 Z^{i,\dagger} = m_{2,\nu^i}^{dia} \quad (109)$$

with

$$\text{sigmaL}(\{\text{gt1}\}) = \sum_j Z_{ji}^{i,*} \nu_j^i \quad (110)$$

- **Mass matrix for CP-even Sneutrino**, Basis: (phiL), (phiL)

$$m_{\nu^R}^2 = \begin{pmatrix} & \\ m_{\text{phiLphiL}} & \end{pmatrix} \quad (111)$$

$$\begin{aligned} m_{\text{phiLphiL}} = & +\frac{1}{8} (g_1^2 + g_2^2) \mathbf{1} (-v_u^2 + v_d^2) \\ & + \frac{1}{32} (32 \Re(m_l^2) \\ & + v_u (v_u (8 (2 \Re(Y_\nu^T Y_\nu^*) + \Re(Q_\nu)) + 8 \Re(Q_\nu^T) + v_u^2 (2 \Re(\kappa_\nu \kappa_\nu^*) + 2 \Re(\kappa_\nu \kappa_\nu^\dagger) + 2 \Re(\kappa_\nu^T \kappa_\nu^*) + 2 \Re(\kappa_\nu^T \kappa_\nu^\dagger))) \\ & - 4 v_d (2 \mu (\kappa_{\nu,o_1 1}^* + \kappa_{\nu,p_1 1}^*) + \mu^* (\kappa_\nu + \kappa_\nu^T + \kappa_{\nu,o_1 1} + \kappa_{\nu,p_1 1}))) \end{aligned} \quad (112)$$

This matrix is diagonalized by  $Z^R$ :

$$Z^R m_{\nu^R}^2 Z^{R,\dagger} = m_{2,\nu^R}^{dia} \quad (113)$$

with

$$\text{phiL}\left(\{\text{gt1}\}\right) = \sum_j Z_{ji}^{R,*} \nu_j^R \quad (114)$$

- **Mass matrix for Higgs**, Basis:  $(\phi_d, \phi_u), (\phi_d, \phi_u)$

$$m_h^2 = \begin{pmatrix} \frac{1}{8}(g_1^2 + g_2^2)(3v_d^2 - v_u^2) + m_{H_d}^2 + |\mu|^2 & -\frac{1}{4}(g_1^2 + g_2^2)v_d v_u - \Re(B_\mu) \\ -\frac{1}{4}(g_1^2 + g_2^2)v_d v_u - \Re(B_\mu) & -\frac{1}{8}(g_1^2 + g_2^2)(-3v_u^2 + v_d^2) + m_{H_u}^2 + |\mu|^2 \end{pmatrix} \quad (115)$$

This matrix is diagonalized by  $Z^H$ :

$$Z^H m_h^2 Z^{H,\dagger} = m_{2,h}^{dia} \quad (116)$$

with

$$\phi_d = \sum_j Z_{j1}^H h_j, \quad \phi_u = \sum_j Z_{j2}^H h_j \quad (117)$$

- **Mass matrix for Pseudo-Scalar Higgs**, Basis:  $(\sigma_d, \sigma_u), (\sigma_d, \sigma_u)$

$$m_{A^0}^2 = \begin{pmatrix} \frac{1}{8}(g_1^2 + g_2^2)(-v_u^2 + v_d^2) + m_{H_d}^2 + |\mu|^2 & \Re(B_\mu) \\ \Re(B_\mu) & -\frac{1}{8}(g_1^2 + g_2^2)(-v_u^2 + v_d^2) + m_{H_u}^2 + |\mu|^2 \end{pmatrix} + \xi_Z m^2(Z) \quad (118)$$

Gauge fixing contributions:

$$m^2(\xi_Z) = \begin{pmatrix} \frac{1}{4}v_d^2(g_1 \sin \Theta_W + g_2 \cos \Theta_W)^2 & -\frac{1}{4}v_d v_u(g_1 \sin \Theta_W + g_2 \cos \Theta_W)^2 \\ -\frac{1}{4}v_d v_u(g_1 \sin \Theta_W + g_2 \cos \Theta_W)^2 & \frac{1}{4}v_u^2(g_1 \sin \Theta_W + g_2 \cos \Theta_W)^2 \end{pmatrix} \quad (119)$$

This matrix is diagonalized by  $Z^A$ :

$$Z^A m_{A^0}^2 Z^{A,\dagger} = m_{2,A^0}^{dia} \quad (120)$$

with

$$\sigma_d = \sum_j Z_{j1}^A A_j^0, \quad \sigma_u = \sum_j Z_{j2}^A A_j^0 \quad (121)$$

- **Mass matrix for Charged Higgs**, Basis:  $(H_d^-, H_u^{+,*}), (H_d^{-,*}, H_u^+)$

$$m_{H^-}^2 = \begin{pmatrix} m_{H_d^- H_d^{-,*}} & \frac{1}{4}g_2^2 v_d v_u + B_\mu^* \\ \frac{1}{4}g_2^2 v_d v_u + B_\mu & m_{H_u^{+,*} H_u^+} \end{pmatrix} + \xi_{W^-} m^2(W^-) \quad (122)$$

$$m_{H_d^- H_d^{-,*}} = \frac{1}{8} \left( g_1^2 (-v_u^2 + v_d^2) + g_2^2 (v_d^2 + v_u^2) \right) + m_{H_d}^2 + |\mu|^2 \quad (123)$$

$$m_{H_u^{+,*} H_u^+} = \frac{1}{8} \left( g_1^2 (-v_d^2 + v_u^2) + g_2^2 (v_d^2 + v_u^2) \right) + m_{H_u}^2 + |\mu|^2 \quad (124)$$

Gauge fixing contributions:

$$m^2(\xi_{W^-}) = \begin{pmatrix} \frac{1}{4}g_2^2 v_d^2 & -\frac{1}{4}g_2^2 v_d v_u \\ -\frac{1}{4}g_2^2 v_d v_u & \frac{1}{4}g_2^2 v_u^2 \end{pmatrix} \quad (125)$$

This matrix is diagonalized by  $Z^+$ :

$$Z^+ m_{H^-}^2 Z^{+,\dagger} = m_{2,H^-}^{dia} \quad (126)$$

with

$$H_d^- = \sum_j Z_{j1}^+ H_j^- , \quad H_u^+ = \sum_j Z_{j2}^+ H_j^+ \quad (127)$$

#### 4.2.2 Mass Matrices for Fermions

- **Mass matrix for Neutralinos**, Basis:  $(\lambda_{\tilde{B}}, \tilde{W}^0, \tilde{H}_d^0, \tilde{H}_u^0)$ ,  $(\lambda_{\tilde{B}}, \tilde{W}^0, \tilde{H}_d^0, \tilde{H}_u^0)$

$$m_{\tilde{\chi}^0} = \begin{pmatrix} M_1 & 0 & -\frac{1}{2}g_1 v_d & \frac{1}{2}g_1 v_u \\ 0 & M_2 & \frac{1}{2}g_2 v_d & -\frac{1}{2}g_2 v_u \\ -\frac{1}{2}g_1 v_d & \frac{1}{2}g_2 v_d & 0 & -\mu \\ \frac{1}{2}g_1 v_u & -\frac{1}{2}g_2 v_u & -\mu & 0 \end{pmatrix} \quad (128)$$

This matrix is diagonalized by  $N$ :

$$N^* m_{\tilde{\chi}^0} N^\dagger = m_{\tilde{\chi}^0}^{dia} \quad (129)$$

with

$$\lambda_{\tilde{B}} = \sum_j N_{j1}^* \lambda_j^0 , \quad \tilde{W}^0 = \sum_j N_{j2}^* \lambda_j^0 , \quad \tilde{H}_d^0 = \sum_j N_{j3}^* \lambda_j^0 \quad (130)$$

$$\tilde{H}_u^0 = \sum_j N_{j4}^* \lambda_j^0 \quad (131)$$

- **Mass matrix for Neutrinos**, Basis:  $(\nu_L), (\nu_L)$

$$m_\nu = \left( \begin{array}{c} \frac{1}{4}v_u^2 (\kappa_\nu + \kappa_\nu^T) \end{array} \right) \quad (132)$$

This matrix is diagonalized by  $U^V$ :

$$U^{V,*} m_\nu U^{V,\dagger} = m_\nu^{dia} \quad (133)$$

with

$$\nu_{L,i} = \sum_j U_{ji}^{V,*} \nu_{M,j} \quad (134)$$

- **Mass matrix for Charginos**, Basis:  $(\tilde{W}^-, \tilde{H}_d^-), (\tilde{W}^+, \tilde{H}_u^+)$

$$m_{\tilde{\chi}^-} = \begin{pmatrix} M_2 & \frac{1}{\sqrt{2}}g_2 v_u \\ \frac{1}{\sqrt{2}}g_2 v_d & \mu \end{pmatrix} \quad (135)$$

This matrix is diagonalized by  $U$  and  $V$

$$U^* m_{\tilde{\chi}^-} V^\dagger = m_{\tilde{\chi}^-}^{dia} \quad (136)$$

with

$$\tilde{W}^- = \sum_{t_2} U_{j1}^* \lambda_j^-, \quad \tilde{H}_d^- = \sum_{t_2} U_{j2}^* \lambda_j^- \quad (137)$$

$$\tilde{W}^+ = \sum_{t_2} V_{1j}^* \lambda_j^+, \quad \tilde{H}_u^+ = \sum_{t_2} V_{2j}^* \lambda_j^+ \quad (138)$$

- **Mass matrix for Leptons**, Basis:  $(e_L), (e_R^*)$

$$m_e = \begin{pmatrix} \frac{1}{\sqrt{2}}v_d Y_e^T \end{pmatrix} \quad (139)$$

This matrix is diagonalized by  $U_L^e$  and  $U_R^e$

$$U_L^{e,*} m_e U_R^{e,\dagger} = m_e^{dia} \quad (140)$$

with

$$e_{L,i} = \sum_{t_2} U_{L,ji}^{e,*} E_{L,j} \quad (141)$$

$$e_{R,i} = \sum_{t_2} U_{R,ij}^e E_{R,j}^* \quad (142)$$

- **Mass matrix for Down-Quarks**, Basis:  $(d_{L,\alpha_1}), (d_{R,\beta_1}^*)$

$$m_d = \begin{pmatrix} \frac{1}{\sqrt{2}}v_d \delta_{\alpha_1 \beta_1} Y_d^T \end{pmatrix} \quad (143)$$

This matrix is diagonalized by  $U_L^d$  and  $U_R^d$

$$U_L^{d,*} m_d U_R^{d,\dagger} = m_d^{dia} \quad (144)$$

with

$$d_{L,i\alpha} = \sum_{t_2} U_{L,ji}^{d,*} D_{L,j\alpha} \quad (145)$$

$$d_{R,i\alpha} = \sum_{t_2} U_{R,ij}^d D_{R,j\alpha}^* \quad (146)$$

- **Mass matrix for Up-Quarks**, Basis:  $(u_{L,\alpha_1}), (u_{R,\beta_1}^*)$

$$m_u = \begin{pmatrix} & \frac{1}{\sqrt{2}}v_u \delta_{\alpha_1 \beta_1} Y_u^T \end{pmatrix} \quad (147)$$

This matrix is diagonalized by  $U_L^u$  and  $U_R^u$

$$U_L^{u,*} m_u U_R^{u,\dagger} = m_u^{dia} \quad (148)$$

with

$$u_{L,i\alpha} = \sum_{t_2} U_{L,ji}^{u,*} U_{L,j\alpha} \quad (149)$$

$$u_{R,i\alpha} = \sum_{t_2} U_{R,ij}^u U_{R,j\alpha}^* \quad (150)$$

## 5 Vacuum Expectation Values

$$H_d^0 = \frac{1}{\sqrt{2}}\phi_d + \frac{1}{\sqrt{2}}v_d + i\frac{1}{\sqrt{2}}\sigma_d \quad (151)$$

$$H_u^0 = \frac{1}{\sqrt{2}}\phi_u + \frac{1}{\sqrt{2}}v_u + i\frac{1}{\sqrt{2}}\sigma_u \quad (152)$$

$$\tilde{\nu}_L = \frac{1}{\sqrt{2}}\text{phiL} + i\frac{1}{\sqrt{2}}\text{sigmaL} \quad (153)$$

## 6 Tadpole Equations

$$\frac{\partial V}{\partial \phi_d} = -\frac{1}{2}v_u(B_\mu + B_\mu^*) + \frac{1}{8}(g_1^2 + g_2^2)v_d(-v_u + v_d)(v_d + v_u) + v_d(m_{H_d}^2 + |\mu|^2) \quad (154)$$

$$\frac{\partial V}{\partial \phi_u} = \frac{1}{8}(g_1^2 + g_2^2)v_u(-v_d^2 + v_u^2) - v_d \Re(B_\mu) + v_u(m_{H_u}^2 + |\mu|^2) \quad (155)$$

$$\frac{\partial V}{\partial \text{phiL}_i} = 0 \quad (156)$$

## 7 Particle content for eigenstates 'EWSB'

Name	Type	complex/real	Generations	Indices
$\tilde{d}$	Scalar	complex	6	generation, 6, color, 3
$\tilde{u}$	Scalar	complex	6	generation, 6, color, 3
$\tilde{e}$	Scalar	complex	6	generation, 6
$\nu^I$	Scalar	real	3	generation, 3

$\nu^R$	Scalar	real	3	generation, 3
$h$	Scalar	real	2	generation, 2
$A^0$	Scalar	real	2	generation, 2
$H^-$	Scalar	complex	2	generation, 2
$\tilde{g}$	Fermion	Majorana	1	color, 8
$\tilde{\chi}^0$	Fermion	Majorana	4	generation, 4
$\nu$	Fermion	Majorana	3	generation, 3
$\tilde{\chi}^-$	Fermion	Dirac	2	generation, 2
$e$	Fermion	Dirac	3	generation, 3
$d$	Fermion	Dirac	3	generation, 3, color, 3
$u$	Fermion	Dirac	3	generation, 3, color, 3
$g$	Vector	real	1	color, 8, lorentz, 4
$\gamma$	Vector	real	1	lorentz, 4
$Z$	Vector	real	1	lorentz, 4
$W^-$	Vector	complex	1	lorentz, 4
$\eta^G$	Ghost	real	1	color, 8
$\eta^\gamma$	Ghost	real	1	
$\eta^Z$	Ghost	real	1	
$\eta^-$	Ghost	complex	1	
$\eta^+$	Ghost	complex	1	

## 8 One Loop Self-Energy and One Loop Tadpoles for eigenstates 'EWSB'

### 8.1 One Loop Self-Energy

- Self-Energy for Down-Squarks ( $\tilde{d}$ )

$$\begin{aligned}
\Pi_{i,j}(p^2) = & +4\Gamma_{\tilde{d}_i, \tilde{d}_j^*, W^+, W^-} \left( -\frac{1}{2}\text{rMS}m_{W^-}^2 + A_0(m_{W^-}^2) \right) + 2\Gamma_{\tilde{d}_i, \tilde{d}_j^*, Z, Z} \left( -\frac{1}{2}\text{rMS}m_Z^2 + A_0(m_Z^2) \right) \\
& - \frac{1}{2} \sum_{a=1}^2 A_0(m_{A_a^0}^2) \Gamma_{\tilde{d}_i, \tilde{d}_j^*, A_a^0, A_a^0} - \sum_{a=1}^2 A_0(m_{H_a^-}^2) \Gamma_{\tilde{d}_i, \tilde{d}_j^*, H_a^+, H_a^-} \\
& - \frac{1}{2} \sum_{a=1}^2 A_0(m_{h_a}^2) \Gamma_{\tilde{d}_i, \tilde{d}_j^*, h_a, h_a} - \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^i}^2) \Gamma_{\tilde{d}_i, \tilde{d}_j^*, \nu_a^i, \nu_a^i} \\
& - \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^R}^2) \Gamma_{\tilde{d}_i, \tilde{d}_j^*, \nu_a^R, \nu_a^R}
\end{aligned}$$

$$\begin{aligned}
& -2 \sum_{a=1}^3 m_{u_a} \sum_{b=1}^2 B_0(p^2, m_{u_a}^2, m_{\tilde{\chi}_b^-}^2) m_{\tilde{\chi}_b^-} \left( \Gamma_{\tilde{d}_j^*, u_a, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{d}_i^*, u_a, \tilde{\chi}_b^-}^R + \Gamma_{\tilde{d}_j^*, u_a, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{d}_i^*, u_a, \tilde{\chi}_b^-}^L \right) \\
& + \sum_{a=1}^3 \sum_{b=1}^2 G_0(p^2, m_{u_a}^2, m_{\tilde{\chi}_b^-}^2) \left( \Gamma_{\tilde{d}_j^*, u_a, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{d}_i^*, u_a, \tilde{\chi}_b^-}^L + \Gamma_{\tilde{d}_j^*, u_a, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{d}_i^*, u_a, \tilde{\chi}_b^-}^R \right) \\
& - 2 \sum_{a=1}^3 m_{d_a} \sum_{b=1}^4 B_0(p^2, m_{d_a}^2, m_{\tilde{\chi}_b^0}^2) m_{\tilde{\chi}_b^0} \left( \Gamma_{\tilde{d}_j^*, d_a, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{d}_i^*, d_a, \tilde{\chi}_b^0}^R + \Gamma_{\tilde{d}_j^*, d_a, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{d}_i^*, d_a, \tilde{\chi}_b^0}^L \right) \\
& + \sum_{a=1}^3 \sum_{b=1}^4 G_0(p^2, m_{d_a}^2, m_{\tilde{\chi}_b^0}^2) \left( \Gamma_{\tilde{d}_j^*, d_a, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{d}_i^*, d_a, \tilde{\chi}_b^0}^L + \Gamma_{\tilde{d}_j^*, d_a, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{d}_i^*, d_a, \tilde{\chi}_b^0}^R \right) \\
& - C \sum_{a=1}^6 A_0(m_{\tilde{d}_a}^2) \Gamma_{\tilde{d}_i^*, \tilde{d}_j^*, \tilde{d}_a, \tilde{d}_a} - \sum_{a=1}^6 A_0(m_{\tilde{e}_a}^2) \Gamma_{\tilde{d}_i^*, \tilde{d}_j^*, \tilde{e}_a^*, \tilde{e}_a} \\
& - C \sum_{a=1}^6 A_0(m_{\tilde{u}_a}^2) \Gamma_{\tilde{d}_i^*, \tilde{d}_j^*, \tilde{u}_a^*, \tilde{u}_a} + \sum_{a=1}^6 \sum_{b=1}^2 B_0(p^2, m_{\tilde{d}_a}^2, m_{A_b^0}^2) \Gamma_{\tilde{d}_j^*, \tilde{d}_a, A_b^0}^* \Gamma_{\tilde{d}_i^*, \tilde{d}_a, A_b^0} \\
& + \sum_{a=1}^6 \sum_{b=1}^2 B_0(p^2, m_{\tilde{d}_a}^2, m_{h_b}^2) \Gamma_{\tilde{d}_j^*, \tilde{d}_a, h_b}^* \Gamma_{\tilde{d}_i^*, \tilde{d}_a, h_b} + \sum_{a=1}^6 \sum_{b=1}^2 B_0(p^2, m_{\tilde{u}_a}^2, m_{H_b^-}^2) \Gamma_{\tilde{d}_j^*, \tilde{u}_a, H_b^-}^* \Gamma_{\tilde{d}_i^*, \tilde{u}_a, H_b^-} \\
& - \frac{8}{3} m_{\tilde{g}} \sum_{b=1}^3 B_0(p^2, m_{\tilde{g}}^2, m_{d_b}^2) m_{d_b} \left( \Gamma_{\tilde{d}_j^*, \tilde{g}_1, d_b}^{L*} \Gamma_{\tilde{d}_i^*, \tilde{g}_1, d_b}^R + \Gamma_{\tilde{d}_j^*, \tilde{g}_1, d_b}^{R*} \Gamma_{\tilde{d}_i^*, \tilde{g}_1, d_b}^L \right) \\
& + \frac{4}{3} \sum_{b=1}^3 G_0(p^2, m_{\tilde{g}}^2, m_{d_b}^2) \left( \Gamma_{\tilde{d}_j^*, \tilde{g}_1, d_b}^{L*} \Gamma_{\tilde{d}_i^*, \tilde{g}_1, d_b}^L + \Gamma_{\tilde{d}_j^*, \tilde{g}_1, d_b}^{R*} \Gamma_{\tilde{d}_i^*, \tilde{g}_1, d_b}^R \right) \\
& + \frac{4}{3} \sum_{b=1}^6 \Gamma_{\tilde{d}_j^*, g, \tilde{d}_b}^* \Gamma_{\tilde{d}_i^*, g, \tilde{d}_b} F_0(p^2, m_{\tilde{d}_b}^2, 0) + \sum_{b=1}^6 \Gamma_{\tilde{d}_j^*, \gamma, \tilde{d}_b}^* \Gamma_{\tilde{d}_i^*, \gamma, \tilde{d}_b} F_0(p^2, m_{\tilde{d}_b}^2, 0) \\
& + \sum_{b=1}^6 \Gamma_{\tilde{d}_j^*, Z, \tilde{d}_b}^* \Gamma_{\tilde{d}_i^*, Z, \tilde{d}_b} F_0(p^2, m_{\tilde{d}_b}^2, m_Z^2) + \sum_{b=1}^6 \Gamma_{\tilde{d}_j^*, W^-, \tilde{u}_b}^* \Gamma_{\tilde{d}_i^*, W^-, \tilde{u}_b} F_0(p^2, m_{\tilde{u}_b}^2, m_{W^-}^2)
\end{aligned} \tag{157}$$

• **Self-Energy for Up-Squarks ( $\tilde{u}$ )**

$$\begin{aligned}
\Pi_{i,j}(p^2) = & +4 \Gamma_{\tilde{u}_i, \tilde{u}_j^*, W^+, W^-} \left( -\frac{1}{2} \text{rMS} m_{W^-}^2 + A_0(m_{W^-}^2) \right) + 2 \Gamma_{\tilde{u}_i, \tilde{u}_j^*, Z, Z} \left( -\frac{1}{2} \text{rMS} m_Z^2 + A_0(m_Z^2) \right) \\
& - \frac{1}{2} \sum_{a=1}^2 A_0(m_{A_a^0}^2) \Gamma_{\tilde{u}_i, \tilde{u}_j^*, A_a^0, A_a^0} - \sum_{a=1}^2 A_0(m_{H_a^-}^2) \Gamma_{\tilde{u}_i, \tilde{u}_j^*, H_a^+, H_a^-} \\
& - \frac{1}{2} \sum_{a=1}^2 A_0(m_{h_a}^2) \Gamma_{\tilde{u}_i, \tilde{u}_j^*, h_a, h_a} \\
& - 2 \sum_{a=1}^2 m_{\tilde{\chi}_a^-} \sum_{b=1}^3 B_0(p^2, m_{\tilde{\chi}_a^-}^2, m_{d_b}^2) m_{d_b} \left( \Gamma_{\tilde{u}_j^*, \tilde{\chi}_a^+, d_b}^{L*} \Gamma_{\tilde{u}_i^*, \tilde{\chi}_a^+, d_b}^R + \Gamma_{\tilde{u}_j^*, \tilde{\chi}_a^+, d_b}^{R*} \Gamma_{\tilde{u}_i^*, \tilde{\chi}_a^+, d_b}^L \right)
\end{aligned}$$

$$\begin{aligned}
& + \sum_{a=1}^2 \sum_{b=1}^3 G_0(p^2, m_{\tilde{\chi}_a^-}^2, m_{d_b}^2) \left( \Gamma_{\tilde{u}_j^*, \tilde{\chi}_a^+, d_b}^{L*} \Gamma_{\tilde{u}_i^*, \tilde{\chi}_a^+, d_b}^L + \Gamma_{\tilde{u}_j^*, \tilde{\chi}_a^+, d_b}^{R*} \Gamma_{\tilde{u}_i^*, \tilde{\chi}_a^+, d_b}^R \right) \\
& + \sum_{a=1}^2 \sum_{b=1}^6 B_0(p^2, m_{H_a^-}^2, m_{\tilde{d}_b}^2) \Gamma_{\tilde{u}_j^*, H_a^+, \tilde{d}_b}^* \Gamma_{\tilde{u}_i^*, H_a^+, \tilde{d}_b} - \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^i}^2) \Gamma_{\tilde{u}_i, \tilde{u}_j^*, \nu_a^i, \nu_a^i} \\
& - \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^R}^2) \Gamma_{\tilde{u}_i, \tilde{u}_j^*, \nu_a^R, \nu_a^R} \\
& - 2 \sum_{a=1}^3 m_{u_a} \sum_{b=1}^4 B_0(p^2, m_{u_a}^2, m_{\tilde{\chi}_b^0}^2) m_{\tilde{\chi}_b^0} \left( \Gamma_{\tilde{u}_j^*, u_a, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{u}_i^*, u_a, \tilde{\chi}_b^0}^R + \Gamma_{\tilde{u}_j^*, u_a, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{u}_i^*, u_a, \tilde{\chi}_b^0}^L \right) \\
& + \sum_{a=1}^3 \sum_{b=1}^4 G_0(p^2, m_{u_a}^2, m_{\tilde{\chi}_b^0}^2) \left( \Gamma_{\tilde{u}_j^*, u_a, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{u}_i^*, u_a, \tilde{\chi}_b^0}^L + \Gamma_{\tilde{u}_j^*, u_a, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{u}_i^*, u_a, \tilde{\chi}_b^0}^R \right) \\
& - C \sum_{a=1}^6 A_0(m_{\tilde{d}_a}^2) \Gamma_{\tilde{u}_i, \tilde{u}_j^*, \tilde{d}_a^*, \tilde{d}_a} - \sum_{a=1}^6 A_0(m_{\tilde{e}_a}^2) \Gamma_{\tilde{u}_i, \tilde{u}_j^*, \tilde{e}_a^*, \tilde{e}_a} \\
& - C \sum_{a=1}^6 A_0(m_{\tilde{u}_a}^2) \Gamma_{\tilde{u}_i, \tilde{u}_j^*, \tilde{u}_a^*, \tilde{u}_a} + \sum_{a=1}^6 \sum_{b=1}^2 B_0(p^2, m_{\tilde{u}_a}^2, m_{A_b^0}^2) \Gamma_{\tilde{u}_j^*, \tilde{u}_a, A_b^0}^* \Gamma_{\tilde{u}_i^*, \tilde{u}_a, A_b^0} \\
& + \sum_{a=1}^6 \sum_{b=1}^2 B_0(p^2, m_{\tilde{u}_a}^2, m_{h_b}^2) \Gamma_{\tilde{u}_j^*, \tilde{u}_a, h_b}^* \Gamma_{\tilde{u}_i^*, \tilde{u}_a, h_b} \\
& - \frac{8}{3} m_{\tilde{g}} \sum_{b=1}^3 B_0(p^2, m_{\tilde{g}}^2, m_{u_b}^2) m_{u_b} \left( \Gamma_{\tilde{u}_j^*, \tilde{g}_1, u_b}^{L*} \Gamma_{\tilde{u}_i^*, \tilde{g}_1, u_b}^R + \Gamma_{\tilde{u}_j^*, \tilde{g}_1, u_b}^{R*} \Gamma_{\tilde{u}_i^*, \tilde{g}_1, u_b}^L \right) \\
& + \frac{4}{3} \sum_{b=1}^3 G_0(p^2, m_{\tilde{g}}^2, m_{u_b}^2) \left( \Gamma_{\tilde{u}_j^*, \tilde{g}_1, u_b}^{L*} \Gamma_{\tilde{u}_i^*, \tilde{g}_1, u_b}^L + \Gamma_{\tilde{u}_j^*, \tilde{g}_1, u_b}^{R*} \Gamma_{\tilde{u}_i^*, \tilde{g}_1, u_b}^R \right) \\
& + \sum_{b=1}^6 \Gamma_{\tilde{u}_j^*, W^+, \tilde{d}_b}^* \Gamma_{\tilde{u}_i^*, W^+, \tilde{d}_b} F_0(p^2, m_{\tilde{d}_b}^2, m_{W^-}^2) + \frac{4}{3} \sum_{b=1}^6 \Gamma_{\tilde{u}_j^*, g, \tilde{u}_b}^* \Gamma_{\tilde{u}_i^*, g, \tilde{u}_b} F_0(p^2, m_{\tilde{u}_b}^2, 0) \\
& + \sum_{b=1}^6 \Gamma_{\tilde{u}_j^*, \gamma, \tilde{u}_b}^* \Gamma_{\tilde{u}_i^*, \gamma, \tilde{u}_b} F_0(p^2, m_{\tilde{u}_b}^2, 0) + \sum_{b=1}^6 \Gamma_{\tilde{u}_j^*, Z, \tilde{u}_b}^* \Gamma_{\tilde{u}_i^*, Z, \tilde{u}_b} F_0(p^2, m_{\tilde{u}_b}^2, m_Z^2) \tag{158}
\end{aligned}$$

• Self-Energy for Sleptons ( $\tilde{e}$ )

$$\begin{aligned}
\Pi_{i,j}(p^2) = & +4\Gamma_{\tilde{e}_i, \tilde{e}_j^*, W^+, W^-} \left( -\frac{1}{2} rMSm_{W^-}^2 + A_0(m_{W^-}^2) \right) + 2\Gamma_{\tilde{e}_i, \tilde{e}_j^*, Z, Z} \left( -\frac{1}{2} rMSm_Z^2 + A_0(m_Z^2) \right) \\
& - \frac{1}{2} \sum_{a=1}^2 A_0(m_{A_a^0}^2) \Gamma_{\tilde{e}_i, \tilde{e}_j^*, A_a^0, A_a^0} - \sum_{a=1}^2 A_0(m_{H_a^-}^2) \Gamma_{\tilde{e}_i, \tilde{e}_j^*, H_a^+, H_a^-} \\
& - \frac{1}{2} \sum_{a=1}^2 A_0(m_{h_a}^2) \Gamma_{\tilde{e}_i, \tilde{e}_j^*, h_a, h_a} - \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^i}^2) \Gamma_{\tilde{e}_i, \tilde{e}_j^*, \nu_a^i, \nu_a^i}
\end{aligned}$$

$$\begin{aligned}
& - \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^R}^2) \Gamma_{\tilde{e}_i, \tilde{\nu}_j^*, \nu_a^R, \nu_a^R} + \sum_{a=1}^3 \sum_{b=1}^2 B_0(p^2, m_{\nu_a^i}^2, m_{H_b^-}^2) \Gamma_{\tilde{e}_j^*, \nu_a^i, H_b^-}^* \Gamma_{\tilde{e}_i^*, \nu_a^i, H_b^-} \\
& + \sum_{a=1}^3 \sum_{b=1}^2 B_0(p^2, m_{\nu_a^R}^2, m_{H_b^-}^2) \Gamma_{\tilde{e}_j^*, \nu_a^R, H_b^-}^* \Gamma_{\tilde{e}_i^*, \nu_a^R, H_b^-} \\
& - 2 \sum_{a=1}^3 m_{\nu_a} \sum_{b=1}^2 B_0(p^2, m_{\nu_a}^2, m_{\tilde{\chi}_b^-}^2) m_{\tilde{\chi}_b^-} \left( \Gamma_{\tilde{e}_j^*, \nu_a, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{e}_i^*, \nu_a, \tilde{\chi}_b^-}^R + \Gamma_{\tilde{e}_j^*, \nu_a, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{e}_i^*, \nu_a, \tilde{\chi}_b^-}^L \right) \\
& + \sum_{a=1}^3 \sum_{b=1}^2 G_0(p^2, m_{\nu_a}^2, m_{\tilde{\chi}_b^-}^2) \left( \Gamma_{\tilde{e}_j^*, \nu_a, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{e}_i^*, \nu_a, \tilde{\chi}_b^-}^L + \Gamma_{\tilde{e}_j^*, \nu_a, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{e}_i^*, \nu_a, \tilde{\chi}_b^-}^R \right) \\
& - 2 \sum_{a=1}^3 m_{e_a} \sum_{b=1}^4 B_0(p^2, m_{e_a}^2, m_{\tilde{\chi}_b^0}^2) m_{\tilde{\chi}_b^0} \left( \Gamma_{\tilde{e}_j^*, e_a, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{e}_i^*, e_a, \tilde{\chi}_b^0}^R + \Gamma_{\tilde{e}_j^*, e_a, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{e}_i^*, e_a, \tilde{\chi}_b^0}^L \right) \\
& + \sum_{a=1}^3 \sum_{b=1}^4 G_0(p^2, m_{e_a}^2, m_{\tilde{\chi}_b^0}^2) \left( \Gamma_{\tilde{e}_j^*, e_a, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{e}_i^*, e_a, \tilde{\chi}_b^0}^L + \Gamma_{\tilde{e}_j^*, e_a, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{e}_i^*, e_a, \tilde{\chi}_b^0}^R \right) \\
& - 3 \sum_{a=1}^6 A_0(m_{\tilde{d}_a}^2) \Gamma_{\tilde{e}_i, \tilde{\nu}_j^*, \tilde{d}_a^*, \tilde{d}_a} - \sum_{a=1}^6 A_0(m_{\tilde{e}_a}^2) \Gamma_{\tilde{e}_i, \tilde{\nu}_j^*, \tilde{e}_a^*, \tilde{e}_a} \\
& - 3 \sum_{a=1}^6 A_0(m_{\tilde{u}_a}^2) \Gamma_{\tilde{e}_i, \tilde{\nu}_j^*, \tilde{u}_a^*, \tilde{u}_a} + \sum_{a=1}^6 \sum_{b=1}^2 B_0(p^2, m_{\tilde{e}_a}^2, m_{A_b^0}^2) \Gamma_{\tilde{e}_j^*, \tilde{e}_a, A_b^0}^* \Gamma_{\tilde{e}_i^*, \tilde{e}_a, A_b^0} \\
& + \sum_{a=1}^6 \sum_{b=1}^2 B_0(p^2, m_{\tilde{e}_a}^2, m_{h_b}^2) \Gamma_{\tilde{e}_j^*, \tilde{e}_a, h_b}^* \Gamma_{\tilde{e}_i^*, \tilde{e}_a, h_b} + \sum_{b=1}^3 \Gamma_{\tilde{e}_j^*, W^-, \nu_b^i}^* \Gamma_{\tilde{e}_i^*, W^-, \nu_b^i} F_0(p^2, m_{\nu_b^i}^2, m_{W^-}^2) \\
& + \sum_{b=1}^3 \Gamma_{\tilde{e}_j^*, W^-, \nu_b^R}^* \Gamma_{\tilde{e}_i^*, W^-, \nu_b^R} F_0(p^2, m_{\nu_b^R}^2, m_{W^-}^2) + \sum_{b=1}^6 \Gamma_{\tilde{e}_j^*, \gamma, \tilde{e}_b}^* \Gamma_{\tilde{e}_i^*, \gamma, \tilde{e}_b} F_0(p^2, m_{\tilde{e}_b}^2, 0) \\
& + \sum_{b=1}^6 \Gamma_{\tilde{e}_j^*, Z, \tilde{e}_b}^* \Gamma_{\tilde{e}_i^*, Z, \tilde{e}_b} F_0(p^2, m_{\tilde{e}_b}^2, m_Z^2)
\end{aligned} \tag{159}$$

• **Self-Energy for CP-odd Sneutrino ( $\nu^i$ )**

$$\begin{aligned}
\Pi_{i,j}(p^2) = & +4\Gamma_{\tilde{\nu}_i^i, \tilde{\nu}_j^i, W^+, W^-} \left( -\frac{1}{2} \text{rMS} m_{W^-}^2 + A_0(m_{W^-}^2) \right) + 2\Gamma_{\tilde{\nu}_i^i, \tilde{\nu}_j^i, Z, Z} \left( -\frac{1}{2} \text{rMS} m_Z^2 + A_0(m_Z^2) \right) \\
& - \frac{1}{2} \sum_{a=1}^2 A_0(m_{A_a^0}^2) \Gamma_{\tilde{\nu}_i^i, \tilde{\nu}_j^i, A_a^0, A_a^0} - \sum_{a=1}^2 A_0(m_{H_a^-}^2) \Gamma_{\tilde{\nu}_i^i, \tilde{\nu}_j^i, H_a^+, H_a^-} \\
& - \frac{1}{2} \sum_{a=1}^2 A_0(m_{h_a}^2) \Gamma_{\tilde{\nu}_i^i, \tilde{\nu}_j^i, h_a, h_a} - \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^i}^2) \Gamma_{\tilde{\nu}_i^i, \tilde{\nu}_j^i, \nu_a^i, \nu_a^i} \\
& - \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^R}^2) \Gamma_{\tilde{\nu}_i^i, \tilde{\nu}_j^i, \nu_a^R, \nu_a^R} + \sum_{a=1}^3 \sum_{b=1}^2 B_0(p^2, m_{\nu_a^i}^2, m_{A_b^0}^2) \Gamma_{\tilde{\nu}_j^i, \nu_a^i, A_b^0}^* \Gamma_{\tilde{\nu}_i^i, \nu_a^i, A_b^0}
\end{aligned}$$

$$\begin{aligned}
& + \sum_{a=1}^3 \sum_{b=1}^2 B_0(p^2, m_{\nu_a^i}^2, m_{h_b}^2) \Gamma_{\tilde{\nu}_j^i, \nu_a^i, h_b}^* \Gamma_{\tilde{\nu}_i^i, \nu_a^i, h_b} \\
& + \sum_{a=1}^3 \sum_{b=1}^2 B_0(p^2, m_{\nu_a^R}^2, m_{A_b^0}^2) \Gamma_{\tilde{\nu}_j^i, \nu_a^R, A_b^0}^* \Gamma_{\tilde{\nu}_i^i, \nu_a^R, A_b^0} \\
& + \sum_{a=1}^3 \sum_{b=1}^2 B_0(p^2, m_{\nu_a^R}^2, m_{h_b}^2) \Gamma_{\tilde{\nu}_j^i, \nu_a^R, h_b}^* \Gamma_{\tilde{\nu}_i^i, \nu_a^R, h_b} \\
& - 4 \sum_{a=1}^3 m_{e_a} \sum_{b=1}^2 B_0(p^2, m_{e_a}^2, m_{\tilde{\chi}_b^-}^2) m_{\tilde{\chi}_b^-} \left( \Gamma_{\tilde{\nu}_j^i, \bar{e}_a, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{\nu}_i^i, \bar{e}_a, \tilde{\chi}_b^-}^R + \Gamma_{\tilde{\nu}_j^i, \bar{e}_a, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{\nu}_i^i, \bar{e}_a, \tilde{\chi}_b^-}^L \right) \\
& + 2 \sum_{a=1}^3 \sum_{b=1}^2 G_0(p^2, m_{e_a}^2, m_{\tilde{\chi}_b^-}^2) \left( \Gamma_{\tilde{\nu}_j^i, \bar{e}_a, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{\nu}_i^i, \bar{e}_a, \tilde{\chi}_b^-}^L + \Gamma_{\tilde{\nu}_j^i, \bar{e}_a, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{\nu}_i^i, \bar{e}_a, \tilde{\chi}_b^-}^R \right) \\
& - 2 \sum_{a=1}^3 m_{\nu_a} \sum_{b=1}^4 B_0(p^2, m_{\nu_a}^2, m_{\tilde{\chi}_b^0}^2) m_{\tilde{\chi}_b^0} \left( \Gamma_{\tilde{\nu}_j^i, \nu_a, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{\nu}_i^i, \nu_a, \tilde{\chi}_b^0}^R + \Gamma_{\tilde{\nu}_j^i, \nu_a, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{\nu}_i^i, \nu_a, \tilde{\chi}_b^0}^L \right) \\
& + \sum_{a=1}^3 \sum_{b=1}^4 G_0(p^2, m_{\nu_a}^2, m_{\tilde{\chi}_b^0}^2) \left( \Gamma_{\tilde{\nu}_j^i, \nu_a, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{\nu}_i^i, \nu_a, \tilde{\chi}_b^0}^L + \Gamma_{\tilde{\nu}_j^i, \nu_a, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{\nu}_i^i, \nu_a, \tilde{\chi}_b^0}^R \right) \\
& - 3 \sum_{a=1}^6 A_0(m_{d_a}^2) \Gamma_{\tilde{\nu}_i^i, \tilde{\nu}_j^i, \tilde{d}_a^*, \tilde{d}_a} - \sum_{a=1}^6 A_0(m_{\tilde{e}_a}^2) \Gamma_{\tilde{\nu}_i^i, \tilde{\nu}_j^i, \tilde{e}_a^*, \tilde{e}_a} \\
& - 3 \sum_{a=1}^6 A_0(m_{\tilde{u}_a}^2) \Gamma_{\tilde{\nu}_i^i, \tilde{\nu}_j^i, \tilde{u}_a^*, \tilde{u}_a} + 2 \sum_{a=1}^6 \sum_{b=1}^2 B_0(p^2, m_{\tilde{e}_a}^2, m_{H_b^-}^2) \Gamma_{\tilde{\nu}_j^i, \tilde{e}_a^*, H_b^-}^* \Gamma_{\tilde{\nu}_i^i, \tilde{e}_a^*, H_b^-} \\
& + \sum_{b=1}^3 \Gamma_{\tilde{\nu}_j^i, Z, \nu_b^R}^* \Gamma_{\tilde{\nu}_i^i, Z, \nu_b^R} F_0(p^2, m_{\nu_b^R}^2, m_Z^2) + 2 \sum_{b=1}^6 \Gamma_{\tilde{\nu}_j^i, W^+, \tilde{e}_b}^* \Gamma_{\tilde{\nu}_i^i, W^+, \tilde{e}_b} F_0(p^2, m_{\tilde{e}_b}^2, m_{W^+}^2) \quad (160)
\end{aligned}$$

• **Self-Energy for CP-even Sneutrino ( $\nu^R$ )**

$$\begin{aligned}
\Pi_{i,j}(p^2) = & +4 \Gamma_{\tilde{\nu}_i^R, \tilde{\nu}_j^R, W^+, W^-} \left( -\frac{1}{2} \text{rMS} m_{W^-}^2 + A_0(m_{W^-}^2) \right) + 2 \Gamma_{\tilde{\nu}_i^R, \tilde{\nu}_j^R, Z, Z} \left( -\frac{1}{2} \text{rMS} m_Z^2 + A_0(m_Z^2) \right) \\
& - \frac{1}{2} \sum_{a=1}^2 A_0(m_{A_a^0}^2) \Gamma_{\tilde{\nu}_i^R, \tilde{\nu}_j^R, A_a^0, A_a^0} - \sum_{a=1}^2 A_0(m_{H_a^-}^2) \Gamma_{\tilde{\nu}_i^R, \tilde{\nu}_j^R, H_a^+, H_a^-} \\
& - \frac{1}{2} \sum_{a=1}^2 A_0(m_{h_a}^2) \Gamma_{\tilde{\nu}_i^R, \tilde{\nu}_j^R, h_a, h_a} - \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^i}^2) \Gamma_{\tilde{\nu}_i^R, \tilde{\nu}_j^R, \nu_a^i, \nu_a^i} \\
& - \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^R}^2) \Gamma_{\tilde{\nu}_i^R, \tilde{\nu}_j^R, \nu_a^R, \nu_a^R} + \sum_{a=1}^3 \sum_{b=1}^2 B_0(p^2, m_{\nu_a^i}^2, m_{A_b^0}^2) \Gamma_{\tilde{\nu}_j^R, \nu_a^i, A_b^0}^* \Gamma_{\tilde{\nu}_i^R, \nu_a^i, A_b^0} \\
& + \sum_{a=1}^3 \sum_{b=1}^2 B_0(p^2, m_{\nu_a^i}^2, m_{h_b}^2) \Gamma_{\tilde{\nu}_j^R, \nu_a^i, h_b}^* \Gamma_{\tilde{\nu}_i^R, \nu_a^i, h_b}
\end{aligned}$$

$$\begin{aligned}
& + \sum_{a=1}^3 \sum_{b=1}^2 B_0(p^2, m_{\nu_a^R}^2, m_{A_b^0}^2) \Gamma_{\tilde{\nu}_j^R, \nu_a^R, A_b^0}^* \Gamma_{\tilde{\nu}_i^R, \nu_a^R, A_b^0} \\
& + \sum_{a=1}^3 \sum_{b=1}^2 B_0(p^2, m_{\nu_a^R}^2, m_{h_b}^2) \Gamma_{\tilde{\nu}_j^R, \nu_a^R, h_b}^* \Gamma_{\tilde{\nu}_i^R, \nu_a^R, h_b} \\
& - 4 \sum_{a=1}^3 m_{e_a} \sum_{b=1}^2 B_0(p^2, m_{e_a}^2, m_{\tilde{\chi}_b^-}^2) m_{\tilde{\chi}_b^-} \left( \Gamma_{\tilde{\nu}_j^R, \bar{e}_a, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{\nu}_i^R, \bar{e}_a, \tilde{\chi}_b^-}^R + \Gamma_{\tilde{\nu}_j^R, \bar{e}_a, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{\nu}_i^R, \bar{e}_a, \tilde{\chi}_b^-}^L \right) \\
& + 2 \sum_{a=1}^3 \sum_{b=1}^2 G_0(p^2, m_{e_a}^2, m_{\tilde{\chi}_b^-}^2) \left( \Gamma_{\tilde{\nu}_j^R, \bar{e}_a, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{\nu}_i^R, \bar{e}_a, \tilde{\chi}_b^-}^L + \Gamma_{\tilde{\nu}_j^R, \bar{e}_a, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{\nu}_i^R, \bar{e}_a, \tilde{\chi}_b^-}^R \right) \\
& - 2 \sum_{a=1}^3 m_{\nu_a} \sum_{b=1}^4 B_0(p^2, m_{\nu_a}^2, m_{\tilde{\chi}_b^0}^2) m_{\tilde{\chi}_b^0} \left( \Gamma_{\tilde{\nu}_j^R, \nu_a, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{\nu}_i^R, \nu_a, \tilde{\chi}_b^0}^R + \Gamma_{\tilde{\nu}_j^R, \nu_a, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{\nu}_i^R, \nu_a, \tilde{\chi}_b^0}^L \right) \\
& + \sum_{a=1}^3 \sum_{b=1}^4 G_0(p^2, m_{\nu_a}^2, m_{\tilde{\chi}_b^0}^2) \left( \Gamma_{\tilde{\nu}_j^R, \nu_a, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{\nu}_i^R, \nu_a, \tilde{\chi}_b^0}^L + \Gamma_{\tilde{\nu}_j^R, \nu_a, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{\nu}_i^R, \nu_a, \tilde{\chi}_b^0}^R \right) \\
& - 3 \sum_{a=1}^6 A_0(m_{\tilde{d}_a}^2) \Gamma_{\tilde{\nu}_i^R, \tilde{\nu}_j^R, \tilde{d}_a^*, \tilde{d}_a} - \sum_{a=1}^6 A_0(m_{\tilde{e}_a}^2) \Gamma_{\tilde{\nu}_i^R, \tilde{\nu}_j^R, \tilde{e}_a^*, \tilde{e}_a} \\
& - 3 \sum_{a=1}^6 A_0(m_{\tilde{u}_a}^2) \Gamma_{\tilde{\nu}_i^R, \tilde{\nu}_j^R, \tilde{u}_a^*, \tilde{u}_a} + 2 \sum_{a=1}^6 \sum_{b=1}^2 B_0(p^2, m_{\tilde{e}_a}^2, m_{H_b^-}^2) \Gamma_{\tilde{\nu}_j^R, \tilde{e}_a^*, H_b^-}^* \Gamma_{\tilde{\nu}_i^R, \tilde{e}_a^*, H_b^-} \\
& + \sum_{b=1}^3 \Gamma_{\tilde{\nu}_j^R, Z, \nu_b^i}^* \Gamma_{\tilde{\nu}_i^R, Z, \nu_b^i} F_0(p^2, m_{\nu_b^i}^2, m_Z^2) + 2 \sum_{b=1}^6 \Gamma_{\tilde{\nu}_j^R, W^+, \tilde{e}_b}^* \Gamma_{\tilde{\nu}_i^R, W^+, \tilde{e}_b} F_0(p^2, m_{\tilde{e}_b}^2, m_{W^-}^2) \quad (161)
\end{aligned}$$

• Self-Energy for Higgs ( $h$ )

$$\begin{aligned}
\Pi_{i,j}(p^2) = & +2 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_Z^2, m_Z^2) \right) \Gamma_{\tilde{h}_j, Z, Z}^* \Gamma_{\tilde{h}_i, Z, Z} + 4 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{W^-}^2, m_{W^-}^2) \right) \Gamma_{\tilde{h}_j, W^+, W^-}^* \Gamma_{\tilde{h}_i, W^+, W^-} \\
& - B_0(p^2, m_{\eta^-}^2, m_{\eta^-}^2) \Gamma_{\tilde{h}_i, \eta^-, \eta^-} \Gamma_{\tilde{h}_j, \eta^-, \eta^-} - B_0(p^2, m_{\eta^+}^2, m_{\eta^+}^2) \Gamma_{\tilde{h}_i, \eta^+, \eta^+} \Gamma_{\tilde{h}_j, \eta^+, \eta^+} \\
& - B_0(p^2, m_{\eta Z}^2, m_{\eta Z}^2) \Gamma_{\tilde{h}_i, \eta Z, \eta Z} \Gamma_{\tilde{h}_j, \eta Z, \eta Z} + 4 \Gamma_{\tilde{h}_i, \tilde{h}_j, W^+, W^-} \left( -\frac{1}{2} \text{rMS} m_{W^-}^2 + A_0(m_{W^-}^2) \right) \\
& + 2 \Gamma_{\tilde{h}_i, \tilde{h}_j, Z, Z} \left( -\frac{1}{2} \text{rMS} m_Z^2 + A_0(m_Z^2) \right) - \frac{1}{2} \sum_{a=1}^2 A_0(m_{A_a^0}^2) \Gamma_{\tilde{h}_i, \tilde{h}_j, A_a^0, A_a^0} \\
& - \sum_{a=1}^2 A_0(m_{H_a^-}^2) \Gamma_{\tilde{h}_i, \tilde{h}_j, H_a^+, H_a^-} - \frac{1}{2} \sum_{a=1}^2 A_0(m_{h_a}^2) \Gamma_{\tilde{h}_i, \tilde{h}_j, h_a, h_a} \\
& + \frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^2 B_0(p^2, m_{A_a^0}^2, m_{A_b^0}^2) \Gamma_{\tilde{h}_j, A_a^0, A_b^0}^* \Gamma_{\tilde{h}_i, A_a^0, A_b^0} \\
& + \sum_{a=1}^2 \sum_{b=1}^2 B_0(p^2, m_{H_a^-}^2, m_{H_b^-}^2) \Gamma_{\tilde{h}_j, H_a^+, H_b^-}^* \Gamma_{\tilde{h}_i, H_a^+, H_b^-}
\end{aligned}$$

$$\begin{aligned}
& + \frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^2 B_0(p^2, m_{h_a}^2, m_{h_b}^2) \Gamma_{\tilde{h}_j, h_a, h_b}^* \Gamma_{\tilde{h}_i, h_a, h_b} \\
& - 2 \sum_{a=1}^2 m_{\tilde{\chi}_a^-} \sum_{b=1}^2 B_0(p^2, m_{\tilde{\chi}_a^-}^2, m_{\tilde{\chi}_b^-}^2) m_{\tilde{\chi}_b^-} \left( \Gamma_{\tilde{h}_j, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{h}_i, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^R + \Gamma_{\tilde{h}_j, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{h}_i, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^L \right) \\
& + \sum_{a=1}^2 \sum_{b=1}^2 G_0(p^2, m_{\tilde{\chi}_a^-}^2, m_{\tilde{\chi}_b^-}^2) \left( \Gamma_{\tilde{h}_j, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{h}_i, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^L + \Gamma_{\tilde{h}_j, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{h}_i, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^R \right) \\
& - \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^i}^2) \Gamma_{\tilde{h}_i, \tilde{h}_j, \nu_a^i, \nu_a^i} - \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^R}^2) \Gamma_{\tilde{h}_i, \tilde{h}_j, \nu_a^R, \nu_a^R} \\
& + \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^3 B_0(p^2, m_{\nu_a^i}^2, m_{\nu_b^i}^2) \Gamma_{\tilde{h}_j, \nu_a^i, \nu_b^i}^* \Gamma_{\tilde{h}_i, \nu_a^i, \nu_b^i} \\
& + \sum_{a=1}^3 \sum_{b=1}^3 B_0(p^2, m_{\nu_a^R}^2, m_{\nu_b^R}^2) \Gamma_{\tilde{h}_j, \nu_a^R, \nu_b^R}^* \Gamma_{\tilde{h}_i, \nu_a^R, \nu_b^R} \\
& + \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^3 B_0(p^2, m_{\nu_a^R}^2, m_{\nu_b^R}^2) \Gamma_{\tilde{h}_j, \nu_a^R, \nu_b^R}^* \Gamma_{\tilde{h}_i, \nu_a^R, \nu_b^R} \\
& - 6 \sum_{a=1}^3 m_{d_a} \sum_{b=1}^3 B_0(p^2, m_{d_a}^2, m_{d_b}^2) m_{d_b} \left( \Gamma_{\tilde{h}_j, \bar{d}_a, d_b}^{L*} \Gamma_{\tilde{h}_i, \bar{d}_a, d_b}^R + \Gamma_{\tilde{h}_j, \bar{d}_a, d_b}^{R*} \Gamma_{\tilde{h}_i, \bar{d}_a, d_b}^L \right) \\
& + 3 \sum_{a=1}^3 \sum_{b=1}^3 G_0(p^2, m_{d_a}^2, m_{d_b}^2) \left( \Gamma_{\tilde{h}_j, \bar{d}_a, d_b}^{L*} \Gamma_{\tilde{h}_i, \bar{d}_a, d_b}^L + \Gamma_{\tilde{h}_j, \bar{d}_a, d_b}^{R*} \Gamma_{\tilde{h}_i, \bar{d}_a, d_b}^R \right) \\
& - 2 \sum_{a=1}^3 m_{e_a} \sum_{b=1}^3 B_0(p^2, m_{e_a}^2, m_{e_b}^2) m_{e_b} \left( \Gamma_{\tilde{h}_j, \bar{e}_a, e_b}^{L*} \Gamma_{\tilde{h}_i, \bar{e}_a, e_b}^R + \Gamma_{\tilde{h}_j, \bar{e}_a, e_b}^{R*} \Gamma_{\tilde{h}_i, \bar{e}_a, e_b}^L \right) \\
& + \sum_{a=1}^3 \sum_{b=1}^3 G_0(p^2, m_{e_a}^2, m_{e_b}^2) \left( \Gamma_{\tilde{h}_j, \bar{e}_a, e_b}^{L*} \Gamma_{\tilde{h}_i, \bar{e}_a, e_b}^L + \Gamma_{\tilde{h}_j, \bar{e}_a, e_b}^{R*} \Gamma_{\tilde{h}_i, \bar{e}_a, e_b}^R \right) \\
& - 6 \sum_{a=1}^3 m_{u_a} \sum_{b=1}^3 B_0(p^2, m_{u_a}^2, m_{u_b}^2) m_{u_b} \left( \Gamma_{\tilde{h}_j, \bar{u}_a, u_b}^{L*} \Gamma_{\tilde{h}_i, \bar{u}_a, u_b}^R + \Gamma_{\tilde{h}_j, \bar{u}_a, u_b}^{R*} \Gamma_{\tilde{h}_i, \bar{u}_a, u_b}^L \right) \\
& + 3 \sum_{a=1}^3 \sum_{b=1}^3 G_0(p^2, m_{u_a}^2, m_{u_b}^2) \left( \Gamma_{\tilde{h}_j, \bar{u}_a, u_b}^{L*} \Gamma_{\tilde{h}_i, \bar{u}_a, u_b}^L + \Gamma_{\tilde{h}_j, \bar{u}_a, u_b}^{R*} \Gamma_{\tilde{h}_i, \bar{u}_a, u_b}^R \right) \\
& - \sum_{a=1}^3 m_{\nu_a} \sum_{b=1}^3 B_0(p^2, m_{\nu_a}^2, m_{\nu_b}^2) m_{\nu_b} \left( \Gamma_{\tilde{h}_j, \nu_a, \nu_b}^{L*} \Gamma_{\tilde{h}_i, \nu_a, \nu_b}^R + \Gamma_{\tilde{h}_j, \nu_a, \nu_b}^{R*} \Gamma_{\tilde{h}_i, \nu_a, \nu_b}^L \right) \\
& + \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^3 G_0(p^2, m_{\nu_a}^2, m_{\nu_b}^2) \left( \Gamma_{\tilde{h}_j, \nu_a, \nu_b}^{L*} \Gamma_{\tilde{h}_i, \nu_a, \nu_b}^L + \Gamma_{\tilde{h}_j, \nu_a, \nu_b}^{R*} \Gamma_{\tilde{h}_i, \nu_a, \nu_b}^R \right)
\end{aligned}$$

$$\begin{aligned}
& - \sum_{a=1}^4 m_{\tilde{\chi}_a^0} \sum_{b=1}^4 B_0(p^2, m_{\tilde{\chi}_a^0}^2, m_{\tilde{\chi}_b^0}^2) m_{\tilde{\chi}_b^0} \left( \Gamma_{\tilde{h}_j, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{h}_i, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^R + \Gamma_{\tilde{h}_j, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{h}_i, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^L \right) \\
& + \frac{1}{2} \sum_{a=1}^4 \sum_{b=1}^4 G_0(p^2, m_{\tilde{\chi}_a^0}^2, m_{\tilde{\chi}_b^0}^2) \left( \Gamma_{\tilde{h}_j, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{h}_i, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^L + \Gamma_{\tilde{h}_j, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{h}_i, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^R \right) \\
& - 3 \sum_{a=1}^6 A_0(m_{\tilde{d}_a}^2) \Gamma_{\tilde{h}_i, \tilde{h}_j, \tilde{d}_a^*, \tilde{d}_a} - \sum_{a=1}^6 A_0(m_{\tilde{e}_a}^2) \Gamma_{\tilde{h}_i, \tilde{h}_j, \tilde{e}_a^*, \tilde{e}_a} \\
& - 3 \sum_{a=1}^6 A_0(m_{\tilde{u}_a}^2) \Gamma_{\tilde{h}_i, \tilde{h}_j, \tilde{u}_a^*, \tilde{u}_a} + 3 \sum_{a=1}^6 \sum_{b=1}^6 B_0(p^2, m_{\tilde{d}_a}^2, m_{\tilde{d}_b}^2) \Gamma_{\tilde{h}_j, \tilde{d}_a^*, \tilde{d}_b}^* \Gamma_{\tilde{h}_i, \tilde{d}_a^*, \tilde{d}_b} \\
& + \sum_{a=1}^6 \sum_{b=1}^6 B_0(p^2, m_{\tilde{e}_a}^2, m_{\tilde{e}_b}^2) \Gamma_{\tilde{h}_j, \tilde{e}_a^*, \tilde{e}_b}^* \Gamma_{\tilde{h}_i, \tilde{e}_a^*, \tilde{e}_b} + 3 \sum_{a=1}^6 \sum_{b=1}^6 B_0(p^2, m_{\tilde{u}_a}^2, m_{\tilde{u}_b}^2) \Gamma_{\tilde{h}_j, \tilde{u}_a^*, \tilde{u}_b}^* \Gamma_{\tilde{h}_i, \tilde{u}_a^*, \tilde{u}_b} \\
& + \sum_{b=1}^2 \Gamma_{\tilde{h}_j, Z, A_b^0}^* \Gamma_{\tilde{h}_i, Z, A_b^0} F_0(p^2, m_{A_b^0}^2, m_Z^2) + 2 \sum_{b=1}^2 \Gamma_{\tilde{h}_j, W^+, H_b^-}^* \Gamma_{\tilde{h}_i, W^+, H_b^-} F_0(p^2, m_{H_b^-}^2, m_{W^-}^2) \tag{162}
\end{aligned}$$

• Self-Energy for Pseudo-Scalar Higgs ( $A^0$ )

$$\begin{aligned}
\Pi_{i,j}(p^2) & = -B_0(p^2, m_{\eta^-}^2, m_{\eta^-}^2) \Gamma_{\tilde{A}_i^0, \eta^-, \eta^-, \eta^-} \Gamma_{\tilde{A}_j^0, \eta^-, \eta^-, \eta^-} - B_0(p^2, m_{\eta^+}^2, m_{\eta^+}^2) \Gamma_{\tilde{A}_i^0, \eta^+, \eta^+, \eta^+} \\
& + 4 \Gamma_{\tilde{A}_i^0, \tilde{A}_j^0, W^+, W^-} \left( -\frac{1}{2} \text{rMS} m_{W^-}^2 + A_0(m_{W^-}^2) \right) + 2 \Gamma_{\tilde{A}_i^0, \tilde{A}_j^0, Z, Z} \left( -\frac{1}{2} \text{rMS} m_Z^2 + A_0(m_Z^2) \right) \\
& - \frac{1}{2} \sum_{a=1}^2 A_0(m_{A_a^0}^2) \Gamma_{\tilde{A}_i^0, \tilde{A}_j^0, A_a^0, A_a^0} - \sum_{a=1}^2 A_0(m_{H_a^-}^2) \Gamma_{\tilde{A}_i^0, \tilde{A}_j^0, H_a^+, H_a^-} \\
& - \frac{1}{2} \sum_{a=1}^2 A_0(m_{h_a}^2) \Gamma_{\tilde{A}_i^0, \tilde{A}_j^0, h_a, h_a} + \sum_{a=1}^2 \sum_{b=1}^2 B_0(p^2, m_{H_a^-}^2, m_{H_b^-}^2) \Gamma_{\tilde{A}_j^0, H_a^+, H_b^-}^* \Gamma_{\tilde{A}_i^0, H_a^+, H_b^-} \\
& + \sum_{a=1}^2 \sum_{b=1}^2 B_0(p^2, m_{h_a}^2, m_{A_b^0}^2) \Gamma_{\tilde{A}_j^0, h_a, A_b^0}^* \Gamma_{\tilde{A}_i^0, h_a, A_b^0} \\
& - 2 \sum_{a=1}^2 m_{\tilde{\chi}_a^-} \sum_{b=1}^2 B_0(p^2, m_{\tilde{\chi}_a^-}^2, m_{\tilde{\chi}_b^-}^2) m_{\tilde{\chi}_b^-} \left( \Gamma_{\tilde{A}_j^0, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{A}_i^0, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^R + \Gamma_{\tilde{A}_j^0, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{A}_i^0, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^L \right) \\
& + \sum_{a=1}^2 \sum_{b=1}^2 G_0(p^2, m_{\tilde{\chi}_a^-}^2, m_{\tilde{\chi}_b^-}^2) \left( \Gamma_{\tilde{A}_j^0, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{A}_i^0, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^L + \Gamma_{\tilde{A}_j^0, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{A}_i^0, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^R \right) \\
& - \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^i}^2) \Gamma_{\tilde{A}_i^0, \tilde{A}_j^0, \nu_a^i, \nu_a^i} - \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^R}^2) \Gamma_{\tilde{A}_i^0, \tilde{A}_j^0, \nu_a^R, \nu_a^R} \\
& + \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^3 B_0(p^2, m_{\nu_a^i}^2, m_{\nu_b^i}^2) \Gamma_{\tilde{A}_j^0, \nu_a^i, \nu_b^i}^* \Gamma_{\tilde{A}_i^0, \nu_a^i, \nu_b^i}
\end{aligned}$$

$$\begin{aligned}
& + \sum_{a=1}^3 \sum_{b=1}^3 B_0(p^2, m_{\nu_a^R}^2, m_{\nu_b^R}^2) \Gamma_{\check{A}_j^0, \nu_a^R, \nu_b^R}^* \Gamma_{\check{A}_i^0, \nu_a^R, \nu_b^R} \\
& + \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^3 B_0(p^2, m_{\nu_a^R}^2, m_{\nu_b^R}^2) \Gamma_{\check{A}_j^0, \nu_a^R, \nu_b^R}^* \Gamma_{\check{A}_i^0, \nu_a^R, \nu_b^R} \\
& - 6 \sum_{a=1}^3 m_{d_a} \sum_{b=1}^3 B_0(p^2, m_{d_a}^2, m_{d_b}^2) m_{d_b} \left( \Gamma_{\check{A}_j^0, \bar{d}_a, d_b}^{L*} \Gamma_{\check{A}_i^0, \bar{d}_a, d_b}^R + \Gamma_{\check{A}_j^0, \bar{d}_a, d_b}^{R*} \Gamma_{\check{A}_i^0, \bar{d}_a, d_b}^L \right) \\
& + 3 \sum_{a=1}^3 \sum_{b=1}^3 G_0(p^2, m_{d_a}^2, m_{d_b}^2) \left( \Gamma_{\check{A}_j^0, \bar{d}_a, d_b}^{L*} \Gamma_{\check{A}_i^0, \bar{d}_a, d_b}^L + \Gamma_{\check{A}_j^0, \bar{d}_a, d_b}^{R*} \Gamma_{\check{A}_i^0, \bar{d}_a, d_b}^R \right) \\
& - 2 \sum_{a=1}^3 m_{e_a} \sum_{b=1}^3 B_0(p^2, m_{e_a}^2, m_{e_b}^2) m_{e_b} \left( \Gamma_{\check{A}_j^0, \bar{e}_a, e_b}^{L*} \Gamma_{\check{A}_i^0, \bar{e}_a, e_b}^R + \Gamma_{\check{A}_j^0, \bar{e}_a, e_b}^{R*} \Gamma_{\check{A}_i^0, \bar{e}_a, e_b}^L \right) \\
& + \sum_{a=1}^3 \sum_{b=1}^3 G_0(p^2, m_{e_a}^2, m_{e_b}^2) \left( \Gamma_{\check{A}_j^0, \bar{e}_a, e_b}^{L*} \Gamma_{\check{A}_i^0, \bar{e}_a, e_b}^L + \Gamma_{\check{A}_j^0, \bar{e}_a, e_b}^{R*} \Gamma_{\check{A}_i^0, \bar{e}_a, e_b}^R \right) \\
& - 6 \sum_{a=1}^3 m_{u_a} \sum_{b=1}^3 B_0(p^2, m_{u_a}^2, m_{u_b}^2) m_{u_b} \left( \Gamma_{\check{A}_j^0, \bar{u}_a, u_b}^{L*} \Gamma_{\check{A}_i^0, \bar{u}_a, u_b}^R + \Gamma_{\check{A}_j^0, \bar{u}_a, u_b}^{R*} \Gamma_{\check{A}_i^0, \bar{u}_a, u_b}^L \right) \\
& + 3 \sum_{a=1}^3 \sum_{b=1}^3 G_0(p^2, m_{u_a}^2, m_{u_b}^2) \left( \Gamma_{\check{A}_j^0, \bar{u}_a, u_b}^{L*} \Gamma_{\check{A}_i^0, \bar{u}_a, u_b}^L + \Gamma_{\check{A}_j^0, \bar{u}_a, u_b}^{R*} \Gamma_{\check{A}_i^0, \bar{u}_a, u_b}^R \right) \\
& - \sum_{a=1}^3 m_{\nu_a} \sum_{b=1}^3 B_0(p^2, m_{\nu_a}^2, m_{\nu_b}^2) m_{\nu_b} \left( \Gamma_{\check{A}_j^0, \nu_a, \nu_b}^{L*} \Gamma_{\check{A}_i^0, \nu_a, \nu_b}^R + \Gamma_{\check{A}_j^0, \nu_a, \nu_b}^{R*} \Gamma_{\check{A}_i^0, \nu_a, \nu_b}^L \right) \\
& + \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^3 G_0(p^2, m_{\nu_a}^2, m_{\nu_b}^2) \left( \Gamma_{\check{A}_j^0, \nu_a, \nu_b}^{L*} \Gamma_{\check{A}_i^0, \nu_a, \nu_b}^L + \Gamma_{\check{A}_j^0, \nu_a, \nu_b}^{R*} \Gamma_{\check{A}_i^0, \nu_a, \nu_b}^R \right) \\
& - \sum_{a=1}^4 m_{\tilde{\chi}_a^0} \sum_{b=1}^4 B_0(p^2, m_{\tilde{\chi}_a^0}^2, m_{\tilde{\chi}_b^0}^2) m_{\tilde{\chi}_b^0} \left( \Gamma_{\check{A}_j^0, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^{L*} \Gamma_{\check{A}_i^0, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^R + \Gamma_{\check{A}_j^0, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^{R*} \Gamma_{\check{A}_i^0, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^L \right) \\
& + \frac{1}{2} \sum_{a=1}^4 \sum_{b=1}^4 G_0(p^2, m_{\tilde{\chi}_a^0}^2, m_{\tilde{\chi}_b^0}^2) \left( \Gamma_{\check{A}_j^0, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^{L*} \Gamma_{\check{A}_i^0, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^L + \Gamma_{\check{A}_j^0, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^{R*} \Gamma_{\check{A}_i^0, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^R \right) \\
& - 3 \sum_{a=1}^6 A_0(m_{\tilde{d}_a}^2) \Gamma_{\check{A}_i^0, \check{A}_j^0, \tilde{d}_a^*, \tilde{d}_a} - \sum_{a=1}^6 A_0(m_{\tilde{e}_a}^2) \Gamma_{\check{A}_i^0, \check{A}_j^0, \tilde{e}_a^*, \tilde{e}_a} \\
& - 3 \sum_{a=1}^6 A_0(m_{\tilde{u}_a}^2) \Gamma_{\check{A}_i^0, \check{A}_j^0, \tilde{u}_a^*, \tilde{u}_a} + 3 \sum_{a=1}^6 \sum_{b=1}^6 B_0(p^2, m_{\tilde{d}_a}^2, m_{\tilde{d}_b}^2) \Gamma_{\check{A}_j^0, \tilde{d}_a^*, \tilde{d}_b}^* \Gamma_{\check{A}_i^0, \tilde{d}_a^*, \tilde{d}_b} \\
& + \sum_{a=1}^6 \sum_{b=1}^6 B_0(p^2, m_{\tilde{e}_a}^2, m_{\tilde{e}_b}^2) \Gamma_{\check{A}_j^0, \tilde{e}_a^*, \tilde{e}_b}^* \Gamma_{\check{A}_i^0, \tilde{e}_a^*, \tilde{e}_b}
\end{aligned}$$

$$\begin{aligned}
& + 3 \sum_{a=1}^6 \sum_{b=1}^6 B_0(p^2, m_{\tilde{u}_a}^2, m_{\tilde{u}_b}^2) \Gamma_{\tilde{A}_j^0, \tilde{u}_a^*, \tilde{u}_b}^* \Gamma_{\tilde{A}_i^0, \tilde{u}_a^*, \tilde{u}_b} + \sum_{b=1}^2 \Gamma_{\tilde{A}_j^0, Z, h_b}^* \Gamma_{\tilde{A}_i^0, Z, h_b} F_0(p^2, m_{h_b}^2, m_Z^2) \\
& + 2 \sum_{b=1}^2 \Gamma_{\tilde{A}_j^0, W^+, H_b^-}^* \Gamma_{\tilde{A}_i^0, W^+, H_b^-} F_0(p^2, m_{H_b^-}^2, m_{W^-}^2)
\end{aligned} \tag{163}$$

• Self-Energy for Charged Higgs ( $H^-$ )

$$\begin{aligned}
\Pi_{i,j}(p^2) = & +4 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, 0, m_{W^-}^2) \right) \Gamma_{\tilde{H}_j^+, W^-, \gamma}^* \Gamma_{\tilde{H}_i^+, W^-, \gamma} + 4 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{W^-}^2, m_Z^2) \right) \Gamma_{\tilde{H}_j^+, Z, W^-}^* \Gamma_{\tilde{H}_i^+, Z, W^-} \\
& - B_0(p^2, m_{\eta^Z}^2, m_{\eta^+}^2) \Gamma_{\tilde{H}_i^+, \eta^+, \eta^Z} \Gamma_{\tilde{H}_j^-, \eta^+, \eta^Z} - B_0(p^2, m_{\eta^-}^2, m_{\eta^Z}^2) \Gamma_{\tilde{H}_i^+, \eta^Z, \eta^-} \Gamma_{\tilde{H}_j^-, \eta^Z, \eta^-} \\
& + 4 \Gamma_{\tilde{H}_i^-, \tilde{H}_j^+, W^+, W^-} \left( -\frac{1}{2} \text{rMS} m_{W^-}^2 + A_0(m_{W^-}^2) \right) + 2 \Gamma_{\tilde{H}_i^-, \tilde{H}_j^+, Z, Z} \left( -\frac{1}{2} \text{rMS} m_Z^2 + A_0(m_Z^2) \right) \\
& - \frac{1}{2} \sum_{a=1}^2 A_0(m_{A_a^0}^2) \Gamma_{\tilde{H}_i^-, \tilde{H}_j^+, A_a^0, A_a^0} - \sum_{a=1}^2 A_0(m_{H_a^-}^2) \Gamma_{\tilde{H}_i^-, \tilde{H}_j^+, H_a^+, H_a^-} \\
& - \frac{1}{2} \sum_{a=1}^2 A_0(m_{h_a}^2) \Gamma_{\tilde{H}_i^-, \tilde{H}_j^+, h_a, h_a} + \sum_{a=1}^2 \sum_{b=1}^2 B_0(p^2, m_{H_a^-}^2, m_{A_b^0}^2) \Gamma_{\tilde{H}_j^+, H_a^-, A_b^0}^* \Gamma_{\tilde{H}_i^+, H_a^-, A_b^0} \\
& + \sum_{a=1}^2 \sum_{b=1}^2 B_0(p^2, m_{H_a^-}^2, m_{h_b}^2) \Gamma_{\tilde{H}_j^+, H_a^-, h_b}^* \Gamma_{\tilde{H}_i^+, H_a^-, h_b} - \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^i}^2) \Gamma_{\tilde{H}_i^-, \tilde{H}_j^+, \nu_a^i, \nu_a^i} \\
& - \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^R}^2) \Gamma_{\tilde{H}_i^-, \tilde{H}_j^+, \nu_a^R, \nu_a^R} \\
& - 6 \sum_{a=1}^3 m_{u_a} \sum_{b=1}^3 B_0(p^2, m_{u_a}^2, m_{d_b}^2) m_{d_b} \left( \Gamma_{\tilde{H}_j^+, \bar{u}_a, d_b}^{L*} \Gamma_{\tilde{H}_i^+, \bar{u}_a, d_b}^R + \Gamma_{\tilde{H}_j^+, \bar{u}_a, d_b}^{R*} \Gamma_{\tilde{H}_i^+, \bar{u}_a, d_b}^L \right) \\
& + 3 \sum_{a=1}^3 \sum_{b=1}^3 G_0(p^2, m_{u_a}^2, m_{d_b}^2) \left( \Gamma_{\tilde{H}_j^+, \bar{u}_a, d_b}^L \Gamma_{\tilde{H}_i^+, \bar{u}_a, d_b}^L + \Gamma_{\tilde{H}_j^+, \bar{u}_a, d_b}^R \Gamma_{\tilde{H}_i^+, \bar{u}_a, d_b}^R \right) \\
& - 2 \sum_{a=1}^3 m_{\nu_a} \sum_{b=1}^3 B_0(p^2, m_{\nu_a}^2, m_{e_b}^2) m_{e_b} \left( \Gamma_{\tilde{H}_j^+, \nu_a, e_b}^{L*} \Gamma_{\tilde{H}_i^+, \nu_a, e_b}^R + \Gamma_{\tilde{H}_j^+, \nu_a, e_b}^{R*} \Gamma_{\tilde{H}_i^+, \nu_a, e_b}^L \right) \\
& + \sum_{a=1}^3 \sum_{b=1}^3 G_0(p^2, m_{\nu_a}^2, m_{e_b}^2) \left( \Gamma_{\tilde{H}_j^+, \nu_a, e_b}^{L*} \Gamma_{\tilde{H}_i^+, \nu_a, e_b}^L + \Gamma_{\tilde{H}_j^+, \nu_a, e_b}^{R*} \Gamma_{\tilde{H}_i^+, \nu_a, e_b}^R \right) \\
& + \sum_{a=1}^3 \sum_{b=1}^6 B_0(p^2, m_{\nu_a^i}^2, m_{\tilde{e}_b}^2) \Gamma_{\tilde{H}_j^+, \nu_a^i, \tilde{e}_b}^* \Gamma_{\tilde{H}_i^+, \nu_a^i, \tilde{e}_b} \\
& + \sum_{a=1}^3 \sum_{b=1}^6 B_0(p^2, m_{\nu_a^R}^2, m_{\tilde{e}_b}^2) \Gamma_{\tilde{H}_j^+, \nu_a^R, \tilde{e}_b}^* \Gamma_{\tilde{H}_i^+, \nu_a^R, \tilde{e}_b}
\end{aligned}$$

$$\begin{aligned}
& - 2 \sum_{a=1}^4 m_{\tilde{\chi}_a^0} \sum_{b=1}^2 B_0(p^2, m_{\tilde{\chi}_a^0}^2, m_{\tilde{\chi}_b^-}^2) m_{\tilde{\chi}_b^-} \left( \Gamma_{H_j^+, \tilde{\chi}_a^0, \tilde{\chi}_b^-}^{L*} \Gamma_{H_i^+, \tilde{\chi}_a^0, \tilde{\chi}_b^-}^R + \Gamma_{H_j^+, \tilde{\chi}_a^0, \tilde{\chi}_b^-}^{R*} \Gamma_{H_i^+, \tilde{\chi}_a^0, \tilde{\chi}_b^-}^L \right) \\
& + \sum_{a=1}^4 \sum_{b=1}^2 G_0(p^2, m_{\tilde{\chi}_a^0}^2, m_{\tilde{\chi}_b^-}^2) \left( \Gamma_{H_j^+, \tilde{\chi}_a^0, \tilde{\chi}_b^-}^{L*} \Gamma_{H_i^+, \tilde{\chi}_a^0, \tilde{\chi}_b^-}^L + \Gamma_{H_j^+, \tilde{\chi}_a^0, \tilde{\chi}_b^-}^{R*} \Gamma_{H_i^+, \tilde{\chi}_a^0, \tilde{\chi}_b^-}^R \right) \\
& - 3 \sum_{a=1}^6 A_0(m_{d_a}^2) \Gamma_{H_i^-, H_j^+, \tilde{d}_a^*, \tilde{d}_a} \Gamma_{H_i^-, H_j^+, \tilde{e}_a^*, \tilde{e}_a} \\
& - 3 \sum_{a=1}^6 A_0(m_{\tilde{u}_a}^2) \Gamma_{H_i^-, H_j^+, \tilde{u}_a^*, \tilde{u}_a} + 3 \sum_{a=1}^6 \sum_{b=1}^6 B_0(p^2, m_{\tilde{u}_a}^2, m_{\tilde{d}_b}^2) \Gamma_{H_j^+, \tilde{u}_a^*, \tilde{d}_b}^* \Gamma_{H_i^+, \tilde{u}_a^*, \tilde{d}_b} \\
& + \sum_{b=1}^2 \Gamma_{H_j^+, W^-, A_b^0}^* \Gamma_{H_i^+, W^-, A_b^0} F_0(p^2, m_{A_b^0}^2, m_{W^-}^2) + \sum_{b=1}^2 \Gamma_{H_j^+, W^-, h_b}^* \Gamma_{H_i^+, W^-, h_b} F_0(p^2, m_{h_b}^2, m_{W^-}^2) \\
& + \sum_{b=1}^2 \Gamma_{H_j^+, \gamma, H_b^-}^* \Gamma_{H_i^+, \gamma, H_b^-} F_0(p^2, m_{H_b^-}^2, 0) + \sum_{b=1}^2 \Gamma_{H_j^+, Z, H_b^-}^* \Gamma_{H_i^+, Z, H_b^-} F_0(p^2, m_{H_b^-}^2, m_Z^2)
\end{aligned} \tag{164}$$

• **Self-Energy for Neutralinos ( $\tilde{\chi}^0$ )**

$$\begin{aligned}
\Sigma_{i,j}^S(p^2) = & + 2 \sum_{a=1}^2 \sum_{b=1}^2 B_0(p^2, m_{\tilde{\chi}_b^-}^2, m_{H_a^-}^2) \Gamma_{\tilde{\chi}_j^0, H_a^+, \tilde{\chi}_b^-}^{L*} m_{\tilde{\chi}_b^-} \Gamma_{\tilde{\chi}_i^0, H_a^+, \tilde{\chi}_b^-}^R \\
& + \sum_{a=1}^2 \sum_{b=1}^4 B_0(p^2, m_{\tilde{\chi}_b^0}^2, m_{h_a}^2) \Gamma_{\tilde{\chi}_j^0, h_a, \tilde{\chi}_b^0}^{L*} m_{\tilde{\chi}_b^0} \Gamma_{\tilde{\chi}_i^0, h_a, \tilde{\chi}_b^0}^R \\
& + \sum_{a=1}^3 \sum_{b=1}^3 B_0(p^2, m_{\nu_b}^2, m_{\nu_a^i}^2) \Gamma_{\tilde{\chi}_j^0, \nu_a^i, \nu_b}^{L*} m_{\nu_b} \Gamma_{\tilde{\chi}_i^0, \nu_a^i, \nu_b}^R \\
& + \sum_{a=1}^3 \sum_{b=1}^3 B_0(p^2, m_{\nu_b}^2, m_{\nu_a^R}^2) \Gamma_{\tilde{\chi}_j^0, \nu_a^R, \nu_b}^{L*} m_{\nu_b} \Gamma_{\tilde{\chi}_i^0, \nu_a^R, \nu_b}^R \\
& + \sum_{a=1}^4 m_{\tilde{\chi}_a^0} \sum_{b=1}^2 B_0(p^2, m_{\tilde{\chi}_a^0}^2, m_{A_b^0}^2) \Gamma_{\tilde{\chi}_j^0, \tilde{\chi}_a^0, A_b^0}^{L*} \Gamma_{\tilde{\chi}_i^0, \tilde{\chi}_a^0, A_b^0}^R \\
& + 6 \sum_{a=1}^6 \sum_{b=1}^3 B_0(p^2, m_{d_b}^2, m_{\tilde{d}_a}^2) \Gamma_{\tilde{\chi}_j^0, \tilde{d}_a^*, d_b}^{L*} m_{d_b} \Gamma_{\tilde{\chi}_i^0, \tilde{d}_a^*, d_b}^R \\
& + 2 \sum_{a=1}^6 \sum_{b=1}^3 B_0(p^2, m_{e_b}^2, m_{\tilde{e}_a}^2) \Gamma_{\tilde{\chi}_j^0, \tilde{e}_a^*, e_b}^{L*} m_{e_b} \Gamma_{\tilde{\chi}_i^0, \tilde{e}_a^*, e_b}^R \\
& + 6 \sum_{a=1}^6 \sum_{b=1}^3 B_0(p^2, m_{u_b}^2, m_{\tilde{u}_a}^2) \Gamma_{\tilde{\chi}_j^0, \tilde{u}_a^*, u_b}^{L*} m_{u_b} \Gamma_{\tilde{\chi}_i^0, \tilde{u}_a^*, u_b}^R
\end{aligned}$$

$$\begin{aligned}
& -8 \sum_{b=1}^2 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{\tilde{\chi}_b^-}^2, m_{W^-}^2) \right) \Gamma_{\tilde{\chi}_j^0, W^+, \tilde{\chi}_b^-}^{R*} m_{\tilde{\chi}_b^-} \Gamma_{\tilde{\chi}_i^0, W^+, \tilde{\chi}_b^-}^L \\
& -4 \sum_{b=1}^4 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{\tilde{\chi}_b^0}^2, m_Z^2) \right) \Gamma_{\tilde{\chi}_j^0, Z, \tilde{\chi}_b^0}^{R*} m_{\tilde{\chi}_b^0} \Gamma_{\tilde{\chi}_i^0, Z, \tilde{\chi}_b^0}^L
\end{aligned} \tag{165}$$

$$\begin{aligned}
\Sigma_{i,j}^R(p^2) = & - \sum_{a=1}^2 \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_b^-}^2, m_{H_a^+}^2) \Gamma_{\tilde{\chi}_j^0, H_a^+, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{\chi}_i^0, H_a^+, \tilde{\chi}_b^-}^R \\
& - \frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^4 B_1(p^2, m_{\tilde{\chi}_b^0}^2, m_{h_a}^2) \Gamma_{\tilde{\chi}_j^0, h_a, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{\chi}_i^0, h_a, \tilde{\chi}_b^0}^R \\
& - \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^3 B_1(p^2, m_{\nu_b}^2, m_{\nu_a^i}^2) \Gamma_{\tilde{\chi}_j^0, \nu_a^i, \nu_b}^{R*} \Gamma_{\tilde{\chi}_i^0, \nu_a^i, \nu_b}^R \\
& - \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^3 B_1(p^2, m_{\nu_b}^2, m_{\nu_a^R}^2) \Gamma_{\tilde{\chi}_j^0, \nu_a^R, \nu_b}^{R*} \Gamma_{\tilde{\chi}_i^0, \nu_a^R, \nu_b}^R \\
& - \frac{1}{2} \sum_{a=1}^4 \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_a^0}^2, m_{A_b^0}^2) \Gamma_{\tilde{\chi}_j^0, \tilde{\chi}_a^0, A_b^0}^{R*} \Gamma_{\tilde{\chi}_i^0, \tilde{\chi}_a^0, A_b^0}^R \\
& - 3 \sum_{a=1}^6 \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_{\tilde{d}_a}^2) \Gamma_{\tilde{\chi}_j^0, \tilde{d}_a^*, d_b}^{R*} \Gamma_{\tilde{\chi}_i^0, \tilde{d}_a^*, d_b}^R \\
& - \sum_{a=1}^6 \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, m_{\tilde{e}_a}^2) \Gamma_{\tilde{\chi}_j^0, \tilde{e}_a^*, e_b}^{R*} \Gamma_{\tilde{\chi}_i^0, \tilde{e}_a^*, e_b}^R \\
& - 3 \sum_{a=1}^6 \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_{\tilde{u}_a}^2) \Gamma_{\tilde{\chi}_j^0, \tilde{u}_a^*, u_b}^{R*} \Gamma_{\tilde{\chi}_i^0, \tilde{u}_a^*, u_b}^R \\
& - 2 \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_b^-}^2, m_{W^-}^2) \Gamma_{\tilde{\chi}_j^0, W^+, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{\chi}_i^0, W^+, \tilde{\chi}_b^-}^L - \sum_{b=1}^4 B_1(p^2, m_{\tilde{\chi}_b^0}^2, m_Z^2) \Gamma_{\tilde{\chi}_j^0, Z, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{\chi}_i^0, Z, \tilde{\chi}_b^0}^L
\end{aligned} \tag{166}$$

$$\begin{aligned}
\Sigma_{i,j}^L(p^2) = & - \sum_{a=1}^2 \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_b^-}^2, m_{H_a^+}^2) \Gamma_{\tilde{\chi}_j^0, H_a^+, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{\chi}_i^0, H_a^+, \tilde{\chi}_b^-}^L \\
& - \frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^4 B_1(p^2, m_{\tilde{\chi}_b^0}^2, m_{h_a}^2) \Gamma_{\tilde{\chi}_j^0, h_a, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{\chi}_i^0, h_a, \tilde{\chi}_b^0}^L \\
& - \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^3 B_1(p^2, m_{\nu_b}^2, m_{\nu_a^i}^2) \Gamma_{\tilde{\chi}_j^0, \nu_a^i, \nu_b}^{L*} \Gamma_{\tilde{\chi}_i^0, \nu_a^i, \nu_b}^L \\
& - \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^3 B_1(p^2, m_{\nu_b}^2, m_{\nu_a^R}^2) \Gamma_{\tilde{\chi}_j^0, \nu_a^R, \nu_b}^{L*} \Gamma_{\tilde{\chi}_i^0, \nu_a^R, \nu_b}^L
\end{aligned}$$

$$\begin{aligned}
& - \frac{1}{2} \sum_{a=1}^4 \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_a^0}^2, m_{A_b^0}^2) \Gamma_{\tilde{\chi}_j^0, \tilde{\chi}_a^0, A_b^0}^{L*} \Gamma_{\tilde{\chi}_i^0, \tilde{\chi}_a^0, A_b^0}^L \\
& - 3 \sum_{a=1}^6 \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_{\tilde{d}_a}^2) \Gamma_{\tilde{\chi}_j^0, \tilde{d}_a^*, d_b}^{L*} \Gamma_{\tilde{\chi}_i^0, \tilde{d}_a^*, d_b}^L \\
& - \sum_{a=1}^6 \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, m_{\tilde{e}_a}^2) \Gamma_{\tilde{\chi}_j^0, \tilde{e}_a^*, e_b}^{L*} \Gamma_{\tilde{\chi}_i^0, \tilde{e}_a^*, e_b}^L \\
& - 3 \sum_{a=1}^6 \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_{\tilde{u}_a}^2) \Gamma_{\tilde{\chi}_j^0, \tilde{u}_a^*, u_b}^{L*} \Gamma_{\tilde{\chi}_i^0, \tilde{u}_a^*, u_b}^L \\
& - 2 \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_b^-}^2, m_{W^-}^2) \Gamma_{\tilde{\chi}_j^0, W^+, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{\chi}_i^0, W^+, \tilde{\chi}_b^-}^R - \sum_{b=1}^4 B_1(p^2, m_{\tilde{\chi}_b^0}^2, m_Z^2) \Gamma_{\tilde{\chi}_j^0, Z, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{\chi}_i^0, Z, \tilde{\chi}_b^0}^R \quad (167)
\end{aligned}$$

• Self-Energy for Neutrinos ( $\nu$ )

$$\begin{aligned}
\Sigma_{i,j}^S(p^2) = & +2 \sum_{a=1}^2 \sum_{b=1}^3 B_0(p^2, m_{e_b}^2, m_{H_a^+}^2) \Gamma_{\tilde{\nu}_j, H_a^+, e_b}^{L*} m_{e_b} \Gamma_{\tilde{\nu}_i, H_a^+, e_b}^R \\
& + \sum_{a=1}^2 \sum_{b=1}^3 B_0(p^2, m_{\nu_b}^2, m_{h_a}^2) \Gamma_{\tilde{\nu}_j, h_a, \nu_b}^{L*} m_{\nu_b} \Gamma_{\tilde{\nu}_i, h_a, \nu_b}^R \\
& + \sum_{a=1}^3 m_{\nu_a} \sum_{b=1}^2 B_0(p^2, m_{\nu_a}^2, m_{A_b^0}^2) \Gamma_{\tilde{\nu}_j, \nu_a, A_b^0}^{L*} \Gamma_{\tilde{\nu}_i, \nu_a, A_b^0}^R \\
& + \sum_{a=1}^3 \sum_{b=1}^4 B_0(p^2, m_{\tilde{\chi}_b^0}^2, m_{\nu_a^i}^2) \Gamma_{\tilde{\nu}_j, \nu_a^i, \tilde{\chi}_b^0}^{L*} m_{\tilde{\chi}_b^0} \Gamma_{\tilde{\nu}_i, \nu_a^i, \tilde{\chi}_b^0}^R \\
& + \sum_{a=1}^3 \sum_{b=1}^4 B_0(p^2, m_{\tilde{\chi}_b^0}^2, m_{\nu_a^R}^2) \Gamma_{\tilde{\nu}_j, \nu_a^R, \tilde{\chi}_b^0}^{L*} m_{\tilde{\chi}_b^0} \Gamma_{\tilde{\nu}_i, \nu_a^R, \tilde{\chi}_b^0}^R \\
& + 2 \sum_{a=1}^6 \sum_{b=1}^2 B_0(p^2, m_{\tilde{\chi}_b^-}^2, m_{\tilde{e}_a}^2) \Gamma_{\tilde{\nu}_j, \tilde{e}_a^*, \tilde{\chi}_b^-}^{L*} m_{\tilde{\chi}_b^-} \Gamma_{\tilde{\nu}_i, \tilde{e}_a^*, \tilde{\chi}_b^-}^R \\
& - 4 \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{\nu_b}^2, m_Z^2) \right) \Gamma_{\tilde{\nu}_j, Z, \nu_b}^{R*} m_{\nu_b} \Gamma_{\tilde{\nu}_i, Z, \nu_b}^L \\
& - 8 \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{e_b}^2, m_{W^-}^2) \right) \Gamma_{\tilde{\nu}_j, W^+, e_b}^{R*} m_{e_b} \Gamma_{\tilde{\nu}_i, W^+, e_b}^L \\
\Sigma_{i,j}^R(p^2) = & - \sum_{a=1}^2 \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, m_{H_a^+}^2) \Gamma_{\tilde{\nu}_j, H_a^+, e_b}^{R*} \Gamma_{\tilde{\nu}_i, H_a^+, e_b}^R
\end{aligned} \quad (168)$$

$$\begin{aligned}
& - \frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^3 B_1(p^2, m_{\nu_b}^2, m_{h_a}^2) \Gamma_{\tilde{\nu}_j, h_a, \nu_b}^{R*} \Gamma_{\tilde{\nu}_i, h_a, \nu_b}^R \\
& - \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^2 B_1(p^2, m_{\nu_a}^2, m_{A_b^0}^2) \Gamma_{\tilde{\nu}_j, \nu_a, A_b^0}^{R*} \Gamma_{\tilde{\nu}_i, \nu_a, A_b^0}^R \\
& - \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^4 B_1(p^2, m_{\tilde{\chi}_b^0}^2, m_{\nu_a^i}^2) \Gamma_{\tilde{\nu}_j, \nu_a^i, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{\nu}_i, \nu_a^i, \tilde{\chi}_b^0}^R \\
& - \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^4 B_1(p^2, m_{\tilde{\chi}_b^0}^2, m_{\nu_a^R}^2) \Gamma_{\tilde{\nu}_j, \nu_a^R, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{\nu}_i, \nu_a^R, \tilde{\chi}_b^0}^R \\
& - \sum_{a=1}^6 \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_b^-}^2, m_{\tilde{e}_a}^2) \Gamma_{\tilde{\nu}_j, \tilde{e}_a^*, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{\nu}_i, \tilde{e}_a^*, \tilde{\chi}_b^-}^R - \sum_{b=1}^3 B_1(p^2, m_{\nu_b}^2, m_Z^2) \Gamma_{\tilde{\nu}_j, Z, \nu_b}^{L*} \Gamma_{\tilde{\nu}_i, Z, \nu_b}^L \\
& - 2 \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, m_{W^-}^2) \Gamma_{\tilde{\nu}_j, W^+, e_b}^{L*} \Gamma_{\tilde{\nu}_i, W^+, e_b}^L
\end{aligned} \tag{169}$$

$$\begin{aligned}
\Sigma_{i,j}^L(p^2) = & - \sum_{a=1}^2 \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, m_{H_a^-}^2) \Gamma_{\tilde{\nu}_j, H_a^+, e_b}^{L*} \Gamma_{\tilde{\nu}_i, H_a^+, e_b}^L \\
& - \frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^3 B_1(p^2, m_{\nu_b}^2, m_{h_a}^2) \Gamma_{\tilde{\nu}_j, h_a, \nu_b}^{L*} \Gamma_{\tilde{\nu}_i, h_a, \nu_b}^L \\
& - \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^2 B_1(p^2, m_{\nu_a}^2, m_{A_b^0}^2) \Gamma_{\tilde{\nu}_j, \nu_a, A_b^0}^{L*} \Gamma_{\tilde{\nu}_i, \nu_a, A_b^0}^L \\
& - \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^4 B_1(p^2, m_{\tilde{\chi}_b^0}^2, m_{\nu_a^i}^2) \Gamma_{\tilde{\nu}_j, \nu_a^i, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{\nu}_i, \nu_a^i, \tilde{\chi}_b^0}^L \\
& - \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^4 B_1(p^2, m_{\tilde{\chi}_b^0}^2, m_{\nu_a^R}^2) \Gamma_{\tilde{\nu}_j, \nu_a^R, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{\nu}_i, \nu_a^R, \tilde{\chi}_b^0}^L \\
& - \sum_{a=1}^6 \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_b^-}^2, m_{\tilde{e}_a}^2) \Gamma_{\tilde{\nu}_j, \tilde{e}_a^*, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{\nu}_i, \tilde{e}_a^*, \tilde{\chi}_b^-}^L - \sum_{b=1}^3 B_1(p^2, m_{\nu_b}^2, m_Z^2) \Gamma_{\tilde{\nu}_j, Z, \nu_b}^{R*} \Gamma_{\tilde{\nu}_i, Z, \nu_b}^R \\
& - 2 \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, m_{W^-}^2) \Gamma_{\tilde{\nu}_j, W^+, e_b}^{R*} \Gamma_{\tilde{\nu}_i, W^+, e_b}^R
\end{aligned} \tag{170}$$

• **Self-Energy for Charginos ( $\tilde{\chi}^-$ )**

$$\Sigma_{i,j}^S(p^2) = + \sum_{a=1}^2 m_{\tilde{\chi}_a^-} \sum_{b=1}^2 B_0(p^2, m_{\tilde{\chi}_a^-}^2, m_{A_b^0}^2) \Gamma_{\tilde{\chi}_j^+, \tilde{\chi}_a^-, A_b^0}^{L*} \Gamma_{\tilde{\chi}_i^+, \tilde{\chi}_a^-, A_b^0}^R$$

$$\begin{aligned}
& + \sum_{a=1}^2 \sum_{b=1}^2 B_0(p^2, m_{\tilde{\chi}_b^-}^2, m_{h_a}^2) \Gamma_{\tilde{\chi}_j^+, h_a, \tilde{\chi}_b^-}^{L*} m_{\tilde{\chi}_b^-} \Gamma_{\tilde{\chi}_i^+, h_a, \tilde{\chi}_b^-}^R \\
& + \sum_{a=1}^2 \sum_{b=1}^4 B_0(p^2, m_{\tilde{\chi}_b^0}^2, m_{H_a^-}^2) \Gamma_{\tilde{\chi}_j^+, H_a^-, \tilde{\chi}_b^0}^{L*} m_{\tilde{\chi}_b^0} \Gamma_{\tilde{\chi}_i^+, H_a^-, \tilde{\chi}_b^0}^R \\
& + \sum_{a=1}^3 \sum_{b=1}^3 B_0(p^2, m_{e_b}^2, m_{\nu_a^i}^2) \Gamma_{\tilde{\chi}_j^+, \nu_a^i, e_b}^{L*} m_{e_b} \Gamma_{\tilde{\chi}_i^+, \nu_a^i, e_b}^R \\
& + \sum_{a=1}^3 \sum_{b=1}^3 B_0(p^2, m_{e_b}^2, m_{\nu_a^R}^2) \Gamma_{\tilde{\chi}_j^+, \nu_a^R, e_b}^{L*} m_{e_b} \Gamma_{\tilde{\chi}_i^+, \nu_a^R, e_b}^R \\
& + 3 \sum_{a=1}^3 m_{u_a} \sum_{b=1}^6 B_0(p^2, m_{u_a}^2, m_{d_b}^2) \Gamma_{\tilde{\chi}_j^+, \bar{u}_a, \bar{d}_b}^{L*} \Gamma_{\tilde{\chi}_i^+, \bar{u}_a, \bar{d}_b}^R \\
& + 3 \sum_{a=1}^6 \sum_{b=1}^3 B_0(p^2, m_{d_b}^2, m_{\bar{u}_a}^2) \Gamma_{\tilde{\chi}_j^+, \bar{u}_a, d_b}^{L*} m_{d_b} \Gamma_{\tilde{\chi}_i^+, \bar{u}_a, d_b}^R \\
& + \sum_{a=1}^6 \sum_{b=1}^3 B_0(p^2, m_{\nu_b}^2, m_{\bar{e}_a}^2) \Gamma_{\tilde{\chi}_j^+, \bar{e}_a, \nu_b}^{L*} m_{\nu_b} \Gamma_{\tilde{\chi}_i^+, \bar{e}_a, \nu_b}^R \\
& - 4 \sum_{b=1}^2 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{\tilde{\chi}_b^-}^2, 0) \right) \Gamma_{\tilde{\chi}_j^+, \gamma, \tilde{\chi}_b^-}^{R*} m_{\tilde{\chi}_b^-} \Gamma_{\tilde{\chi}_i^+, \gamma, \tilde{\chi}_b^-}^L \\
& - 4 \sum_{b=1}^2 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{\tilde{\chi}_b^-}^2, m_Z^2) \right) \Gamma_{\tilde{\chi}_j^+, Z, \tilde{\chi}_b^-}^{R*} m_{\tilde{\chi}_b^-} \Gamma_{\tilde{\chi}_i^+, Z, \tilde{\chi}_b^-}^L \\
& - 4 \sum_{b=1}^4 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{\tilde{\chi}_b^0}^2, m_{W^-}^2) \right) \Gamma_{\tilde{\chi}_j^+, W^-, \tilde{\chi}_b^0}^{R*} m_{\tilde{\chi}_b^0} \Gamma_{\tilde{\chi}_i^+, W^-, \tilde{\chi}_b^0}^L \\
\Sigma_{i,j}^R(p^2) = & -\frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_a^-}^2, m_{A_b^0}^2) \Gamma_{\tilde{\chi}_j^+, \tilde{\chi}_a^-, A_b^0}^{R*} \Gamma_{\tilde{\chi}_i^+, \tilde{\chi}_a^-, A_b^0}^R \\
& - \frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_b^-}^2, m_{h_a}^2) \Gamma_{\tilde{\chi}_j^+, h_a, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{\chi}_i^+, h_a, \tilde{\chi}_b^-}^R \\
& - \frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^4 B_1(p^2, m_{\tilde{\chi}_b^0}^2, m_{H_a^-}^2) \Gamma_{\tilde{\chi}_j^+, H_a^-, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{\chi}_i^+, H_a^-, \tilde{\chi}_b^0}^R \\
& - \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, m_{\nu_a^i}^2) \Gamma_{\tilde{\chi}_j^+, \nu_a^i, e_b}^{R*} \Gamma_{\tilde{\chi}_i^+, \nu_a^i, e_b}^R \\
& - \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, m_{\nu_a^R}^2) \Gamma_{\tilde{\chi}_j^+, \nu_a^R, e_b}^{R*} \Gamma_{\tilde{\chi}_i^+, \nu_a^R, e_b}^R
\end{aligned} \tag{171}$$

$$\begin{aligned}
& - \frac{3}{2} \sum_{a=1}^3 \sum_{b=1}^6 B_1(p^2, m_{u_a}^2, m_{d_b}^2) \Gamma_{\tilde{\chi}_j^+, \bar{u}_a, \tilde{d}_b}^{R*} \Gamma_{\tilde{\chi}_i^+, \bar{u}_a, \tilde{d}_b}^R \\
& - \frac{3}{2} \sum_{a=1}^6 \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_{\bar{u}_a}^2) \Gamma_{\tilde{\chi}_j^+, \bar{u}_a^*, d_b}^{R*} \Gamma_{\tilde{\chi}_i^+, \bar{u}_a^*, d_b}^R \\
& - \frac{1}{2} \sum_{a=1}^6 \sum_{b=1}^3 B_1(p^2, m_{\nu_b}^2, m_{e_a}^2) \Gamma_{\tilde{\chi}_j^+, \bar{e}_a, \nu_b}^{R*} \Gamma_{\tilde{\chi}_i^+, \bar{e}_a, \nu_b}^R - \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_b^-}^2, 0) \Gamma_{\tilde{\chi}_j^+, \gamma, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{\chi}_i^+, \gamma, \tilde{\chi}_b^-}^L \\
& - \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_b^-}^2, m_Z^2) \Gamma_{\tilde{\chi}_j^+, Z, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{\chi}_i^+, Z, \tilde{\chi}_b^-}^L - \sum_{b=1}^4 B_1(p^2, m_{\tilde{\chi}_b^0}^2, m_{W^-}^2) \Gamma_{\tilde{\chi}_j^+, W^-, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{\chi}_i^+, W^-, \tilde{\chi}_b^0}^L
\end{aligned} \tag{172}$$

$$\begin{aligned}
\Sigma_{i,j}^L(p^2) = & - \frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_a^-}^2, m_{A_b^0}^2) \Gamma_{\tilde{\chi}_j^+, \tilde{\chi}_a^-, A_b^0}^{L*} \Gamma_{\tilde{\chi}_i^+, \tilde{\chi}_a^-, A_b^0}^L \\
& - \frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_b^-}^2, m_{h_a}^2) \Gamma_{\tilde{\chi}_j^+, h_a, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{\chi}_i^+, h_a, \tilde{\chi}_b^-}^L \\
& - \frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^4 B_1(p^2, m_{\tilde{\chi}_b^0}^2, m_{H_a^-}^2) \Gamma_{\tilde{\chi}_j^+, H_a^-, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{\chi}_i^+, H_a^-, \tilde{\chi}_b^0}^L \\
& - \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, m_{\nu_a^i}^2) \Gamma_{\tilde{\chi}_j^+, \nu_a^i, e_b}^{L*} \Gamma_{\tilde{\chi}_i^+, \nu_a^i, e_b}^L \\
& - \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, m_{\nu_a^R}^2) \Gamma_{\tilde{\chi}_j^+, \nu_a^R, e_b}^{L*} \Gamma_{\tilde{\chi}_i^+, \nu_a^R, e_b}^L \\
& - \frac{3}{2} \sum_{a=1}^3 \sum_{b=1}^6 B_1(p^2, m_{u_a}^2, m_{d_b}^2) \Gamma_{\tilde{\chi}_j^+, \bar{u}_a, \tilde{d}_b}^{L*} \Gamma_{\tilde{\chi}_i^+, \bar{u}_a, \tilde{d}_b}^L \\
& - \frac{3}{2} \sum_{a=1}^6 \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_{\bar{u}_a}^2) \Gamma_{\tilde{\chi}_j^+, \bar{u}_a^*, d_b}^{L*} \Gamma_{\tilde{\chi}_i^+, \bar{u}_a^*, d_b}^L \\
& - \frac{1}{2} \sum_{a=1}^6 \sum_{b=1}^3 B_1(p^2, m_{\nu_b}^2, m_{\bar{e}_a}^2) \Gamma_{\tilde{\chi}_j^+, \bar{e}_a, \nu_b}^{L*} \Gamma_{\tilde{\chi}_i^+, \bar{e}_a, \nu_b}^L - \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_b^-}^2, 0) \Gamma_{\tilde{\chi}_j^+, \gamma, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{\chi}_i^+, \gamma, \tilde{\chi}_b^-}^R \\
& - \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_b^-}^2, m_Z^2) \Gamma_{\tilde{\chi}_j^+, Z, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{\chi}_i^+, Z, \tilde{\chi}_b^-}^R - \sum_{b=1}^4 B_1(p^2, m_{\tilde{\chi}_b^0}^2, m_{W^-}^2) \Gamma_{\tilde{\chi}_j^+, W^-, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{\chi}_i^+, W^-, \tilde{\chi}_b^0}^R
\end{aligned} \tag{173}$$

• **Self-Energy for Leptons (e)**

$$\Sigma_{i,j}^S(p^2) = + \sum_{a=1}^2 \sum_{b=1}^3 B_0(p^2, m_{e_b}^2, m_{h_a}^2) \Gamma_{\tilde{e}_j, h_a, e_b}^{L*} m_{e_b} \Gamma_{\tilde{e}_i, h_a, e_b}^R$$

$$\begin{aligned}
& + \sum_{a=1}^2 \sum_{b=1}^3 B_0(p^2, m_{\nu_b}^2, m_{H_a^-}^2) \Gamma_{\tilde{e}_j, H_a^-, \nu_b}^{L*} m_{\nu_b} \Gamma_{\tilde{e}_i, H_a^-, \nu_b}^R \\
& + \sum_{a=1}^3 m_{e_a} \sum_{b=1}^2 B_0(p^2, m_{e_a}^2, m_{A_b^0}^2) \Gamma_{\tilde{e}_j, e_a, A_b^0}^{L*} \Gamma_{\tilde{e}_i, e_a, A_b^0}^R \\
& + \sum_{a=1}^3 \sum_{b=1}^2 B_0(p^2, m_{\tilde{\chi}_b^-}^2, m_{\nu_a^i}^2) \Gamma_{\tilde{e}_j, \nu_a^i, \tilde{\chi}_b^-}^{L*} m_{\tilde{\chi}_b^-} \Gamma_{\tilde{e}_i, \nu_a^i, \tilde{\chi}_b^-}^R \\
& + \sum_{a=1}^3 \sum_{b=1}^2 B_0(p^2, m_{\tilde{\chi}_b^-}^2, m_{\nu_a^R}^2) \Gamma_{\tilde{e}_j, \nu_a^R, \tilde{\chi}_b^-}^{L*} m_{\tilde{\chi}_b^-} \Gamma_{\tilde{e}_i, \nu_a^R, \tilde{\chi}_b^-}^R \\
& + \sum_{a=1}^6 \sum_{b=1}^4 B_0(p^2, m_{\tilde{\chi}_b^0}^2, m_{\tilde{e}_a}^2) \Gamma_{\tilde{e}_j, \tilde{e}_a, \tilde{\chi}_b^0}^{L*} m_{\tilde{\chi}_b^0} \Gamma_{\tilde{e}_i, \tilde{e}_a, \tilde{\chi}_b^0}^R \\
& - 4 \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{e_b}^2, 0) \right) \Gamma_{\tilde{e}_j, \gamma, e_b}^{R*} m_{e_b} \Gamma_{\tilde{e}_i, \gamma, e_b}^L \\
& - 4 \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{\nu_b}^2, m_{W^-}^2) \right) \Gamma_{\tilde{e}_j, W^-, \nu_b}^{R*} m_{\nu_b} \Gamma_{\tilde{e}_i, W^-, \nu_b}^L \\
& - 4 \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{e_b}^2, m_Z^2) \right) \Gamma_{\tilde{e}_j, Z, e_b}^{R*} m_{e_b} \Gamma_{\tilde{e}_i, Z, e_b}^L
\end{aligned} \tag{174}$$

$$\begin{aligned}
\Sigma_{i,j}^R(p^2) = & -\frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, m_{h_a}^2) \Gamma_{\tilde{e}_j, h_a, e_b}^{R*} \Gamma_{\tilde{e}_i, h_a, e_b}^R \\
& - \frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^3 B_1(p^2, m_{\nu_b}^2, m_{H_a^-}^2) \Gamma_{\tilde{e}_j, H_a^-, \nu_b}^{R*} \Gamma_{\tilde{e}_i, H_a^-, \nu_b}^R \\
& - \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^2 B_1(p^2, m_{e_a}^2, m_{A_b^0}^2) \Gamma_{\tilde{e}_j, e_a, A_b^0}^{R*} \Gamma_{\tilde{e}_i, e_a, A_b^0}^R \\
& - \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_b^-}^2, m_{\nu_a^i}^2) \Gamma_{\tilde{e}_j, \nu_a^i, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{e}_i, \nu_a^i, \tilde{\chi}_b^-}^R \\
& - \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_b^-}^2, m_{\nu_a^R}^2) \Gamma_{\tilde{e}_j, \nu_a^R, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{e}_i, \nu_a^R, \tilde{\chi}_b^-}^R \\
& - \frac{1}{2} \sum_{a=1}^6 \sum_{b=1}^4 B_1(p^2, m_{\tilde{\chi}_b^0}^2, m_{\tilde{e}_a}^2) \Gamma_{\tilde{e}_j, \tilde{e}_a, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{e}_i, \tilde{e}_a, \tilde{\chi}_b^0}^R \\
& - \frac{1}{2} \sum_{a=1}^6 \sum_{b=1}^4 B_1(p^2, m_{\tilde{\chi}_b^0}^2, m_{\tilde{e}_a}^2) \Gamma_{\tilde{e}_j, \tilde{e}_a, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{e}_i, \tilde{e}_a, \tilde{\chi}_b^0}^R - \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, 0) \Gamma_{\tilde{e}_j, \gamma, e_b}^{L*} \Gamma_{\tilde{e}_i, \gamma, e_b}^L \\
& - \sum_{b=1}^3 B_1(p^2, m_{\nu_b}^2, m_{W^-}^2) \Gamma_{\tilde{e}_j, W^-, \nu_b}^{L*} \Gamma_{\tilde{e}_i, W^-, \nu_b}^L - \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, m_Z^2) \Gamma_{\tilde{e}_j, Z, e_b}^{L*} \Gamma_{\tilde{e}_i, Z, e_b}^L
\end{aligned} \tag{175}$$

$$\begin{aligned}
\Sigma_{i,j}^L(p^2) = & -\frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, m_{h_a}^2) \Gamma_{\tilde{e}_j, h_a, e_b}^{L*} \Gamma_{\tilde{e}_i, h_a, e_b}^L \\
& -\frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^3 B_1(p^2, m_{\nu_b}^2, m_{H_a^-}^2) \Gamma_{\tilde{e}_j, H_a^-, \nu_b}^{L*} \Gamma_{\tilde{e}_i, H_a^-, \nu_b}^L \\
& -\frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^2 B_1(p^2, m_{e_a}^2, m_{A_b^0}^2) \Gamma_{\tilde{e}_j, e_a, A_b^0}^{L*} \Gamma_{\tilde{e}_i, e_a, A_b^0}^L \\
& -\frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_b^-}^2, m_{\nu_a^i}^2) \Gamma_{\tilde{e}_j, \nu_a^i, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{e}_i, \nu_a^i, \tilde{\chi}_b^-}^L \\
& -\frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_b^-}^2, m_{\nu_a^R}^2) \Gamma_{\tilde{e}_j, \nu_a^R, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{e}_i, \nu_a^R, \tilde{\chi}_b^-}^L \\
& -\frac{1}{2} \sum_{a=1}^6 \sum_{b=1}^4 B_1(p^2, m_{\tilde{\chi}_b^0}^2, m_{\tilde{e}_a}^2) \Gamma_{\tilde{e}_j, \tilde{e}_a, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{e}_i, \tilde{e}_a, \tilde{\chi}_b^0}^L - \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, 0) \Gamma_{\tilde{e}_j, \gamma, e_b}^{R*} \Gamma_{\tilde{e}_i, \gamma, e_b}^R \\
& -\sum_{b=1}^3 B_1(p^2, m_{\nu_b}^2, m_{W^-}^2) \Gamma_{\tilde{e}_j, W^-, \nu_b}^{R*} \Gamma_{\tilde{e}_i, W^-, \nu_b}^R - \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, m_Z^2) \Gamma_{\tilde{e}_j, Z, e_b}^{R*} \Gamma_{\tilde{e}_i, Z, e_b}^R \quad (176)
\end{aligned}$$

- Self-Energy for Down-Quarks (d)

$$\begin{aligned}
\Sigma_{i,j}^S(p^2) = & + \sum_{a=1}^2 \sum_{b=1}^3 B_0(p^2, m_{d_b}^2, m_{h_a}^2) \Gamma_{\tilde{d}_j, h_a, d_b}^{L*} m_{d_b} \Gamma_{\tilde{d}_i, h_a, d_b}^R \\
& + \sum_{a=1}^2 \sum_{b=1}^3 B_0(p^2, m_{u_b}^2, m_{H_a^-}^2) \Gamma_{\tilde{d}_j, H_a^-, u_b}^{L*} m_{u_b} \Gamma_{\tilde{d}_i, H_a^-, u_b}^R \\
& + \sum_{a=1}^3 m_{d_a} \sum_{b=1}^2 B_0(p^2, m_{d_a}^2, m_{A_b^0}^2) \Gamma_{\tilde{d}_j, d_a, A_b^0}^{L*} \Gamma_{\tilde{d}_i, d_a, A_b^0}^R \\
& + \sum_{a=1}^6 \sum_{b=1}^2 B_0(p^2, m_{\tilde{\chi}_b^-}^2, m_{\tilde{u}_a}^2) \Gamma_{\tilde{d}_j, \tilde{u}_a, \tilde{\chi}_b^-}^{L*} m_{\tilde{\chi}_b^-} \Gamma_{\tilde{d}_i, \tilde{u}_a, \tilde{\chi}_b^-}^R \\
& + \sum_{a=1}^6 \sum_{b=1}^4 B_0(p^2, m_{\tilde{\chi}_b^0}^2, m_{\tilde{d}_a}^2) \Gamma_{\tilde{d}_j, \tilde{d}_a, \tilde{\chi}_b^0}^{L*} m_{\tilde{\chi}_b^0} \Gamma_{\tilde{d}_i, \tilde{d}_a, \tilde{\chi}_b^0}^R \\
& + \frac{4}{3} m_{\tilde{g}} \sum_{a=1}^6 B_0(p^2, m_{\tilde{g}}^2, m_{\tilde{d}_a}^2) \Gamma_{\tilde{d}_j, \tilde{d}_a, \tilde{g}_1}^{L*} \Gamma_{\tilde{d}_i, \tilde{d}_a, \tilde{g}_1}^R - \frac{16}{3} \sum_{b=1}^3 \left( -\frac{1}{2} rMS + B_0(p^2, m_{d_b}^2, 0) \right) \Gamma_{\tilde{d}_j, g, d_b}^{R*} m_{d_b} \Gamma_{\tilde{d}_i, g, d_b}^L \\
& - 4 \sum_{b=1}^3 \left( -\frac{1}{2} rMS + B_0(p^2, m_{d_b}^2, 0) \right) \Gamma_{\tilde{d}_j, \gamma, d_b}^{R*} m_{d_b} \Gamma_{\tilde{d}_i, \gamma, d_b}^L
\end{aligned}$$

$$\begin{aligned}
& -4 \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{u_b}^2, m_{W^-}^2) \right) \Gamma_{\tilde{d}_j, W^-, u_b}^{R*} m_{u_b} \Gamma_{\tilde{d}_i, W^-, u_b}^L \\
& -4 \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{d_b}^2, m_Z^2) \right) \Gamma_{\tilde{d}_j, Z, d_b}^{R*} m_{d_b} \Gamma_{\tilde{d}_i, Z, d_b}^L
\end{aligned} \tag{177}$$

$$\begin{aligned}
\Sigma_{i,j}^R(p^2) = & -\frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_{h_a}^2) \Gamma_{\tilde{d}_j, h_a, d_b}^{R*} \Gamma_{\tilde{d}_i, h_a, d_b}^R \\
& -\frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_{H_a^-}^2) \Gamma_{\tilde{d}_j, H_a^-, u_b}^{R*} \Gamma_{\tilde{d}_i, H_a^-, u_b}^R \\
& -\frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^2 B_1(p^2, m_{d_a}^2, m_{A_b^0}^2) \Gamma_{\tilde{d}_j, d_a, A_b^0}^{R*} \Gamma_{\tilde{d}_i, d_a, A_b^0}^R \\
& -\frac{1}{2} \sum_{a=1}^6 \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_b^-}^2, m_{\tilde{u}_a}^2) \Gamma_{\tilde{d}_j, \tilde{u}_a, \tilde{\chi}_b^-}^{R*} \Gamma_{\tilde{d}_i, \tilde{u}_a, \tilde{\chi}_b^-}^R \\
& -\frac{1}{2} \sum_{a=1}^6 \sum_{b=1}^4 B_1(p^2, m_{\tilde{\chi}_b^0}^2, m_{\tilde{d}_a}^2) \Gamma_{\tilde{d}_j, \tilde{d}_a, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{d}_i, \tilde{d}_a, \tilde{\chi}_b^0}^R \\
& -\frac{2}{3} \sum_{a=1}^6 B_1(p^2, m_{\tilde{g}}^2, m_{\tilde{d}_a}^2) \Gamma_{\tilde{d}_j, \tilde{d}_a, \tilde{g}_1}^{R*} \Gamma_{\tilde{d}_i, \tilde{d}_a, \tilde{g}_1}^R - \frac{4}{3} \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, 0) \Gamma_{\tilde{d}_j, g, d_b}^{L*} \Gamma_{\tilde{d}_i, g, d_b}^L \\
& -\sum_{b=1}^3 B_1(p^2, m_{d_b}^2, 0) \Gamma_{\tilde{d}_j, \gamma, d_b}^{L*} \Gamma_{\tilde{d}_i, \gamma, d_b}^L - \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_{W^-}^2) \Gamma_{\tilde{d}_j, W^-, u_b}^{L*} \Gamma_{\tilde{d}_i, W^-, u_b}^L \\
& -\sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_Z^2) \Gamma_{\tilde{d}_j, Z, d_b}^{L*} \Gamma_{\tilde{d}_i, Z, d_b}^L
\end{aligned} \tag{178}$$

$$\begin{aligned}
\Sigma_{i,j}^L(p^2) = & -\frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_{h_a}^2) \Gamma_{\tilde{d}_j, h_a, d_b}^{L*} \Gamma_{\tilde{d}_i, h_a, d_b}^L \\
& -\frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_{H_a^-}^2) \Gamma_{\tilde{d}_j, H_a^-, u_b}^{L*} \Gamma_{\tilde{d}_i, H_a^-, u_b}^L \\
& -\frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^2 B_1(p^2, m_{d_a}^2, m_{A_b^0}^2) \Gamma_{\tilde{d}_j, d_a, A_b^0}^{L*} \Gamma_{\tilde{d}_i, d_a, A_b^0}^L \\
& -\frac{1}{2} \sum_{a=1}^6 \sum_{b=1}^2 B_1(p^2, m_{\tilde{\chi}_b^-}^2, m_{\tilde{u}_a}^2) \Gamma_{\tilde{d}_j, \tilde{u}_a, \tilde{\chi}_b^-}^{L*} \Gamma_{\tilde{d}_i, \tilde{u}_a, \tilde{\chi}_b^-}^L \\
& -\frac{1}{2} \sum_{a=1}^6 \sum_{b=1}^4 B_1(p^2, m_{\tilde{\chi}_b^0}^2, m_{\tilde{d}_a}^2) \Gamma_{\tilde{d}_j, \tilde{d}_a, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{d}_i, \tilde{d}_a, \tilde{\chi}_b^0}^L
\end{aligned}$$

$$\begin{aligned}
& - \frac{2}{3} \sum_{a=1}^6 B_1(p^2, m_g^2, m_{d_a}^2) \Gamma_{\tilde{d}_j, \tilde{d}_a, \tilde{g}_1}^{L*} \Gamma_{\tilde{d}_i, \tilde{d}_a, \tilde{g}_1}^L - \frac{4}{3} \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, 0) \Gamma_{\tilde{d}_j, g, d_b}^{R*} \Gamma_{\tilde{d}_i, g, d_b}^R \\
& - \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, 0) \Gamma_{\tilde{d}_j, \gamma, d_b}^{R*} \Gamma_{\tilde{d}_i, \gamma, d_b}^R - \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_{W^-}^2) \Gamma_{\tilde{d}_j, W^-, u_b}^{R*} \Gamma_{\tilde{d}_i, W^-, u_b}^R \\
& - \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_Z^2) \Gamma_{\tilde{d}_j, Z, d_b}^{R*} \Gamma_{\tilde{d}_i, Z, d_b}^R
\end{aligned} \tag{179}$$

• **Self-Energy for Up-Quarks ( $u$ )**

$$\begin{aligned}
\Sigma_{i,j}^S(p^2) = & + \sum_{a=1}^2 \sum_{b=1}^3 B_0(p^2, m_{d_b}^2, m_{H_a^-}^2) \Gamma_{\tilde{u}_j, H_a^+, d_b}^{L*} m_{d_b} \Gamma_{\tilde{u}_i, H_a^+, d_b}^R \\
& + \sum_{a=1}^2 \sum_{b=1}^3 B_0(p^2, m_{u_b}^2, m_{h_a}^2) \Gamma_{\tilde{u}_j, h_a, u_b}^{L*} m_{u_b} \Gamma_{\tilde{u}_i, h_a, u_b}^R \\
& + \sum_{a=1}^2 m_{\tilde{\chi}_a^-} \sum_{b=1}^6 B_0(p^2, m_{\tilde{\chi}_a^-}^2, m_{\tilde{d}_b}^2) \Gamma_{\tilde{u}_j, \tilde{\chi}_a^+, \tilde{d}_b}^{L*} \Gamma_{\tilde{u}_i, \tilde{\chi}_a^+, \tilde{d}_b}^R \\
& + \sum_{a=1}^3 m_{u_a} \sum_{b=1}^2 B_0(p^2, m_{u_a}^2, m_{A_b^0}^2) \Gamma_{\tilde{u}_j, u_a, A_b^0}^{L*} \Gamma_{\tilde{u}_i, u_a, A_b^0}^R \\
& + \sum_{a=1}^6 \sum_{b=1}^4 B_0(p^2, m_{\tilde{\chi}_b^0}^2, m_{\tilde{u}_a}^2) \Gamma_{\tilde{u}_j, \tilde{u}_a, \tilde{\chi}_b^0}^{L*} m_{\tilde{\chi}_b^0} \Gamma_{\tilde{u}_i, \tilde{u}_a, \tilde{\chi}_b^0}^R \\
& + \frac{4}{3} m_g \sum_{a=1}^6 B_0(p^2, m_g^2, m_{\tilde{u}_a}^2) \Gamma_{\tilde{u}_j, \tilde{u}_a, \tilde{g}_1}^{L*} \Gamma_{\tilde{u}_i, \tilde{u}_a, \tilde{g}_1}^R - \frac{16}{3} \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{u_b}^2, 0) \right) \Gamma_{\tilde{u}_j, g, u_b}^{R*} m_{u_b} \Gamma_{\tilde{u}_i, g, u_b}^L \\
& - 4 \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{u_b}^2, 0) \right) \Gamma_{\tilde{u}_j, \gamma, u_b}^{R*} m_{u_b} \Gamma_{\tilde{u}_i, \gamma, u_b}^L - 4 \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{u_b}^2, m_Z^2) \right) \Gamma_{\tilde{u}_j, Z, u_b}^{R*} m_{u_b} \Gamma_{\tilde{u}_i, Z, u_b}^L \\
& - 4 \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{d_b}^2, m_{W^-}^2) \right) \Gamma_{\tilde{u}_j, W^+, d_b}^{R*} m_{d_b} \Gamma_{\tilde{u}_i, W^+, d_b}^L
\end{aligned} \tag{180}$$

$$\begin{aligned}
\Sigma_{i,j}^R(p^2) = & - \frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_{H_a^-}^2) \Gamma_{\tilde{u}_j, H_a^+, d_b}^{R*} \Gamma_{\tilde{u}_i, H_a^+, d_b}^R \\
& - \frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_{h_a}^2) \Gamma_{\tilde{u}_j, h_a, u_b}^{R*} \Gamma_{\tilde{u}_i, h_a, u_b}^R \\
& - \frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^6 B_1(p^2, m_{\tilde{\chi}_a^-}^2, m_{\tilde{d}_b}^2) \Gamma_{\tilde{u}_j, \tilde{\chi}_a^+, \tilde{d}_b}^{R*} \Gamma_{\tilde{u}_i, \tilde{\chi}_a^+, \tilde{d}_b}^R
\end{aligned}$$

$$\begin{aligned}
& - \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^2 B_1(p^2, m_{u_a}^2, m_{A_b^0}^2) \Gamma_{\tilde{u}_j, u_a, A_b^0}^{R*} \Gamma_{\tilde{u}_i, u_a, A_b^0}^R \\
& - \frac{1}{2} \sum_{a=1}^6 \sum_{b=1}^4 B_1(p^2, m_{\tilde{\chi}_b^0}^2, m_{\tilde{u}_a}^2) \Gamma_{\tilde{u}_j, \tilde{u}_a, \tilde{\chi}_b^0}^{R*} \Gamma_{\tilde{u}_i, \tilde{u}_a, \tilde{\chi}_b^0}^R \\
& - \frac{2}{3} \sum_{a=1}^6 B_1(p^2, m_{\tilde{g}}^2, m_{\tilde{u}_a}^2) \Gamma_{\tilde{u}_j, \tilde{u}_a, \tilde{g}_1}^{R*} \Gamma_{\tilde{u}_i, \tilde{u}_a, \tilde{g}_1}^R - \frac{4}{3} \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, 0) \Gamma_{\tilde{u}_j, g, u_b}^{L*} \Gamma_{\tilde{u}_i, g, u_b}^L \\
& - \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, 0) \Gamma_{\tilde{u}_j, \gamma, u_b}^{L*} \Gamma_{\tilde{u}_i, \gamma, u_b}^L - \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_Z^2) \Gamma_{\tilde{u}_j, Z, u_b}^{L*} \Gamma_{\tilde{u}_i, Z, u_b}^L \\
& - \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_{W^-}^2) \Gamma_{\tilde{u}_j, W^+, d_b}^{L*} \Gamma_{\tilde{u}_i, W^+, d_b}^L
\end{aligned} \tag{181}$$

$$\begin{aligned}
\Sigma_{i,j}^L(p^2) = & - \frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_{H_a^-}^2) \Gamma_{\tilde{u}_j, H_a^-, d_b}^{L*} \Gamma_{\tilde{u}_i, H_a^-, d_b}^L \\
& - \frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_{h_a}^2) \Gamma_{\tilde{u}_j, h_a, u_b}^{L*} \Gamma_{\tilde{u}_i, h_a, u_b}^L \\
& - \frac{1}{2} \sum_{a=1}^2 \sum_{b=1}^6 B_1(p^2, m_{\tilde{\chi}_a^-}^2, m_{d_b}^2) \Gamma_{\tilde{u}_j, \tilde{\chi}_a^-, d_b}^{L*} \Gamma_{\tilde{u}_i, \tilde{\chi}_a^-, d_b}^L \\
& - \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^2 B_1(p^2, m_{u_a}^2, m_{A_b^0}^2) \Gamma_{\tilde{u}_j, u_a, A_b^0}^{L*} \Gamma_{\tilde{u}_i, u_a, A_b^0}^L \\
& - \frac{1}{2} \sum_{a=1}^6 \sum_{b=1}^4 B_1(p^2, m_{\tilde{\chi}_b^0}^2, m_{\tilde{u}_a}^2) \Gamma_{\tilde{u}_j, \tilde{u}_a, \tilde{\chi}_b^0}^{L*} \Gamma_{\tilde{u}_i, \tilde{u}_a, \tilde{\chi}_b^0}^L \\
& - \frac{2}{3} \sum_{a=1}^6 B_1(p^2, m_{\tilde{g}}^2, m_{\tilde{u}_a}^2) \Gamma_{\tilde{u}_j, \tilde{u}_a, \tilde{g}_1}^{L*} \Gamma_{\tilde{u}_i, \tilde{u}_a, \tilde{g}_1}^L - \frac{4}{3} \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, 0) \Gamma_{\tilde{u}_j, g, u_b}^{R*} \Gamma_{\tilde{u}_i, g, u_b}^R \\
& - \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, 0) \Gamma_{\tilde{u}_j, \gamma, u_b}^{R*} \Gamma_{\tilde{u}_i, \gamma, u_b}^R - \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_Z^2) \Gamma_{\tilde{u}_j, Z, u_b}^{R*} \Gamma_{\tilde{u}_i, Z, u_b}^R \\
& - \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_{W^-}^2) \Gamma_{\tilde{u}_j, W^+, d_b}^{R*} \Gamma_{\tilde{u}_i, W^+, d_b}^R
\end{aligned} \tag{182}$$

• **Self-Energy for Gluino ( $\tilde{g}$ )**

$$\Sigma^S(p^2) = + \sum_{a=1}^6 \sum_{b=1}^3 B_0(p^2, m_{d_b}^2, m_{\tilde{d}_a}^2) \Gamma_{\tilde{g}_j, \tilde{d}_a^*, d_b}^{L*} m_{d_b} \Gamma_{\tilde{g}_i, \tilde{d}_a^*, d_b}^R$$

$$+ \sum_{a=1}^6 \sum_{b=1}^3 B_0(p^2, m_{u_b}^2, m_{\tilde{u}_a}^2) \Gamma_{\tilde{g}_j, \tilde{u}_a^*, u_b}^{L*} m_{u_b} \Gamma_{\tilde{g}_i, \tilde{u}_a^*, u_b}^R - 12 \left( -\frac{1}{2} rMS + B_0(p^2, m_{\tilde{g}}^2, 0) \right) \Gamma_{\tilde{g}_j, g, \tilde{g}_1}^{R*} m_{\tilde{g}} \Gamma_{\tilde{g}_i, g, \tilde{g}_1}^L \\ (183)$$

$$\Sigma^R(p^2) = -\frac{1}{2} \sum_{a=1}^6 \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_{\tilde{d}_a}^2) \Gamma_{\tilde{g}_j, \tilde{d}_a^*, d_b}^{R*} \Gamma_{\tilde{g}_i, \tilde{d}_a^*, d_b}^R \\ - \frac{1}{2} \sum_{a=1}^6 \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_{\tilde{u}_a}^2) \Gamma_{\tilde{g}_j, \tilde{u}_a^*, u_b}^{R*} \Gamma_{\tilde{g}_i, \tilde{u}_a^*, u_b}^R - 3B_1(p^2, m_{\tilde{g}}^2, 0) \Gamma_{\tilde{g}_j, g, \tilde{g}_1}^{L*} \Gamma_{\tilde{g}_i, g, \tilde{g}_1}^L \\ (184)$$

$$\Sigma^L(p^2) = -\frac{1}{2} \sum_{a=1}^6 \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_{\tilde{d}_a}^2) \Gamma_{\tilde{g}_j, \tilde{d}_a^*, d_b}^{L*} \Gamma_{\tilde{g}_i, \tilde{d}_a^*, d_b}^L \\ - \frac{1}{2} \sum_{a=1}^6 \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_{\tilde{u}_a}^2) \Gamma_{\tilde{g}_j, \tilde{u}_a^*, u_b}^{L*} \Gamma_{\tilde{g}_i, \tilde{u}_a^*, u_b}^L - 3B_1(p^2, m_{\tilde{g}}^2, 0) \Gamma_{\tilde{g}_j, g, \tilde{g}_1}^{R*} \Gamma_{\tilde{g}_i, g, \tilde{g}_1}^R \\ (185)$$

• **Self-Energy for Z-Boson (Z)**

$$\Pi(p^2) = +|\Gamma_{Z, \eta^-, \eta^-}|^2 B_{00}(p^2, m_{\eta^-}^2, m_{\eta^-}^2) + |\Gamma_{Z, \eta^+, \eta^+}|^2 B_{00}(p^2, m_{\eta^+}^2, m_{\eta^+}^2) \\ - |\Gamma_{Z, W^+, W^-}|^2 \left( 10B_{00}(p^2, m_{W^-}^2, m_{W^-}^2) + 2A_0(m_{W^-}^2) - 2rMS \left( 2m_{W^-}^2 - \frac{1}{3} p^2 \right) + B_0(p^2, m_{W^-}^2, m_{W^-}^2) \left( 2m_{W^-}^2 + 4p^2 \right) \right) \\ + \frac{1}{2} \sum_{a=1}^2 A_0(m_{A_a^0}^2) \Gamma_{Z, Z, A_a^0, A_a^0} + \sum_{a=1}^2 A_0(m_{H_a^+}^2) \Gamma_{Z, Z, H_a^+, H_a^-} + \frac{1}{2} \sum_{a=1}^2 A_0(m_{h_a}^2) \Gamma_{Z, Z, h_a, h_a} \\ - 4 \sum_{a=1}^2 \sum_{b=1}^2 |\Gamma_{Z, h_a, A_b^0}|^2 B_{00}(p^2, m_{A_b^0}^2, m_{h_a}^2) - 4 \sum_{a=1}^2 \sum_{b=1}^2 |\Gamma_{Z, H_a^+, H_b^-}|^2 B_{00}(p^2, m_{H_a^+}^2, m_{H_b^-}^2) \\ + \sum_{a=1}^2 \sum_{b=1}^2 \left[ (|\Gamma_{Z, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^L|^2 + |\Gamma_{Z, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^R|^2) H_0(p^2, m_{\tilde{\chi}_a^+}^2, m_{\tilde{\chi}_b^-}^2) \right. \\ \left. + 4B_0(p^2, m_{\tilde{\chi}_a^-}^2, m_{\tilde{\chi}_b^-}^2) m_{\tilde{\chi}_a^-} m_{\tilde{\chi}_b^-} \Re(\Gamma_{Z, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^{L*} \Gamma_{Z, \tilde{\chi}_a^+, \tilde{\chi}_b^-}^R) \right] \\ + \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^i}^2) \Gamma_{Z, Z, \nu_a^i, \nu_a^i} + \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^R}^2) \Gamma_{Z, Z, \nu_a^R, \nu_a^R} \\ - 4 \sum_{a=1}^3 \sum_{b=1}^3 |\Gamma_{Z, \nu_a^R, \nu_b^i}|^2 B_{00}(p^2, m_{\nu_b^i}^2, m_{\nu_a^R}^2) \\ + 3 \sum_{a=1}^3 \sum_{b=1}^3 \left[ (|\Gamma_{Z, \bar{d}_a, d_b}^L|^2 + |\Gamma_{Z, \bar{d}_a, d_b}^R|^2) H_0(p^2, m_{d_a}^2, m_{d_b}^2) \right. \\ \left. + 4B_0(p^2, m_{d_a}^2, m_{d_b}^2) m_{d_a} m_{d_b} \Re(\Gamma_{Z, \bar{d}_a, d_b}^{L*} \Gamma_{Z, \bar{d}_a, d_b}^R) \right] \\ + \sum_{a=1}^3 \sum_{b=1}^3 \left[ (|\Gamma_{Z, \bar{e}_a, e_b}^L|^2 + |\Gamma_{Z, \bar{e}_a, e_b}^R|^2) H_0(p^2, m_{e_a}^2, m_{e_b}^2) \right]$$

$$\begin{aligned}
& + 4B_0(p^2, m_{e_a}^2, m_{e_b}^2) m_{e_a} m_{e_b} \Re(\Gamma_{Z, \bar{e}_a, e_b}^{L*} \Gamma_{Z, \bar{e}_a, e_b}^R) \\
& + 3 \sum_{a=1}^3 \sum_{b=1}^3 \left[ \left( |\Gamma_{Z, \bar{u}_a, u_b}^L|^2 + |\Gamma_{Z, \bar{u}_a, u_b}^R|^2 \right) H_0(p^2, m_{u_a}^2, m_{u_b}^2) \right. \\
& + 4B_0(p^2, m_{u_a}^2, m_{u_b}^2) m_{u_a} m_{u_b} \Re(\Gamma_{Z, \bar{u}_a, u_b}^{L*} \Gamma_{Z, \bar{u}_a, u_b}^R) \\
& + \frac{1}{2} \sum_{a=1}^3 \sum_{b=1}^3 \left[ \left( |\Gamma_{Z, \nu_a, \nu_b}^L|^2 + |\Gamma_{Z, \nu_a, \nu_b}^R|^2 \right) H_0(p^2, m_{\nu_a}^2, m_{\nu_b}^2) \right. \\
& + 4B_0(p^2, m_{\nu_a}^2, m_{\nu_b}^2) m_{\nu_a} m_{\nu_b} \Re(\Gamma_{Z, \nu_a, \nu_b}^{L*} \Gamma_{Z, \nu_a, \nu_b}^R) \\
& + \frac{1}{2} \sum_{a=1}^4 \sum_{b=1}^4 \left[ \left( |\Gamma_{Z, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^L|^2 + |\Gamma_{Z, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^R|^2 \right) H_0(p^2, m_{\tilde{\chi}_a^0}^2, m_{\tilde{\chi}_b^0}^2) \right. \\
& + 4B_0(p^2, m_{\tilde{\chi}_a^0}^2, m_{\tilde{\chi}_b^0}^2) m_{\tilde{\chi}_a^0} m_{\tilde{\chi}_b^0} \Re(\Gamma_{Z, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^{L*} \Gamma_{Z, \tilde{\chi}_a^0, \tilde{\chi}_b^0}^R) \\
& + 3 \sum_{a=1}^6 A_0(m_{\tilde{d}_a}^2) \Gamma_{Z, Z, \tilde{d}_a^*, \tilde{d}_a} + \sum_{a=1}^6 A_0(m_{\tilde{e}_a}^2) \Gamma_{Z, Z, \tilde{e}_a^*, \tilde{e}_a} + 3 \sum_{a=1}^6 A_0(m_{\tilde{u}_a}^2) \Gamma_{Z, Z, \tilde{u}_a^*, \tilde{u}_a} \\
& - 12 \sum_{a=1}^6 \sum_{b=1}^6 |\Gamma_{Z, \tilde{d}_a^*, \tilde{d}_b}|^2 B_{00}(p^2, m_{\tilde{d}_a}^2, m_{\tilde{d}_b}^2) - 4 \sum_{a=1}^6 \sum_{b=1}^6 |\Gamma_{Z, \tilde{e}_a^*, \tilde{e}_b}|^2 B_{00}(p^2, m_{\tilde{e}_a}^2, m_{\tilde{e}_b}^2) \\
& - 12 \sum_{a=1}^6 \sum_{b=1}^6 |\Gamma_{Z, \tilde{u}_a^*, \tilde{u}_b}|^2 B_{00}(p^2, m_{\tilde{u}_a}^2, m_{\tilde{u}_b}^2) + 2 \sum_{b=1}^2 |\Gamma_{Z, W^+, H_b^-}|^2 B_0(p^2, m_{W^-}^2, m_{H_b^-}^2) \\
& + \sum_{b=1}^2 |\Gamma_{Z, Z, h_b}|^2 B_0(p^2, m_Z^2, m_{h_b}^2) + 2rMSm_{W^-}^2 \Gamma_{Z, Z, W^+, W^-}^1 - A_0(m_{W^-}^2) (4\Gamma_{Z, Z, W^+, W^-}^1 + \Gamma_{Z, Z, W^+, W^-}^2 + \Gamma_{Z, Z, W^+, W^-}^3)
\end{aligned} \tag{186}$$

• Self-Energy for W-Boson ( $W^-$ )

$$\begin{aligned}
\Pi(p^2) = & -12 \sum_{a=1}^6 \sum_{b=1}^6 |\Gamma_{W^+, \tilde{u}_a^*, \tilde{d}_b}|^2 B_{00}(p^2, m_{\tilde{d}_b}^2, m_{\tilde{u}_a}^2) + 2rMSm_{W^-}^2 \Gamma_{W^-, W^+, W^-}^1 + 3 \sum_{a=1}^3 \sum_{b=1}^3 \left[ \left( |\Gamma_{W^+, \bar{u}_a, d_b}^L|^2 + |\Gamma_{W^+, \bar{u}_a, d_b}^R|^2 \right) H_0(p^2, m_{\bar{u}_a}^2, m_{d_b}^2) \right. \\
& + 4B_0(p^2, m_{u_a}^2, m_{d_b}^2) m_{d_b} m_{u_a} \Re(\Gamma_{W^+, \bar{u}_a, d_b}^{L*} \Gamma_{W^+, \bar{u}_a, d_b}^R) \left. \right] + 3 \sum_{a=1}^6 A_0(m_{\tilde{d}_a}^2) \Gamma_{W^-, W^+, \tilde{d}_a^*, \tilde{d}_a} + 3 \sum_{a=1}^6 A_0(m_{\tilde{u}_a}^2) \Gamma_{W^-, W^+, \tilde{u}_a^*, \tilde{u}_a} \\
& + 4B_0(p^2, m_{\nu_a}^2, m_{e_b}^2) m_{e_b} m_{\nu_a} \Re(\Gamma_{W^+, \nu_a, e_b}^{L*} \Gamma_{W^+, \nu_a, e_b}^R) \left. \right] + \sum_{a=1}^4 \sum_{b=1}^2 \left[ \left( |\Gamma_{W^+, \tilde{\chi}_a^0, \tilde{\chi}_b^-}^L|^2 + |\Gamma_{W^+, \tilde{\chi}_a^0, \tilde{\chi}_b^-}^R|^2 \right) H_0(p^2, m_{\tilde{\chi}_a^0}^2, m_{\tilde{\chi}_b^-}^2) \right. \\
& + 4B_0(p^2, m_{\tilde{\chi}_a^0}^2, m_{\tilde{\chi}_b^-}^2) m_{\tilde{\chi}_b^-} m_{\tilde{\chi}_a^0} \Re(\Gamma_{W^+, \tilde{\chi}_a^0, \tilde{\chi}_b^-}^{L*} \Gamma_{W^+, \tilde{\chi}_a^0, \tilde{\chi}_b^-}^R) \left. \right] + \sum_{a=1}^6 A_0(m_{\tilde{e}_a}^2) \Gamma_{W^-, W^+, \tilde{e}_a^*, \tilde{e}_a} + \sum_{b=1}^2 |\Gamma_{W^+, \gamma, H_b^-}|^2 B_0(p^2, 0, m_{H_b^-}^2)
\end{aligned} \tag{187}$$

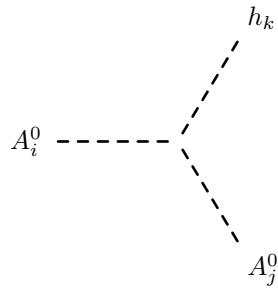
## 8.2 Tadpoles

$$\begin{aligned}
\delta t_h^{(1)} = & + A_0(m_{\eta^-}^2) \Gamma_{\check{h}_i, \eta^-, \eta^-} + A_0(m_{\eta^+}^2) \Gamma_{\check{h}_i, \bar{\eta}^+, \eta^+} + A_0(m_{\eta^Z}^2) \Gamma_{\check{h}_i, \eta^Z, \eta^Z} \\
& + 4\Gamma_{\check{h}_i, W^+, W^-} \left( -\frac{1}{2} \text{rMS} m_{W^-}^2 + A_0(m_{W^-}^2) \right) + 2\Gamma_{\check{h}_i, Z, Z} \left( -\frac{1}{2} \text{rMS} m_Z^2 + A_0(m_Z^2) \right) - \frac{1}{2} \sum_{a=1}^2 A_0(m_{A_a^0}^2) \Gamma_{\check{h}_i, A_a^0, A_a^0} \\
& - \sum_{a=1}^2 A_0(m_{H_a^-}^2) \Gamma_{\check{h}_i, H_a^+, H_a^-} - \frac{1}{2} \sum_{a=1}^2 A_0(m_{h_a}^2) \Gamma_{\check{h}_i, h_a, h_a} \\
& + 2 \sum_{a=1}^2 A_0(m_{\tilde{\chi}_a^-}^2) m_{\tilde{\chi}_a^-} \left( \Gamma_{\check{h}_i, \tilde{\chi}_a^+, \tilde{\chi}_a^-}^L + \Gamma_{\check{h}_i, \tilde{\chi}_a^+, \tilde{\chi}_a^-}^R \right) - \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^i}^2) \Gamma_{\check{h}_i, \nu_a^i, \nu_a^i} \\
& - \frac{1}{2} \sum_{a=1}^3 A_0(m_{\nu_a^R}^2) \Gamma_{\check{h}_i, \nu_a^R, \nu_a^R} + 6 \sum_{a=1}^3 A_0(m_{d_a}^2) m_{d_a} \left( \Gamma_{\check{h}_i, \bar{d}_a, d_a}^L + \Gamma_{\check{h}_i, \bar{d}_a, d_a}^R \right) \\
& + 2 \sum_{a=1}^3 A_0(m_{e_a}^2) m_{e_a} \left( \Gamma_{\check{h}_i, \bar{e}_a, e_a}^L + \Gamma_{\check{h}_i, \bar{e}_a, e_a}^R \right) \\
& + 6 \sum_{a=1}^3 A_0(m_{u_a}^2) m_{u_a} \left( \Gamma_{\check{h}_i, \bar{u}_a, u_a}^L + \Gamma_{\check{h}_i, \bar{u}_a, u_a}^R \right) + \sum_{a=1}^3 A_0(m_{\nu_a}^2) m_{\nu_a} \left( \Gamma_{\check{h}_i, \nu_a, \nu_a}^L + \Gamma_{\check{h}_i, \nu_a, \nu_a}^R \right) \\
& + \sum_{a=1}^4 A_0(m_{\tilde{\chi}_a^0}^2) m_{\tilde{\chi}_a^0} \left( \Gamma_{\check{h}_i, \tilde{\chi}_a^0, \tilde{\chi}_a^0}^L + \Gamma_{\check{h}_i, \tilde{\chi}_a^0, \tilde{\chi}_a^0}^R \right) - 3 \sum_{a=1}^6 A_0(m_{\tilde{d}_a}^2) \Gamma_{\check{h}_i, \tilde{d}_a^*, \tilde{d}_a} \\
& - \sum_{a=1}^6 A_0(m_{\tilde{e}_a}^2) \Gamma_{\check{h}_i, \tilde{e}_a^*, \tilde{e}_a} - 3 \sum_{a=1}^6 A_0(m_{\tilde{u}_a}^2) \Gamma_{\check{h}_i, \tilde{u}_a^*, \tilde{u}_a} \tag{188}
\end{aligned}$$

$$\delta t_{\nu^R}^{(1)} = 0 \tag{189}$$

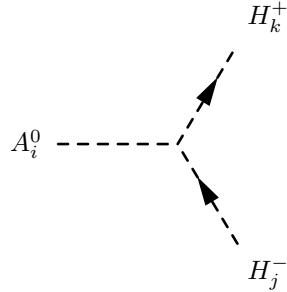
## 9 Interactions for eigenstates 'EWSB'

### 9.1 Three Scalar-Interaction



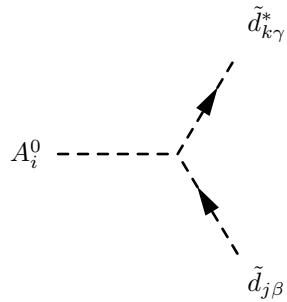
$$-\frac{i}{4} \left( g_1^2 + g_2^2 \right) \left( Z_{i1}^A Z_{j1}^A - Z_{i2}^A Z_{j2}^A \right) \left( v_d Z_{k1}^H - v_u Z_{k2}^H \right) \quad (190)$$


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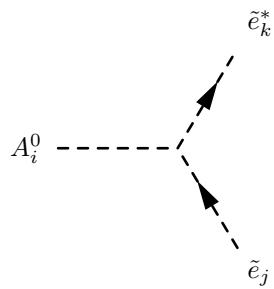
$$\frac{1}{4} g_2^2 \left( v_d Z_{i2}^A + v_u Z_{i1}^A \right) \left( -Z_{j1}^+ Z_{k2}^+ + Z_{j2}^+ Z_{k1}^+ \right) \quad (191)$$


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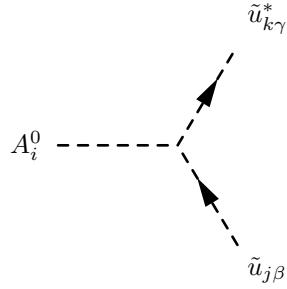


$$\begin{aligned} & \frac{1}{\sqrt{2}} \delta_{\beta\gamma} \left( \sum_{b=1}^3 Z_{jb}^{D,*} \sum_{a=1}^3 Z_{k3+a}^D T_{d,ab} Z_{i1}^A - \sum_{b=1}^3 \sum_{a=1}^3 Z_{j3+a}^{D,*} T_{d,ab}^* Z_{kb}^D Z_{i1}^A \right. \\ & \left. + \left( -\mu \sum_{b=1}^3 \sum_{a=1}^3 Y_{d,ab}^* Z_{j3+a}^{D,*} Z_{kb}^D + \mu^* \sum_{b=1}^3 Z_{jb}^{D,*} \sum_{a=1}^3 Y_{d,ab} Z_{k3+a}^D \right) Z_{i2}^A \right) \end{aligned} \quad (192)$$

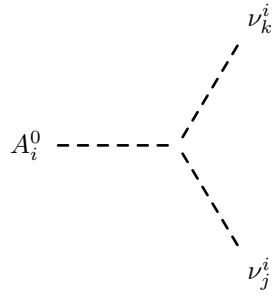

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$$\begin{aligned} & \frac{1}{\sqrt{2}} \left( \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Z_{k3+a}^E T_{e,ab} Z_{i1}^A - \sum_{b=1}^3 \sum_{a=1}^3 Z_{j3+a}^{E,*} T_{e,ab}^* Z_{kb}^E Z_{i1}^A \right. \\ & \left. + \left( -\mu \sum_{b=1}^3 \sum_{a=1}^3 Y_{e,ab}^* Z_{j3+a}^{E,*} Z_{kb}^E + \mu^* \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Y_{e,ab} Z_{k3+a}^E \right) Z_{i2}^A \right) \end{aligned} \quad (193)$$



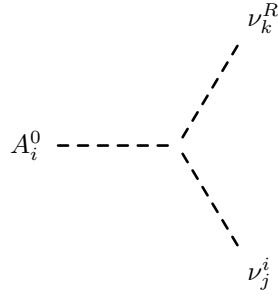
$$\begin{aligned} & \frac{1}{\sqrt{2}} \delta_{\beta\gamma} \left( \mu^* \sum_{b=1}^3 Z_{jb}^{U,*} \sum_{a=1}^3 Y_{u,ab} Z_{k3+a}^U Z_{i1}^A - \mu \sum_{b=1}^3 \sum_{a=1}^3 Y_{u,ab}^* Z_{j3+a}^{U,*} Z_{kb}^U Z_{i1}^A \right. \\ & \left. + \left( - \sum_{b=1}^3 \sum_{a=1}^3 Z_{j3+a}^{U,*} T_{u,ab}^* Z_{kb}^U + \sum_{b=1}^3 Z_{jb}^{U,*} \sum_{a=1}^3 Z_{k3+a}^U T_{u,ab} \right) Z_{i2}^A \right) \end{aligned} \quad (194)$$



$$\begin{aligned} & \frac{1}{8} \left( -v_u \mu^* \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} Z_{i1}^A - v_u \mu^* \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,ab} Z_{i1}^A \right. \\ & + 2v_u \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} Q_{\nu,ab}^* Z_{i2}^A + 2v_u \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab}^* Z_{i2}^A \\ & \left. + v_d \mu^* \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} Z_{i2}^A + v_d \mu^* \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,ab} Z_{i2}^A \right) \end{aligned}$$

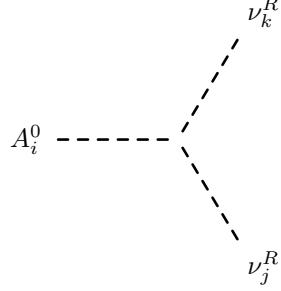
$$\begin{aligned}
& -2v_u \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} Q_{\nu,ab} Z_{i2}^A - 2v_u \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab} Z_{i2}^A \\
& + Z_{k1}^{i,*} \left( 2v_u \mu \sum_{a=1}^3 \kappa_{\nu,a1}^* Z_{ja}^{i,*} Z_{i1}^A + v_d \mu^* \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,a1} Z_{i2}^A \right) \\
& + Z_{j1}^{i,*} \left( 2v_u \mu \sum_{a=1}^3 \kappa_{\nu,a1}^* Z_{ka}^{i,*} Z_{i1}^A + v_d \mu^* \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,a1} Z_{i2}^A \right)
\end{aligned} \tag{195}$$


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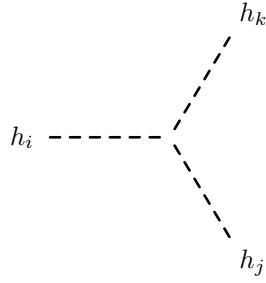


$$\begin{aligned}
& \frac{i}{8} \left( v_u \mu^* \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} Z_{i1}^A + v_u \mu^* \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} Z_{i1}^A \right. \\
& + 2v_u \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{i,*} Q_{\nu,ab}^* Z_{i2}^A + 2v_u \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{R,*} Q_{\nu,ab}^* Z_{i2}^A \\
& - v_d \mu^* \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} Z_{i2}^A - v_d \mu^* \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} Z_{i2}^A \\
& + 2v_u \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{i,*} Q_{\nu,ab} Z_{i2}^A + 2v_u \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{R,*} Q_{\nu,ab} Z_{i2}^A \\
& + Z_{k1}^{R,*} \left( 2v_u \mu \sum_{a=1}^3 \kappa_{\nu,a1}^* Z_{ja}^{i,*} Z_{i1}^A - v_d \mu^* \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,a1} Z_{i2}^A \right) \\
& \left. + Z_{j1}^{i,*} \left( 2v_u \mu \sum_{a=1}^3 \kappa_{\nu,a1}^* Z_{ka}^{R,*} Z_{i1}^A - v_d \mu^* \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,a1} Z_{i2}^A \right) \right)
\end{aligned} \tag{196}$$

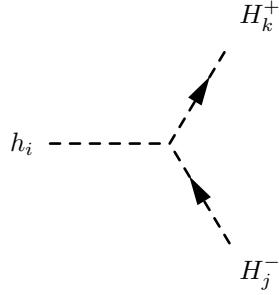

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$$\begin{aligned}
& \frac{1}{8} \left( v_u \mu^* \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,ab} Z_{i1}^A + v_u \mu^* \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} Z_{i1}^A \right. \\
& - 2v_u \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{R,*} Q_{\nu,ab}^* Z_{i2}^A - 2v_u \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} Q_{\nu,ab}^* Z_{i2}^A \\
& - v_d \mu^* \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,ab} Z_{i2}^A - v_d \mu^* \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} Z_{i2}^A \\
& + 2v_u \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{R,*} Q_{\nu,ab} Z_{i2}^A + 2v_u \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} Q_{\nu,ab} Z_{i2}^A \\
& \left. - Z_{k1}^{R,*} \left( 2v_u \mu \sum_{a=1}^3 \kappa_{\nu,a1}^* Z_{ja}^{R,*} Z_{i1}^A + v_d \mu^* \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,a1} Z_{i2}^A \right) \right. \\
& \left. - Z_{j1}^{R,*} \left( 2v_u \mu \sum_{a=1}^3 \kappa_{\nu,a1}^* Z_{ka}^{R,*} Z_{i1}^A + v_d \mu^* \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,a1} Z_{i2}^A \right) \right) \tag{197}
\end{aligned}$$

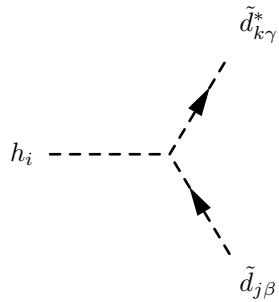


$$\begin{aligned}
& \frac{i}{4} \left( g_1^2 + g_2^2 \right) \left( Z_{i2}^H \left( Z_{j1}^H \left( v_d Z_{k2}^H + v_u Z_{k1}^H \right) + Z_{j2}^H \left( -3v_u Z_{k2}^H + v_d Z_{k1}^H \right) \right) \right. \\
& \left. + Z_{i1}^H \left( Z_{j1}^H \left( -3v_d Z_{k1}^H + v_u Z_{k2}^H \right) + Z_{j2}^H \left( v_d Z_{k2}^H + v_u Z_{k1}^H \right) \right) \right) \tag{198}
\end{aligned}$$



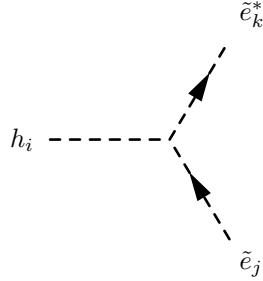
$$\begin{aligned}
& - \frac{i}{4} \left( Z_{i1}^H \left( Z_{j1}^+ \left( (g_1^2 + g_2^2) v_d Z_{k1}^+ + g_2^2 v_u Z_{k2}^+ \right) + Z_{j2}^+ \left( (-g_1^2 + g_2^2) v_d Z_{k2}^+ + g_2^2 v_u Z_{k1}^+ \right) \right) \right. \\
& \left. + Z_{i2}^H \left( Z_{j1}^+ \left( (-g_1^2 + g_2^2) v_u Z_{k1}^+ + g_2^2 v_d Z_{k2}^+ \right) + Z_{j2}^+ \left( (g_1^2 + g_2^2) v_u Z_{k2}^+ + g_2^2 v_d Z_{k1}^+ \right) \right) \right)
\end{aligned} \tag{199}$$


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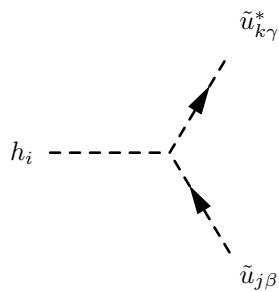


$$\begin{aligned}
& \frac{i}{12} \delta_{\beta\gamma} \left( (3g_2^2 + g_1^2) \sum_{a=1}^3 Z_{ja}^{D,*} Z_{ka}^D \left( v_d Z_{i1}^H - v_u Z_{i2}^H \right) \right. \\
& + 2 \left( g_1^2 \sum_{a=1}^3 Z_{j3+a}^{D,*} Z_{k3+a}^D \left( v_d Z_{i1}^H - v_u Z_{i2}^H \right) \right. \\
& - 3 \left( \sqrt{2} \sum_{b=1}^3 Z_{jb}^{D,*} \sum_{a=1}^3 Z_{k3+a}^D T_{d,ab} Z_{i1}^H + \sqrt{2} \sum_{b=1}^3 \sum_{a=1}^3 Z_{j3+a}^{D,*} T_{d,ab}^* Z_{kb}^D Z_{i1}^H \right. \\
& + 2v_d \sum_{c=1}^3 Z_{j3+c}^{D,*} \sum_{b=1}^3 \sum_{a=1}^3 Y_{d,ca}^* Y_{d,ba} Z_{k3+b}^D Z_{i1}^H + 2v_d \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{D,*} \sum_{a=1}^3 Y_{d,ac}^* Y_{d,ab} Z_{kc}^D Z_{i1}^H \\
& \left. \left. - \sqrt{2} \mu^* \sum_{b=1}^3 Z_{jb}^{D,*} \sum_{a=1}^3 Y_{d,ab} Z_{k3+a}^D Z_{i2}^H - \sqrt{2} \mu \sum_{b=1}^3 \sum_{a=1}^3 Y_{d,ab}^* Z_{j3+a}^{D,*} Z_{kb}^D Z_{i2}^H \right) \right)
\end{aligned} \tag{200}$$


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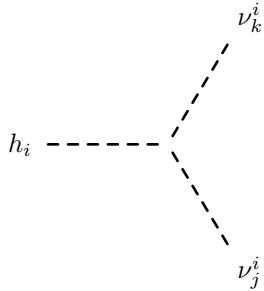
$$\begin{aligned}
& -\frac{i}{4} \left( \left( -g_2^2 + g_1^2 \right) \sum_{a=1}^3 Z_{ja}^{E,*} Z_{ka}^E \left( v_d Z_{i1}^H - v_u Z_{i2}^H \right) \right. \\
& + 2 \left( \sqrt{2} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Z_{k3+a}^E T_{e,ab} Z_{i1}^H + \sqrt{2} \sum_{b=1}^3 \sum_{a=1}^3 Z_{j3+a}^{E,*} T_{e,ab}^* Z_{kb}^E Z_{i1}^H \right. \\
& + 2v_d \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 \sum_{a=1}^3 Y_{e,ca}^* Y_{e,ba} Z_{k3+b}^E Z_{i1}^H + 2v_d \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{e,ab} Z_{kc}^E Z_{i1}^H \\
& - \sqrt{2}\mu^* \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Y_{e,ab} Z_{k3+a}^E Z_{i2}^H - \sqrt{2}\mu \sum_{b=1}^3 \sum_{a=1}^3 Y_{e,ab}^* Z_{j3+a}^{E,*} Z_{kb}^E Z_{i2}^H \\
& \left. \left. + g_1^2 \sum_{a=1}^3 Z_{j3+a}^{E,*} Z_{k3+a}^E \left( -v_d Z_{i1}^H + v_u Z_{i2}^H \right) \right) \right) \tag{201}
\end{aligned}$$



$$\begin{aligned}
& \frac{i}{12} \delta_{\beta\gamma} \left( \left( -3g_2^2 + g_1^2 \right) \sum_{a=1}^3 Z_{ja}^{U,*} Z_{ka}^U \left( v_d Z_{i1}^H - v_u Z_{i2}^H \right) \right. \\
& - 2 \left( -3\sqrt{2}\mu^* \sum_{b=1}^3 Z_{jb}^{U,*} \sum_{a=1}^3 Y_{u,ab} Z_{k3+a}^U Z_{i1}^H - 3\sqrt{2}\mu \sum_{b=1}^3 \sum_{a=1}^3 Y_{u,ab}^* Z_{j3+a}^{U,*} Z_{kb}^U Z_{i1}^H \right. \\
& + 3\sqrt{2} \sum_{b=1}^3 Z_{jb}^{U,*} \sum_{a=1}^3 Z_{k3+a}^U T_{u,ab} Z_{i2}^H + 3\sqrt{2} \sum_{b=1}^3 \sum_{a=1}^3 Z_{j3+a}^{U,*} T_{u,ab}^* Z_{kb}^U Z_{i2}^H
\end{aligned}$$

$$\begin{aligned}
& + 6v_u \sum_{c=1}^3 Z_{j3+c}^{U,*} \sum_{b=1}^3 \sum_{a=1}^3 Y_{u,ca}^* Y_{u,ba} Z_{k3+b}^U Z_{i2}^H + 6v_u \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{U,*} \sum_{a=1}^3 Y_{u,ac}^* Y_{u,ab} Z_{kc}^U Z_{i2}^H \\
& + 2g_1^2 \sum_{a=1}^3 Z_{j3+a}^{U,*} Z_{k3+a}^U \left( v_d Z_{i1}^H - v_u Z_{i2}^H \right) \Big) \Big) \tag{202}
\end{aligned}$$

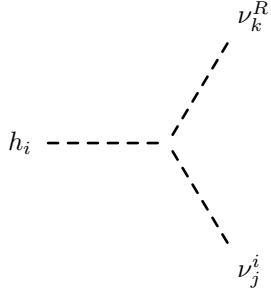

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$$\begin{aligned}
& - \frac{i}{8} \left( 2g_1^2 v_d \sum_{a=1}^3 Z_{ja}^{i,*} Z_{ka}^{i,*} Z_{i1}^H + 2g_2^2 v_d \sum_{a=1}^3 Z_{ja}^{i,*} Z_{ka}^{i,*} Z_{i1}^H \right. \\
& + v_u \mu^* \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} Z_{i1}^H + v_u \mu^* \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,ab} Z_{i1}^H \\
& - 2g_1^2 v_u \sum_{a=1}^3 Z_{ja}^{i,*} Z_{ka}^{i,*} Z_{i2}^H - 2g_2^2 v_u \sum_{a=1}^3 Z_{ja}^{i,*} Z_{ka}^{i,*} Z_{i2}^H \\
& - 2v_u \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} Q_{\nu,ab}^* Z_{i2}^H - 2v_u \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab}^* Z_{i2}^H \\
& + v_d \mu^* \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} Z_{i2}^H + v_d \mu^* \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,ab} Z_{i2}^H \\
& - 2v_u \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} Q_{\nu,ab} Z_{i2}^H - 2v_u \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab} Z_{i2}^H \\
& + v_u^3 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{i2}^H + v_u^3 \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{i2}^H \\
& + v_u^3 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{i2}^H + v_u^3 \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{i2}^H \\
& + v_u^3 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} Z_{i2}^H + v_u^3 \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} Z_{i2}^H \\
& + v_u^3 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} Z_{i2}^H + v_u^3 \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} Z_{i2}^H
\end{aligned}$$

$$\begin{aligned}
& + 4v_u \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} Z_{i2}^H + 4v_u \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} Z_{i2}^H \\
& + Z_{k1}^{i,*} \left( 2v_u \mu \sum_{a=1}^3 \kappa_{\nu,a1}^* Z_{ja}^{i,*} Z_{i1}^H + v_d \mu^* \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,a1} Z_{i2}^H \right) \\
& + Z_{j1}^{i,*} \left( 2v_u \mu \sum_{a=1}^3 \kappa_{\nu,a1}^* Z_{ka}^{i,*} Z_{i1}^H + v_d \mu^* \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,a1} Z_{i2}^H \right)
\end{aligned} \tag{203}$$

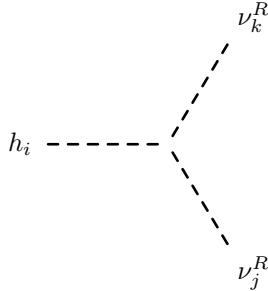

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$$\begin{aligned}
& \frac{1}{8} \left( -v_u \mu^* \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} Z_{i1}^H - v_u \mu^* \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} Z_{i1}^H \right. \\
& - 2v_u \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{i,*} Q_{\nu,ab}^* Z_{i2}^H - 2v_u \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{R,*} Q_{\nu,ab}^* Z_{i2}^H \\
& - v_d \mu^* \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} Z_{i2}^H - v_d \mu^* \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} Z_{i2}^H \\
& + 2v_u \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{i,*} Q_{\nu,ab} Z_{i2}^H + 2v_u \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{R,*} Q_{\nu,ab} Z_{i2}^H \\
& + v_u^3 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{i2}^H \\
& - v_u^3 \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{i2}^H \\
& + v_u^3 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{i2}^H \\
& - v_u^3 \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{i2}^H \\
& + v_u^3 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} Z_{i2}^H
\end{aligned}$$

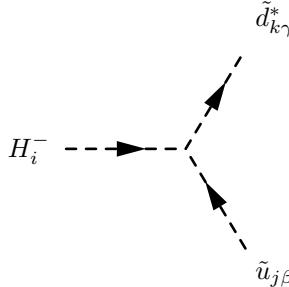
$$\begin{aligned}
& - v_u^3 \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} Z_{i2}^H \\
& + v_u^3 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} Z_{i2}^H \\
& - v_u^3 \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} Z_{i2}^H \\
& + 4v_u \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} Z_{i2}^H - 4v_u \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} Z_{i2}^H \\
& + Z_{k1}^{R,*} \left( 2v_u \mu \sum_{a=1}^3 \kappa_{\nu,a1}^* Z_{ja}^{i,*} Z_{i1}^H - v_d \mu^* \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,a1} Z_{i2}^H \right) \\
& + Z_{j1}^{i,*} \left( 2v_u \mu \sum_{a=1}^3 \kappa_{\nu,a1}^* Z_{ka}^{R,*} Z_{i1}^H - v_d \mu^* \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,a1} Z_{i2}^H \right) \tag{204}
\end{aligned}$$


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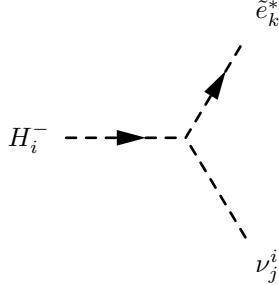
$$\begin{aligned}
& - \frac{i}{8} \left( 2g_1^2 v_d \sum_{a=1}^3 Z_{ja}^{R,*} Z_{ka}^{R,*} Z_{i1}^H + 2g_2^2 v_d \sum_{a=1}^3 Z_{ja}^{R,*} Z_{ka}^{R,*} Z_{i1}^H \right. \\
& - v_u \mu^* \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,ab} Z_{i1}^H - v_u \mu^* \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} Z_{i1}^H \\
& - 2g_1^2 v_u \sum_{a=1}^3 Z_{ja}^{R,*} Z_{ka}^{R,*} Z_{i2}^H - 2g_2^2 v_u \sum_{a=1}^3 Z_{ja}^{R,*} Z_{ka}^{R,*} Z_{i2}^H \\
& + 2v_u \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{R,*} Q_{\nu,ab}^* Z_{i2}^H + 2v_u \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} Q_{\nu,ab}^* Z_{i2}^H \\
& - v_d \mu^* \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,ab} Z_{i2}^H - v_d \mu^* \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} Z_{i2}^H \\
& \left. + 2v_u \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{R,*} Q_{\nu,ab} Z_{i2}^H + 2v_u \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} Q_{\nu,ab} Z_{i2}^H \right)
\end{aligned}$$

$$\begin{aligned}
& + v_u^3 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{i2}^H + v_u^3 \sum_{c=1}^3 Z_{jc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{i2}^H \\
& + v_u^3 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{i2}^H + v_u^3 \sum_{c=1}^3 Z_{jc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{i2}^H \\
& + v_u^3 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} Z_{i2}^H + v_u^3 \sum_{c=1}^3 Z_{jc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} Z_{i2}^H \\
& + v_u^3 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} Z_{i2}^H + v_u^3 \sum_{c=1}^3 Z_{jc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} Z_{i2}^H \\
& + 4v_u \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} Z_{i2}^H + 4v_u \sum_{c=1}^3 Z_{jc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} Z_{i2}^H \\
& - Z_{k1}^{R,*} \left( 2v_u \mu \sum_{a=1}^3 \kappa_{\nu,a1}^* Z_{ja}^{R,*} Z_{i1}^H + v_d \mu^* \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,a1} Z_{i2}^H \right) \\
& - Z_{j1}^{R,*} \left( 2v_u \mu \sum_{a=1}^3 \kappa_{\nu,a1}^* Z_{ka}^{R,*} Z_{i1}^H + v_d \mu^* \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,a1} Z_{i2}^H \right)
\end{aligned} \tag{205}$$



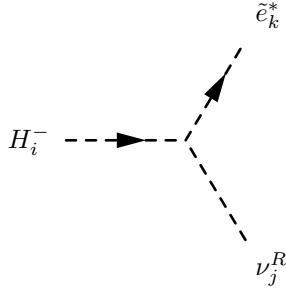
$$\begin{aligned}
& - \frac{i}{4} \delta_{\beta\gamma} \left( \sqrt{2} g_2^2 \sum_{a=1}^3 Z_{ja}^{U,*} Z_{ka}^D \left( v_d Z_{i1}^+ + v_u Z_{i2}^+ \right) \right. \\
& \left. - 2 \left( 2 \sum_{b=1}^3 Z_{jb}^{U,*} \sum_{a=1}^3 Z_{k3+a}^D T_{d,ab} Z_{i1}^+ + 2\mu \sum_{b=1}^3 \sum_{a=1}^3 Y_{u,ab}^* Z_{j3+a}^{U,*} Z_{kb}^D Z_{i1}^+ \right. \right. \\
& \left. \left. + \sqrt{2} v_u \sum_{c=1}^3 Z_{j3+c}^{U,*} \sum_{b=1}^3 \sum_{a=1}^3 Y_{u,ca}^* Y_{d,ba} Z_{k3+b}^D Z_{i1}^+ \right. \right. \\
& \left. \left. + \sqrt{2} v_d \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{U,*} \sum_{a=1}^3 Y_{d,ac}^* Y_{d,ab} Z_{kc}^D Z_{i1}^+ + 2\mu^* \sum_{b=1}^3 Z_{jb}^{U,*} \sum_{a=1}^3 Y_{d,ab} Z_{k3+a}^D Z_{i2}^+ \right. \right. \\
& \left. \left. + 2 \sum_{b=1}^3 \sum_{a=1}^3 Z_{j3+a}^{U,*} T_{u,ab}^* Z_{kb}^D Z_{i2}^+ + \sqrt{2} v_d \sum_{c=1}^3 Z_{j3+c}^{U,*} \sum_{b=1}^3 \sum_{a=1}^3 Y_{u,ca}^* Y_{d,ba} Z_{k3+b}^D Z_{i2}^+ \right) \right)
\end{aligned}$$

$$+ \sqrt{2}v_u \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{U,*} \sum_{a=1}^3 Y_{u,ac}^* Y_{u,ab} Z_{kc}^D Z_{i2}^+ \Big) \Big) \quad (206)$$

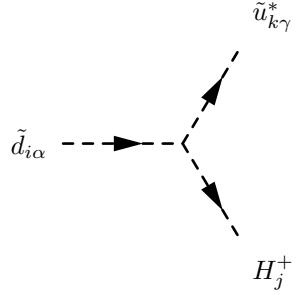


$$\begin{aligned}
& \frac{1}{16} \left( 4v_u \mu Z_{j1}^{i,*} \sum_{a=1}^3 \kappa_{\nu,a1}^* Z_{ka}^E Z_{i1}^+ - 8\sqrt{2} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{k3+a}^E T_{e,ab} Z_{i1}^+ \right. \\
& + 2\sqrt{2}v_u^2 \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ac}^* Y_{e,ba} Z_{k3+b}^E Z_{i1}^+ \\
& + 2\sqrt{2}v_u^2 \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ca}^* Y_{e,ba} Z_{k3+b}^E Z_{i1}^+ \\
& - 8v_d \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{e,ab} Z_{kc}^E Z_{i1}^+ + 4v_u \mu \sum_{a=1}^3 \kappa_{\nu,a1}^* Z_{ja}^{i,*} Z_{k1}^E Z_{i1}^+ \\
& + 4v_u \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Q_{\nu,ab}^* Z_{ka}^E Z_{i2}^+ - 8\sqrt{2}\mu^* \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Y_{e,ab} Z_{k3+a}^E Z_{i2}^+ \\
& + 4v_u \sum_{b=1}^3 \sum_{a=1}^3 Z_{ja}^{i,*} Q_{\nu,ab}^* Z_{kb}^E Z_{i2}^+ + 2\sqrt{2}v_d v_u \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ac}^* Y_{e,ba} Z_{k3+b}^E Z_{i2}^+ \\
& + 2\sqrt{2}v_d v_u \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ca}^* Y_{e,ba} Z_{k3+b}^E Z_{i2}^+ \\
& - v_u^3 \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{kc}^E Z_{i2}^+ \\
& - v_u^3 \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{kc}^E Z_{i2}^+ \\
& - v_u^3 \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} Z_{kc}^E Z_{i2}^+ \\
& - v_u^3 \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} Z_{kc}^E Z_{i2}^+ - 8v_u \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} Z_{kc}^E Z_{i2}^+
\end{aligned}$$

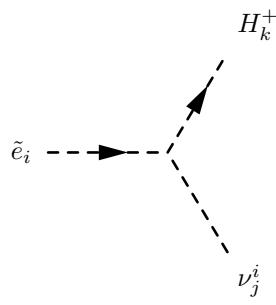
$$+ 4g_2^2 \sum_{a=1}^3 Z_{ja}^{i,*} Z_{ka}^E \left( v_d Z_{i1}^+ + v_u Z_{i2}^+ \right) \quad (207)$$



$$\begin{aligned}
& \frac{i}{16} \left( 4v_u \mu Z_{j1}^{R,*} \sum_{a=1}^3 \kappa_{\nu,a1}^* Z_{ka}^E Z_{i1}^+ + 8\sqrt{2} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{k3+a}^E T_{e,ab} Z_{i1}^+ \right. \\
& + 2\sqrt{2} v_u^2 \sum_{c=1}^3 Z_{jc}^{R,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ac}^* Y_{e,ba} Z_{k3+b}^E Z_{i1}^+ \\
& + 2\sqrt{2} v_u^2 \sum_{c=1}^3 Z_{jc}^{R,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ca}^* Y_{e,ba} Z_{k3+b}^E Z_{i1}^+ \\
& + 8v_d \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{e,ab} Z_{kc}^E Z_{i1}^+ + 4v_u \mu \sum_{a=1}^3 \kappa_{\nu,a1}^* Z_{ja}^{R,*} Z_{k1}^E Z_{i1}^+ \\
& + 4v_u \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Q_{\nu,ab}^* Z_{ka}^E Z_{i2}^+ + 8\sqrt{2} \mu^* \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Y_{e,ab} Z_{k3+a}^E Z_{i2}^+ \\
& + 4v_u \sum_{b=1}^3 \sum_{a=1}^3 Z_{ja}^{R,*} Q_{\nu,ab}^* Z_{kb}^E Z_{i2}^+ + 2\sqrt{2} v_d v_u \sum_{c=1}^3 Z_{jc}^{R,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ac}^* Y_{e,ba} Z_{k3+b}^E Z_{i2}^+ \\
& + 2\sqrt{2} v_d v_u \sum_{c=1}^3 Z_{jc}^{R,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ca}^* Y_{e,ba} Z_{k3+b}^E Z_{i2}^+ \\
& + v_u^3 \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{kc}^E Z_{i2}^+ + v_u^3 \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{kc}^E Z_{i2}^+ \\
& + v_u^3 \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} Z_{kc}^E Z_{i2}^+ + v_u^3 \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} Z_{kc}^E Z_{i2}^+ \\
& \left. + 8v_u \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} Z_{kc}^E Z_{i2}^+ - 4g_2^2 \sum_{a=1}^3 Z_{ja}^{R,*} Z_{ka}^E \left( v_d Z_{i1}^+ + v_u Z_{i2}^+ \right) \right) \quad (208)
\end{aligned}$$

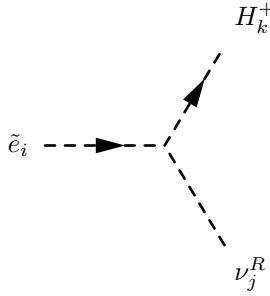


$$\begin{aligned}
& -\frac{i}{4}\delta_{\alpha\gamma}\left(\sqrt{2}g_2^2\sum_{a=1}^3Z_{ia}^{D,*}Z_{ka}^U\left(v_dZ_{j1}^++v_uZ_{j2}^+\right)\right. \\
& -2\left(2\mu^*\sum_{b=1}^3Z_{ib}^{D,*}\sum_{a=1}^3Y_{u,ab}Z_{k3+a}^UZ_{j1}^++2\sum_{b=1}^3\sum_{a=1}^3Z_{i3+a}^{D,*}T_{d,ab}^*Z_{kb}^UZ_{j1}^+\right. \\
& +\sqrt{2}v_u\sum_{c=1}^3Z_{i3+c}^{D,*}\sum_{b=1}^3\sum_{a=1}^3Y_{d,ca}^*Y_{u,ba}Z_{k3+b}^UZ_{j1}^+ \\
& +\sqrt{2}v_d\sum_{c=1}^3\sum_{b=1}^3Z_{ib}^{D,*}\sum_{a=1}^3Y_{d,ac}^*Y_{d,ab}Z_{kc}^UZ_{j1}^++2\sum_{b=1}^3Z_{ib}^{D,*}\sum_{a=1}^3Z_{k3+a}^UT_{u,ab}Z_{j2}^+ \\
& +2\mu\sum_{b=1}^3\sum_{a=1}^3Y_{d,ab}^*Z_{i3+a}^{D,*}Z_{kb}^UZ_{j2}^++\sqrt{2}v_d\sum_{c=1}^3Z_{i3+c}^{D,*}\sum_{b=1}^3\sum_{a=1}^3Y_{d,ca}^*Y_{u,ba}Z_{k3+b}^UZ_{j2}^+ \\
& \left.\left.+\sqrt{2}v_u\sum_{c=1}^3\sum_{b=1}^3Z_{ib}^{D,*}\sum_{a=1}^3Y_{u,ac}^*Y_{u,ab}Z_{kc}^UZ_{j2}^+\right)\right) \tag{209}
\end{aligned}$$



$$\begin{aligned}
& \frac{1}{16}\left(8\sqrt{2}\sum_{b=1}^3Z_{jb}^{i,*}\sum_{a=1}^3Z_{i3+a}^{E,*}T_{e,ab}^*Z_{k1}^+-4v_u\mu^*\sum_{b=1}^3Z_{jb}^{i,*}\sum_{a=1}^3Z_{ia}^{E,*}\kappa_{\nu,ab}Z_{k1}^+\right. \\
& -2\sqrt{2}v_u^2\sum_{c=1}^3Z_{i3+c}^{E,*}\sum_{b=1}^3Z_{jb}^{i,*}\sum_{a=1}^3Y_{e,ca}^*\kappa_{\nu,ab}Z_{k1}^+
\end{aligned}$$

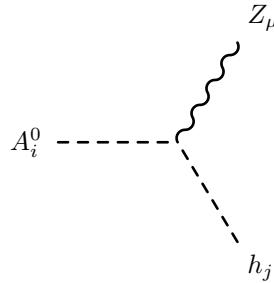
$$\begin{aligned}
& -2\sqrt{2}v_u^2 \sum_{c=1}^3 Z_{i3+c}^{E,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ba} Z_{k1}^+ \\
& + 8v_d \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{e,ab} Z_{k1}^+ + 4v_d \mu^* Z_{j1}^{i,*} \sum_{a=1}^3 Z_{ia}^{E,*} \kappa_{\nu,a1} Z_{k2}^+ \\
& + 8\sqrt{2}\mu \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Y_{e,ab}^* Z_{i3+a}^{E,*} Z_{k2}^+ + 4v_d \mu^* \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} Z_{k2}^+ \\
& - 4v_u \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ia}^{E,*} Q_{\nu,ab} Z_{k2}^+ - 4v_u \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 Z_{ja}^{i,*} Q_{\nu,ab} Z_{k2}^+ \\
& + v_u^3 \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{k2}^+ + v_u^3 \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{k2}^+ \\
& - 2\sqrt{2}v_d v_u \sum_{c=1}^3 Z_{i3+c}^{E,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ab} Z_{k2}^+ \\
& + v_u^3 \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} Z_{k2}^+ + v_u^3 \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} Z_{k2}^+ \\
& - 2\sqrt{2}v_d v_u \sum_{c=1}^3 Z_{i3+c}^{E,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ba} Z_{k2}^+ \\
& + 8v_u \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} Z_{k2}^+ - 4g_2^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ja}^{i,*} (v_d Z_{k1}^+ + v_u Z_{k2}^+) \tag{210}
\end{aligned}$$



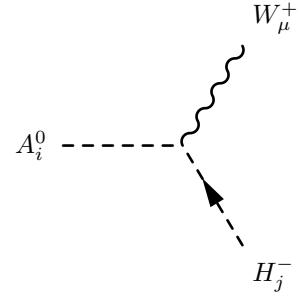
$$\begin{aligned}
& \frac{i}{16} \left( 8\sqrt{2} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{i3+a}^{E,*} T_{e,ab}^* Z_{k1}^+ + 4v_u \mu^* \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ia}^{E,*} \kappa_{\nu,ab} Z_{k1}^+ \right. \\
& \left. + 2\sqrt{2}v_u^2 \sum_{c=1}^3 Z_{i3+c}^{E,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ab} Z_{k1}^+ \right. \\
& \left. + 2\sqrt{2}v_u^2 \sum_{c=1}^3 Z_{i3+c}^{E,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ba} Z_{k1}^+ \right)
\end{aligned}$$

$$\begin{aligned}
& + 8v_d \sum_{c=1}^3 Z_{jc}^{R,*} \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{e,ab} Z_{k1}^+ - 4v_d \mu^* Z_{j1}^{R,*} \sum_{a=1}^3 Z_{ia}^{E,*} \kappa_{\nu,a1} Z_{k2}^+ \\
& + 8\sqrt{2}\mu \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Y_{e,ab}^* Z_{i3+a}^{E,*} Z_{k2}^+ - 4v_d \mu^* \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,ab} Z_{k2}^+ \\
& + 4v_u \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ia}^{E,*} Q_{\nu,ab} Z_{k2}^+ + 4v_u \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 Z_{ja}^{R,*} Q_{\nu,ab} Z_{k2}^+ \\
& + v_u^3 \sum_{c=1}^3 Z_{jc}^{R,*} \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{k2}^+ + v_u^3 \sum_{c=1}^3 Z_{jc}^{R,*} \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{k2}^+ \\
& + 2\sqrt{2}v_d v_u \sum_{c=1}^3 Z_{i3+c}^{E,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ab} Z_{k2}^+ \\
& + v_u^3 \sum_{c=1}^3 Z_{jc}^{R,*} \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} Z_{k2}^+ + v_u^3 \sum_{c=1}^3 Z_{jc}^{R,*} \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} Z_{k2}^+ \\
& + 2\sqrt{2}v_d v_u \sum_{c=1}^3 Z_{i3+c}^{E,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ba} Z_{k2}^+ \\
& + 8v_u \sum_{c=1}^3 Z_{jc}^{R,*} \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} Z_{k2}^+ - 4g_2^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ja}^{R,*} (v_d Z_{k1}^+ + v_u Z_{k2}^+) \tag{211}
\end{aligned}$$

## 9.2 Two Scalar-One Vector Boson-Interaction

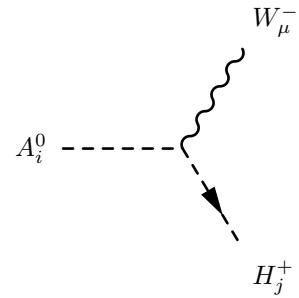


$$\frac{1}{2} (g_1 \sin \Theta_W + g_2 \cos \Theta_W) (Z_{i1}^A Z_{j1}^H - Z_{i2}^A Z_{j2}^H) (-p_\mu^{h_j} + p_\mu^{A_i^0}) \tag{212}$$



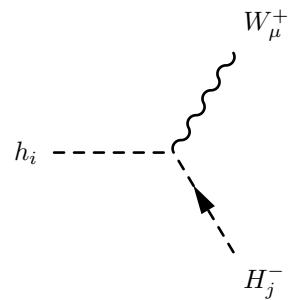
$$\frac{1}{2}g_2 \left( Z_{i1}^A Z_{j1}^+ + Z_{i2}^A Z_{j2}^+ \right) \left( -p_\mu^{H_j^-} + p_\mu^{A_i^0} \right) \quad (213)$$


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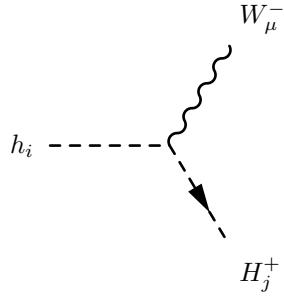
$$\frac{1}{2}g_2 \left( Z_{i1}^A Z_{j1}^+ + Z_{i2}^A Z_{j2}^+ \right) \left( -p_\mu^{H_j^+} + p_\mu^{A_i^0} \right) \quad (214)$$


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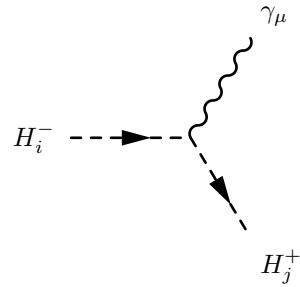
$$\frac{i}{2}g_2 \left( Z_{i1}^H Z_{j1}^+ - Z_{i2}^H Z_{j2}^+ \right) \left( -p_\mu^{H_j^-} + p_\mu^{h_i} \right) \quad (215)$$


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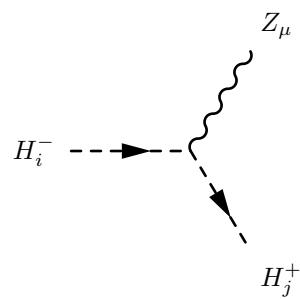
$$-\frac{i}{2}g_2 \left( Z_{i1}^H Z_{j1}^+ - Z_{i2}^H Z_{j2}^+ \right) \left( -p_\mu^{H_j^+} + p_\mu^{h_i} \right) \quad (216)$$


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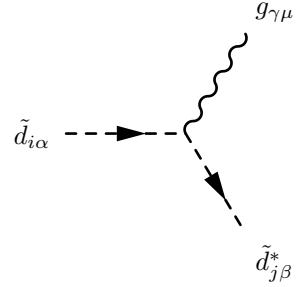
$$\frac{i}{2} \left( g_1 \cos \Theta_W + g_2 \sin \Theta_W \right) \left( Z_{i1}^+ Z_{j1}^+ + Z_{i2}^+ Z_{j2}^+ \right) \left( -p_\mu^{H_j^+} + p_\mu^{H_i^-} \right) \quad (217)$$


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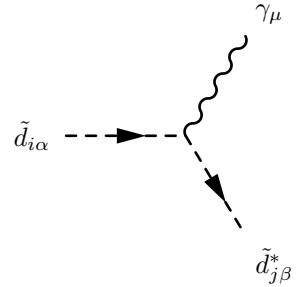
$$\frac{i}{2} \left( -g_1 \sin \Theta_W + g_2 \cos \Theta_W \right) \left( Z_{i1}^+ Z_{j1}^+ + Z_{i2}^+ Z_{j2}^+ \right) \left( -p_\mu^{H_j^+} + p_\mu^{H_i^-} \right) \quad (218)$$


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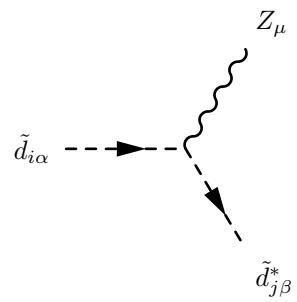
$$- \frac{i}{2} g_3 \delta_{ij} \lambda_{\beta,\alpha}^\gamma \left( - p_\mu^{\tilde{d}_{j\beta}^*} + p_\mu^{\tilde{d}_{i\alpha}} \right) \quad (219)$$


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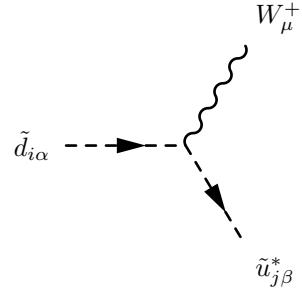
$$- \frac{i}{6} \delta_{\alpha\beta} \left( - 2g_1 \cos \Theta_W \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{j3+a}^D + \left( - 3g_2 \sin \Theta_W + g_1 \cos \Theta_W \right) \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ja}^D \right) \left( - p_\mu^{\tilde{d}_{j\beta}^*} + p_\mu^{\tilde{d}_{i\alpha}} \right) \quad (220)$$


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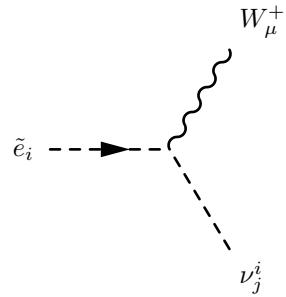
$$\frac{i}{6} \delta_{\alpha\beta} \left( - 2g_1 \sin \Theta_W \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{j3+a}^D + \left( 3g_2 \cos \Theta_W + g_1 \sin \Theta_W \right) \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ja}^D \right) \left( - p_\mu^{\tilde{d}_{j\beta}^*} + p_\mu^{\tilde{d}_{i\alpha}} \right) \quad (221)$$


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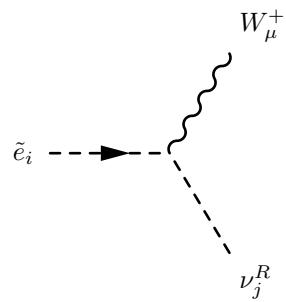
$$- i \frac{1}{\sqrt{2}} g_2 \delta_{\alpha\beta} \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ja}^U \left( - p_\mu^{\tilde{u}_{j\beta}^*} + p_\mu^{\tilde{d}_{i\alpha}} \right) \quad (222)$$


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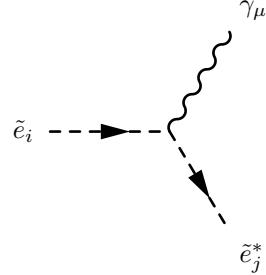
$$- \frac{1}{2} g_2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ja}^{i,*} \left( - p_\mu^{\nu_j^i} + p_\mu^{\tilde{e}_i} \right) \quad (223)$$


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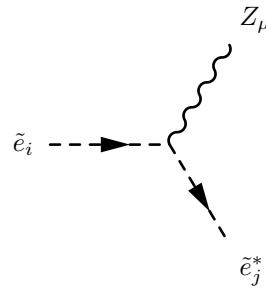
$$- \frac{i}{2} g_2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ja}^{R,*} \left( - p_\mu^{\nu_j^R} + p_\mu^{\tilde{e}_i} \right) \quad (224)$$


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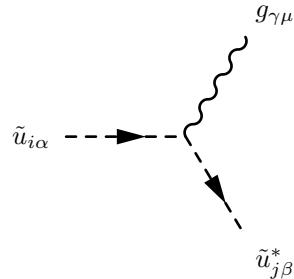
$$\frac{i}{2} \left( 2g_1 \cos \Theta_W \sum_{a=1}^3 Z_{i3+a}^{E,*} Z_{j3+a}^E + \left( g_1 \cos \Theta_W + g_2 \sin \Theta_W \right) \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ja}^E \right) \left( -p_\mu^{\tilde{e}_j^*} + p_\mu^{\tilde{e}_i} \right) \quad (225)$$


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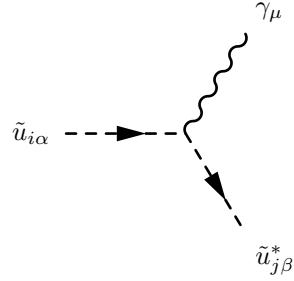
$$\frac{i}{2} \left( -2g_1 \sin \Theta_W \sum_{a=1}^3 Z_{i3+a}^{E,*} Z_{j3+a}^E + \left( -g_1 \sin \Theta_W + g_2 \cos \Theta_W \right) \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ja}^E \right) \left( -p_\mu^{\tilde{e}_j^*} + p_\mu^{\tilde{e}_i} \right) \quad (226)$$


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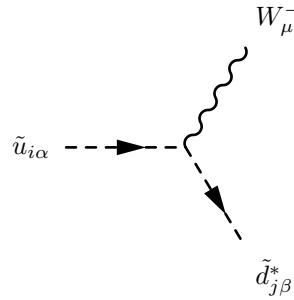
$$- \frac{i}{2} g_3 \delta_{ij} \lambda_{\beta,\alpha}^\gamma \left( -p_\mu^{\tilde{u}_{j\beta}^*} + p_\mu^{\tilde{u}_{i\alpha}} \right) \quad (227)$$


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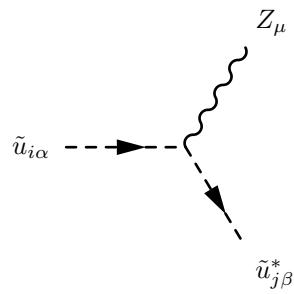
$$-\frac{i}{6}\delta_{\alpha\beta}\left(\left(3g_2\sin\Theta_W + g_1\cos\Theta_W\right)\sum_{a=1}^3 Z_{ia}^{U,*}Z_{ja}^U + 4g_1\cos\Theta_W\sum_{a=1}^3 Z_{i3+a}^{U,*}Z_{j3+a}^U\right)\left(-p_\mu^{\tilde{u}_{j\beta}^*} + p_\mu^{\tilde{u}_{i\alpha}}\right) \quad (228)$$


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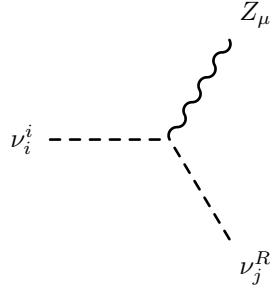
$$-i\frac{1}{\sqrt{2}}g_2\delta_{\alpha\beta}\sum_{a=1}^3 Z_{ia}^{U,*}Z_{ja}^D\left(-p_\mu^{\tilde{d}_{j\beta}^*} + p_\mu^{\tilde{u}_{i\alpha}}\right) \quad (229)$$


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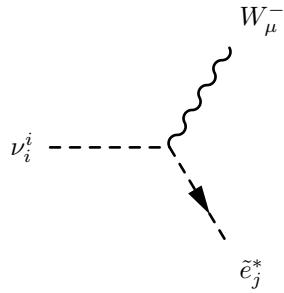
$$-\frac{i}{6}\delta_{\alpha\beta}\left(\left(3g_2\cos\Theta_W - g_1\sin\Theta_W\right)\sum_{a=1}^3 Z_{ia}^{U,*}Z_{ja}^U - 4g_1\sin\Theta_W\sum_{a=1}^3 Z_{i3+a}^{U,*}Z_{j3+a}^U\right)\left(-p_\mu^{\tilde{u}_{j\beta}^*} + p_\mu^{\tilde{u}_{i\alpha}}\right) \quad (230)$$


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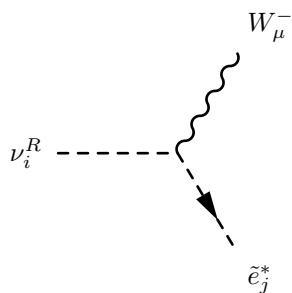
$$\frac{1}{2} \left( g_1 \sin \Theta_W + g_2 \cos \Theta_W \right) \sum_{a=1}^3 Z_{ia}^{i,*} Z_{ja}^{R,*} \left( -p_\mu^{\nu_j^R} + p_\mu^{\nu_i^i} \right) \quad (231)$$


---



$$\frac{1}{2} g_2 \sum_{a=1}^3 Z_{ia}^{i,*} Z_{ja}^E \left( -p_\mu^{\tilde{e}_j^*} + p_\mu^{\nu_i^i} \right) \quad (232)$$

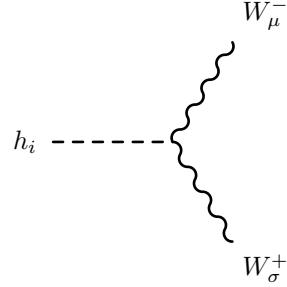

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$$-\frac{i}{2} g_2 \sum_{a=1}^3 Z_{ia}^{R,*} Z_{ja}^E \left( -p_\mu^{\tilde{e}_j^*} + p_\mu^{\nu_i^R} \right) \quad (233)$$

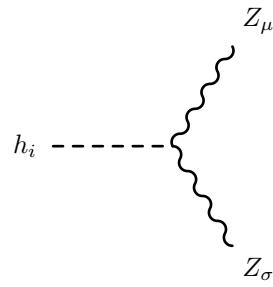

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### 9.3 One Scalar-Two Vector Boson-Interaction



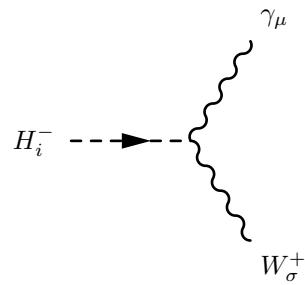
$$\frac{i}{2} g_2^2 \left( v_d Z_{i1}^H + v_u Z_{i2}^H \right) \left( g_{\sigma\mu} \right) \quad (234)$$


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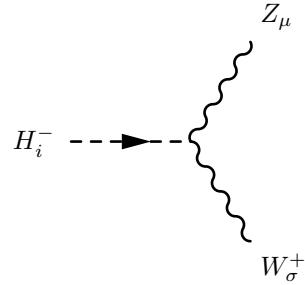
$$\frac{i}{2} \left( g_1 \sin \Theta_W + g_2 \cos \Theta_W \right)^2 \left( v_d Z_{i1}^H + v_u Z_{i2}^H \right) \left( g_{\sigma\mu} \right) \quad (235)$$


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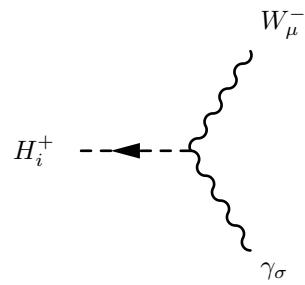
$$-\frac{i}{2} g_1 g_2 \cos \Theta_W \left( v_d Z_{i1}^+ - v_u Z_{i2}^+ \right) \left( g_{\sigma\mu} \right) \quad (236)$$


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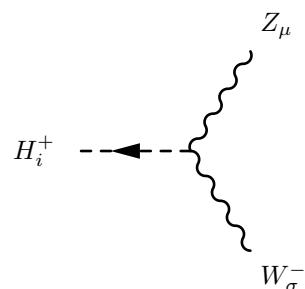
$$\frac{i}{2} g_1 g_2 \sin \Theta_W (v_d Z_{i1}^+ - v_u Z_{i2}^+) (g_{\sigma\mu}) \quad (237)$$


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$$- \frac{i}{2} g_1 g_2 \cos \Theta_W (v_d Z_{i1}^+ - v_u Z_{i2}^+) (g_{\sigma\mu}) \quad (238)$$

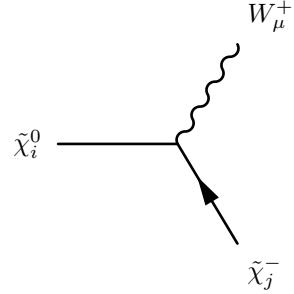

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$$\frac{i}{2} g_1 g_2 \sin \Theta_W (v_d Z_{i1}^+ - v_u Z_{i2}^+) (g_{\sigma\mu}) \quad (239)$$


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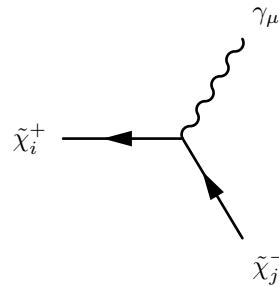
## 9.4 Two Fermion-One Vector Boson-Interaction



$$-\frac{i}{2}g_2 \left( 2U_{j1}^* N_{i2} + \sqrt{2}U_{j2}^* N_{i3} \right) \left( \gamma_\mu \cdot \frac{1 - \gamma_5}{2} \right) \quad (240)$$

$$+ \left( i \frac{1}{\sqrt{2}} g_2 N_{i4}^* V_{j2} - i g_2 N_{i2}^* V_{j1} \right) \left( \gamma_\mu \cdot \frac{1 + \gamma_5}{2} \right) \quad (241)$$

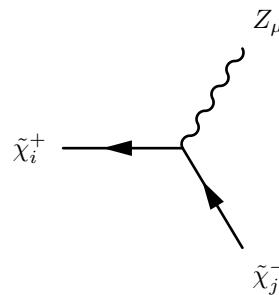

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$$\frac{i}{2} \left( 2g_2 U_{j1}^* \sin \Theta_W U_{i1} + U_{j2}^* \left( g_1 \cos \Theta_W + g_2 \sin \Theta_W \right) U_{i2} \right) \left( \gamma_\mu \cdot \frac{1 - \gamma_5}{2} \right) \quad (242)$$

$$+ \frac{i}{2} \left( 2g_2 V_{i1}^* \sin \Theta_W V_{j1} + V_{i2}^* \left( g_1 \cos \Theta_W + g_2 \sin \Theta_W \right) V_{j2} \right) \left( \gamma_\mu \cdot \frac{1 + \gamma_5}{2} \right) \quad (243)$$

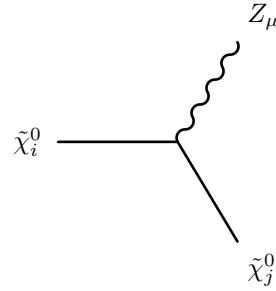

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$$\frac{i}{2} \left( 2g_2 U_{j1}^* \cos \Theta_W U_{i1} + U_{j2}^* \left( -g_1 \sin \Theta_W + g_2 \cos \Theta_W \right) U_{i2} \right) \left( \gamma_\mu \cdot \frac{1 - \gamma_5}{2} \right) \quad (244)$$

$$+ \frac{i}{2} \left( 2g_2 V_{i1}^* \cos \Theta_W V_{j1} + V_{i2}^* \left( -g_1 \sin \Theta_W + g_2 \cos \Theta_W \right) V_{j2} \right) \left( \gamma_\mu \cdot \frac{1 + \gamma_5}{2} \right) \quad (245)$$

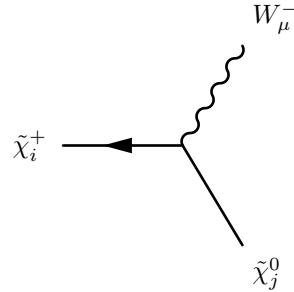

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$$- \frac{i}{2} \left( g_1 \sin \Theta_W + g_2 \cos \Theta_W \right) \left( N_{j3}^* N_{i3} - N_{j4}^* N_{i4} \right) \left( \gamma_\mu \cdot \frac{1 - \gamma_5}{2} \right) \quad (246)$$

$$+ \frac{i}{2} \left( g_1 \sin \Theta_W + g_2 \cos \Theta_W \right) \left( N_{i3}^* N_{j3} - N_{i4}^* N_{j4} \right) \left( \gamma_\mu \cdot \frac{1 + \gamma_5}{2} \right) \quad (247)$$

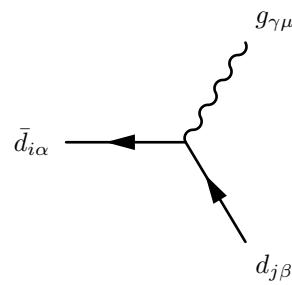

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$$- \frac{i}{2} g_2 \left( 2N_{j2}^* U_{i1} + \sqrt{2} N_{j3}^* U_{i2} \right) \left( \gamma_\mu \cdot \frac{1 - \gamma_5}{2} \right) \quad (248)$$

$$+ \left( i \frac{1}{\sqrt{2}} g_2 V_{i2}^* N_{j4} - i g_2 V_{i1}^* N_{j2} \right) \left( \gamma_\mu \cdot \frac{1 + \gamma_5}{2} \right) \quad (249)$$

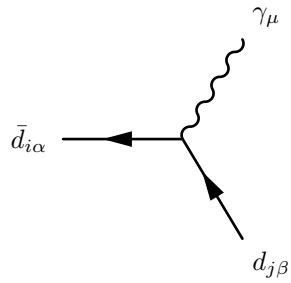

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$$-\frac{i}{2}g_3\delta_{ij}\lambda_{\alpha,\beta}^{\gamma}\left(\gamma_{\mu}\cdot\frac{1-\gamma_5}{2}\right) \quad (250)$$

$$+\frac{i}{2}g_3\delta_{ij}\lambda_{\alpha,\beta}^{\gamma}\left(\gamma_{\mu}\cdot\frac{1+\gamma_5}{2}\right) \quad (251)$$

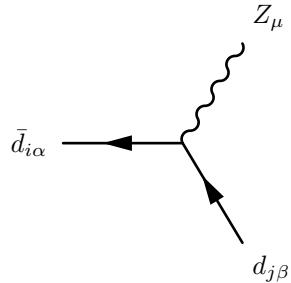

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$$-\frac{i}{6}\delta_{\alpha\beta}\delta_{ij}\left(-3g_2\sin\Theta_W+g_1\cos\Theta_W\right)\left(\gamma_{\mu}\cdot\frac{1-\gamma_5}{2}\right) \quad (252)$$

$$+\frac{i}{3}g_1\cos\Theta_W\delta_{\alpha\beta}\delta_{ij}\left(\gamma_{\mu}\cdot\frac{1+\gamma_5}{2}\right) \quad (253)$$

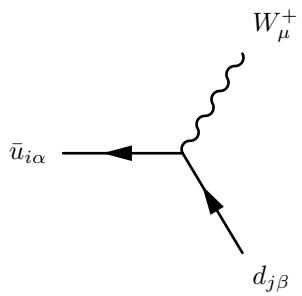

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$$\frac{i}{6}\delta_{\alpha\beta}\delta_{ij}\left(3g_2\cos\Theta_W+g_1\sin\Theta_W\right)\left(\gamma_{\mu}\cdot\frac{1-\gamma_5}{2}\right) \quad (254)$$

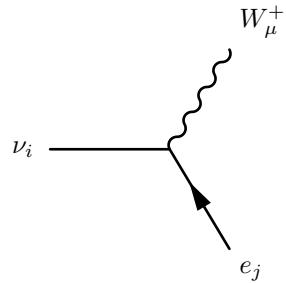
$$+\frac{i}{3}g_1\delta_{\alpha\beta}\delta_{ij}\sin\Theta_W\left(\gamma_{\mu}\cdot\frac{1+\gamma_5}{2}\right) \quad (255)$$


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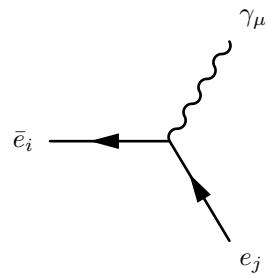
$$- i \frac{1}{\sqrt{2}} g_2 \delta_{\alpha\beta} \sum_{a=1}^3 U_{L,ja}^{d,*} U_{L,ia}^u \left( \gamma_\mu \cdot \frac{1 - \gamma_5}{2} \right) \quad (256)$$


---



$$- i \frac{1}{\sqrt{2}} g_2 \sum_{a=1}^3 U_{L,ja}^{e,*} U_{ia}^V \left( \gamma_\mu \cdot \frac{1 - \gamma_5}{2} \right) \quad (257)$$

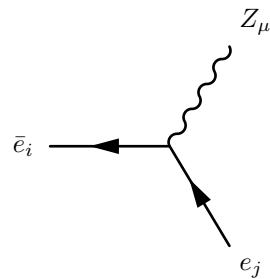

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$$\frac{i}{2} \delta_{ij} \left( g_1 \cos \Theta_W + g_2 \sin \Theta_W \right) \left( \gamma_\mu \cdot \frac{1 - \gamma_5}{2} \right) \quad (258)$$

$$+ i g_1 \cos \Theta_W \delta_{ij} \left( \gamma_\mu \cdot \frac{1 + \gamma_5}{2} \right) \quad (259)$$

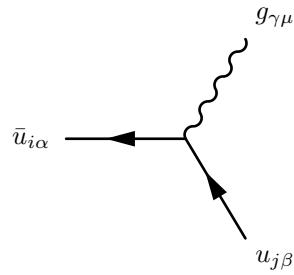

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$$\frac{i}{2} \delta_{ij} \left( -g_1 \sin \Theta_W + g_2 \cos \Theta_W \right) \left( \gamma_\mu \cdot \frac{1 - \gamma_5}{2} \right) \quad (260)$$

$$+ -ig_1 \delta_{ij} \sin \Theta_W \left( \gamma_\mu \cdot \frac{1 + \gamma_5}{2} \right) \quad (261)$$

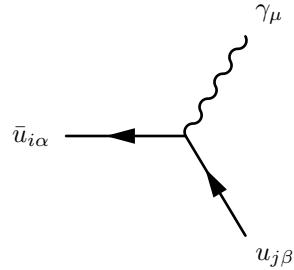

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$$- \frac{i}{2} g_3 \delta_{ij} \lambda_{\alpha,\beta}^\gamma \left( \gamma_\mu \cdot \frac{1 - \gamma_5}{2} \right) \quad (262)$$

$$+ -\frac{i}{2} g_3 \delta_{ij} \lambda_{\alpha,\beta}^\gamma \left( \gamma_\mu \cdot \frac{1 + \gamma_5}{2} \right) \quad (263)$$

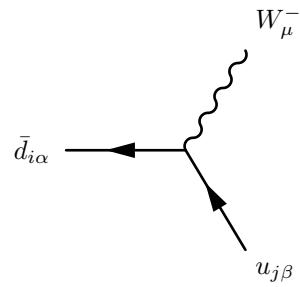

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$$- \frac{i}{6} \delta_{\alpha\beta} \delta_{ij} \left( 3g_2 \sin \Theta_W + g_1 \cos \Theta_W \right) \left( \gamma_\mu \cdot \frac{1 - \gamma_5}{2} \right) \quad (264)$$

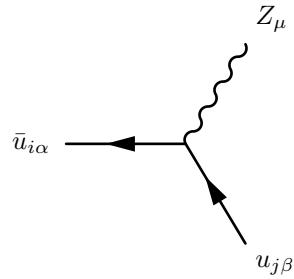
$$+ -\frac{2i}{3} g_1 \cos \Theta_W \delta_{\alpha\beta} \delta_{ij} \left( \gamma_\mu \cdot \frac{1 + \gamma_5}{2} \right) \quad (265)$$


---



$$- i \frac{1}{\sqrt{2}} g_2 \delta_{\alpha\beta} \sum_{a=1}^3 U_{L,ja}^{u,*} U_{L,ia}^d \left( \gamma_\mu \cdot \frac{1 - \gamma_5}{2} \right) \quad (266)$$

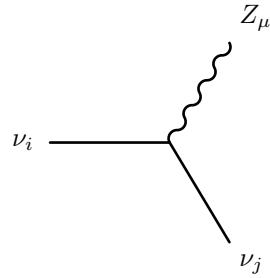

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$$- \frac{i}{6} \delta_{\alpha\beta} \delta_{ij} \left( 3g_2 \cos \Theta_W - g_1 \sin \Theta_W \right) \left( \gamma_\mu \cdot \frac{1 - \gamma_5}{2} \right) \quad (267)$$

$$+ \frac{2i}{3} g_1 \delta_{\alpha\beta} \delta_{ij} \sin \Theta_W \left( \gamma_\mu \cdot \frac{1 + \gamma_5}{2} \right) \quad (268)$$

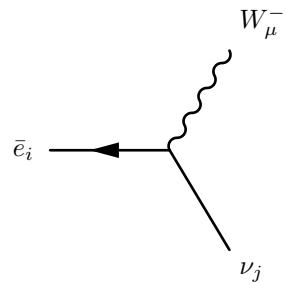

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$$- \frac{i}{2} \delta_{ij} \left( g_1 \sin \Theta_W + g_2 \cos \Theta_W \right) \left( \gamma_\mu \cdot \frac{1 - \gamma_5}{2} \right) \quad (269)$$

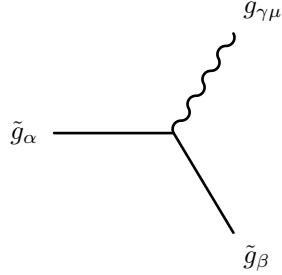
$$+ \frac{i}{2} \delta_{ij} \left( g_1 \sin \Theta_W + g_2 \cos \Theta_W \right) \left( \gamma_\mu \cdot \frac{1 + \gamma_5}{2} \right) \quad (270)$$


---



$$- i \frac{1}{\sqrt{2}} g_2 \sum_{a=1}^3 U_{ja}^{V,*} U_{L,ia}^e \left( \gamma_\mu \cdot \frac{1 - \gamma_5}{2} \right) \quad (271)$$


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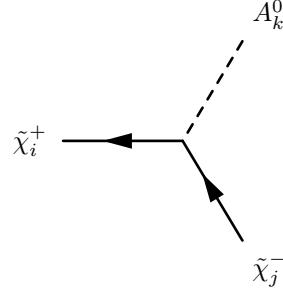


$$- g_3 |\phi_{\tilde{g}}|^2 f_{\alpha,\beta,\gamma} \left( \gamma_\mu \cdot \frac{1 - \gamma_5}{2} \right) \quad (272)$$

$$+ - g_3 |\phi_{\tilde{g}}|^2 f_{\alpha,\beta,\gamma} \left( \gamma_\mu \cdot \frac{1 + \gamma_5}{2} \right) \quad (273)$$


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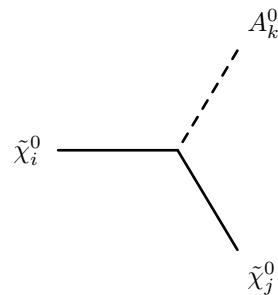
## 9.5 Two Fermion-One Scalar Boson-Interaction



$$- \frac{1}{\sqrt{2}} g_2 \left( U_{j1}^* V_{i2}^* Z_{k2}^A + U_{j2}^* V_{i1}^* Z_{k1}^A \right) \left( \frac{1 - \gamma_5}{2} \right) \quad (274)$$

$$+ \frac{1}{\sqrt{2}} g_2 \left( U_{i1} V_{j2} Z_{k2}^A + U_{i2} V_{j1} Z_{k1}^A \right) \left( \frac{1 + \gamma_5}{2} \right) \quad (275)$$

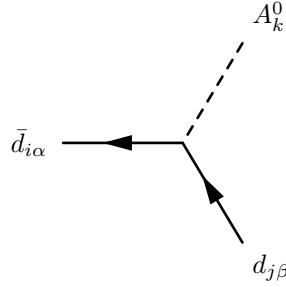

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$$\begin{aligned} & \frac{1}{2} \left( N_{i3}^* \left( g_1 N_{j1}^* - g_2 N_{j2}^* \right) Z_{k1}^A - g_2 N_{i2}^* N_{j3}^* Z_{k1}^A - g_1 N_{i4}^* N_{j1}^* Z_{k2}^A + g_2 N_{i4}^* N_{j2}^* Z_{k2}^A \right. \\ & \left. + g_2 N_{i2}^* N_{j4}^* Z_{k2}^A + g_1 N_{i1}^* \left( N_{j3}^* Z_{k1}^A - N_{j4}^* Z_{k2}^A \right) \right) \left( \frac{1 - \gamma_5}{2} \right) \end{aligned} \quad (276)$$

$$\begin{aligned} & + \frac{1}{2} \left( Z_{k1}^A \left( \left( -g_1 N_{i1} + g_2 N_{i2} \right) N_{j3} + N_{i3} \left( -g_1 N_{j1} + g_2 N_{j2} \right) \right) \right. \\ & \left. + Z_{k2}^A \left( \left( g_1 N_{i1} - g_2 N_{i2} \right) N_{j4} + N_{i4} \left( g_1 N_{j1} - g_2 N_{j2} \right) \right) \right) \left( \frac{1 + \gamma_5}{2} \right) \end{aligned} \quad (277)$$

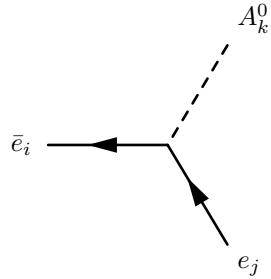

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$$\frac{1}{\sqrt{2}} \delta_{\alpha\beta} \sum_{b=1}^3 U_{L,jb}^{d,*} \sum_{a=1}^3 U_{R,ia}^{d,*} Y_{d,ab} Z_{k1}^A \left( \frac{1 - \gamma_5}{2} \right) \quad (278)$$

$$+ -\frac{1}{\sqrt{2}} \delta_{\alpha\beta} \sum_{b=1}^3 \sum_{a=1}^3 Y_{d,ab}^* U_{R,ja}^d U_{L,ib}^d Z_{k1}^A \left( \frac{1 + \gamma_5}{2} \right) \quad (279)$$

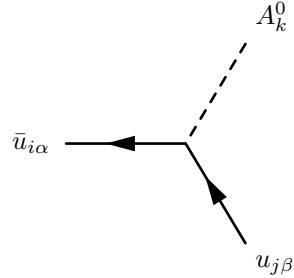

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$$\frac{1}{\sqrt{2}} \sum_{b=1}^3 U_{L,jb}^{e,*} \sum_{a=1}^3 U_{R,ia}^{e,*} Y_{e,ab} Z_{k1}^A \left( \frac{1 - \gamma_5}{2} \right) \quad (280)$$

$$+ -\frac{1}{\sqrt{2}} \sum_{b=1}^3 \sum_{a=1}^3 Y_{e,ab}^* U_{R,ja}^e U_{L,ib}^e Z_{k1}^A \left( \frac{1 + \gamma_5}{2} \right) \quad (281)$$

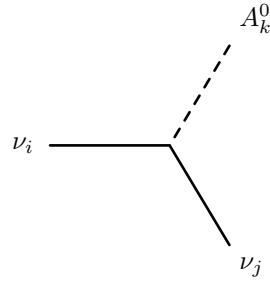

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$$\frac{1}{\sqrt{2}} \delta_{\alpha\beta} \sum_{b=1}^3 U_{L,jb}^{u,*} \sum_{a=1}^3 U_{R,ia}^{u,*} Y_{u,ab} Z_{k2}^A \left( \frac{1 - \gamma_5}{2} \right) \quad (282)$$

$$+ -\frac{1}{\sqrt{2}} \delta_{\alpha\beta} \sum_{b=1}^3 \sum_{a=1}^3 Y_{u,ab}^* U_{R,ja}^u U_{L,ib}^u Z_{k2}^A \left( \frac{1 + \gamma_5}{2} \right) \quad (283)$$

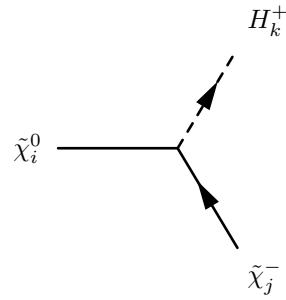

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$$\frac{1}{2} v_u \left( \sum_{b=1}^3 U_{jb}^{V,*} \sum_{a=1}^3 U_{ia}^{V,*} \kappa_{\nu,ab} + \sum_{b=1}^3 U_{ib}^{V,*} \sum_{a=1}^3 U_{ja}^{V,*} \kappa_{\nu,ab} \right) Z_{k2}^A \left( \frac{1 - \gamma_5}{2} \right) \quad (284)$$

$$+ -\frac{1}{2} v_u \left( \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ab}^* U_{ja}^V U_{ib}^V + \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ab}^* U_{ia}^V U_{jb}^V \right) Z_{k2}^A \left( \frac{1 + \gamma_5}{2} \right) \quad (285)$$

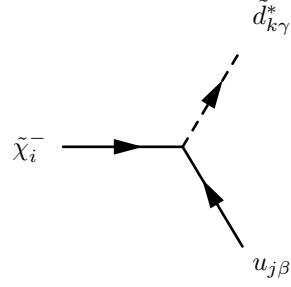

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$$\frac{i}{2} \left( -2g_2 U_{j1}^* N_{i3}^* + \sqrt{2} U_{j2}^* (g_1 N_{i1}^* + g_2 N_{i2}^*) \right) Z_{k1}^+ \left( \frac{1 - \gamma_5}{2} \right) \quad (286)$$

$$+ -\frac{i}{2} \left( 2g_2 V_{j1} N_{i4} + \sqrt{2} V_{j2} (g_1 N_{i1} + g_2 N_{i2}) \right) Z_{k2}^+ \left( \frac{1 + \gamma_5}{2} \right) \quad (287)$$

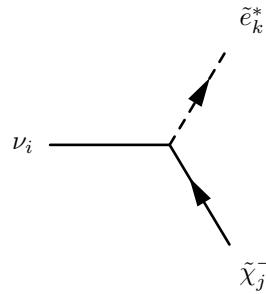

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$$- i\delta_{\beta\gamma} \left( g_2 U_{i1}^* \sum_{a=1}^3 U_{L,ja}^{u,*} Z_{ka}^D - U_{i2}^* \sum_{b=1}^3 U_{L,jb}^{u,*} \sum_{a=1}^3 Y_{d,ab} Z_{k3+a}^D \right) \left( \frac{1 - \gamma_5}{2} \right) \quad (288)$$

$$+ i\delta_{\beta\gamma} \sum_{b=1}^3 \sum_{a=1}^3 Y_{u,ab}^* U_{R,ja}^u Z_{kb}^D V_{i2} \left( \frac{1 + \gamma_5}{2} \right) \quad (289)$$

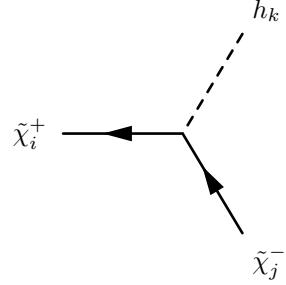

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$$- i \left( g_2 U_{j1}^* \sum_{a=1}^3 U_{ia}^{V,*} Z_{ka}^E - U_{j2}^* \sum_{b=1}^3 U_{ib}^{V,*} \sum_{a=1}^3 Y_{e,ab} Z_{k3+a}^E \right) \left( \frac{1 - \gamma_5}{2} \right) \quad (290)$$

$$+ \frac{i}{2} \frac{1}{\sqrt{2}} v_u \left( \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ab}^* Z_{ka}^E U_{ib}^V + \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ab}^* U_{ia}^V Z_{kb}^E \right) V_{j2} \left( \frac{1 + \gamma_5}{2} \right) \quad (291)$$

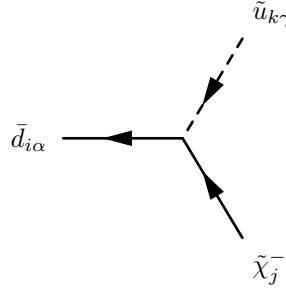

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$$- i \frac{1}{\sqrt{2}} g_2 \left( U_{j1}^* V_{i2}^* Z_{k2}^H + U_{j2}^* V_{i1}^* Z_{k1}^H \right) \left( \frac{1 - \gamma_5}{2} \right) \quad (292)$$

$$+ -i \frac{1}{\sqrt{2}} g_2 \left( U_{i1} V_{j2} Z_{k2}^H + U_{i2} V_{j1} Z_{k1}^H \right) \left( \frac{1 + \gamma_5}{2} \right) \quad (293)$$

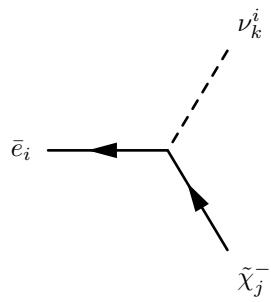

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$$i U_{j2}^* \delta_{\alpha\gamma} \sum_{b=1}^3 Z_{kb}^{U,*} \sum_{a=1}^3 U_{R,ia}^{d,*} Y_{d,ab} \left( \frac{1 - \gamma_5}{2} \right) \quad (294)$$

$$+ -i \delta_{\alpha\gamma} \left( g_2 \sum_{a=1}^3 Z_{ka}^{U,*} U_{L,ia}^d V_{j1} - \sum_{b=1}^3 \sum_{a=1}^3 Y_{u,ab}^* Z_{k3+a}^{U,*} U_{L,ib}^d V_{j2} \right) \left( \frac{1 + \gamma_5}{2} \right) \quad (295)$$

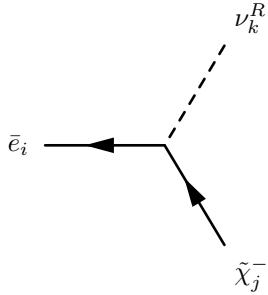

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$$-\frac{1}{\sqrt{2}}U_{j2}^*\sum_{b=1}^3Z_{kb}^{i,*}\sum_{a=1}^3U_{R,ia}^{e,*}Y_{e,ab}\left(\frac{1-\gamma_5}{2}\right) \quad (296)$$

$$+\frac{1}{4}\left(2\sqrt{2}g_2\sum_{a=1}^3Z_{ka}^{i,*}U_{L,ia}^eV_{j1}+v_u\left(\sum_{b=1}^3Z_{kb}^{i,*}\sum_{a=1}^3\kappa_{\nu,ab}^*U_{L,ia}^e+\sum_{b=1}^3\sum_{a=1}^3\kappa_{\nu,ab}^*Z_{ka}^{i,*}U_{L,ib}^e\right)V_{j2}\right)\left(\frac{1+\gamma_5}{2}\right) \quad (297)$$

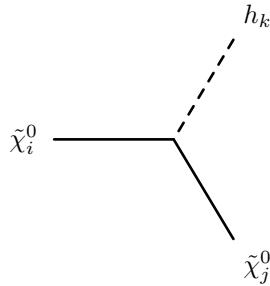

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$$i\frac{1}{\sqrt{2}}U_{j2}^*\sum_{b=1}^3Z_{kb}^{R,*}\sum_{a=1}^3U_{R,ia}^{e,*}Y_{e,ab}\left(\frac{1-\gamma_5}{2}\right) \quad (298)$$

$$+\frac{i}{4}\left(2\sqrt{2}g_2\sum_{a=1}^3Z_{ka}^{R,*}U_{L,ia}^eV_{j1}-v_u\left(\sum_{b=1}^3Z_{kb}^{R,*}\sum_{a=1}^3\kappa_{\nu,ab}^*U_{L,ia}^e+\sum_{b=1}^3\sum_{a=1}^3\kappa_{\nu,ab}^*Z_{ka}^{R,*}U_{L,ib}^e\right)V_{j2}\right)\left(\frac{1+\gamma_5}{2}\right) \quad (299)$$

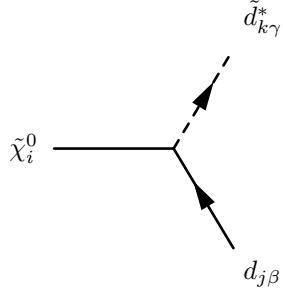

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$$\begin{aligned} &\frac{i}{2}\left(N_{i3}^*\left(g_1N_{j1}^*-g_2N_{j2}^*\right)Z_{k1}^H-g_2N_{i2}^*N_{j3}^*Z_{k1}^H-g_1N_{i4}^*N_{j1}^*Z_{k2}^H+g_2N_{i4}^*N_{j2}^*Z_{k2}^H\right. \\ &+g_2N_{i2}^*N_{j4}^*Z_{k2}^H+g_1N_{i1}^*\left(N_{j3}^*Z_{k1}^H-N_{j4}^*Z_{k2}^H\right)\left.\right)\left(\frac{1-\gamma_5}{2}\right) \end{aligned} \quad (300)$$

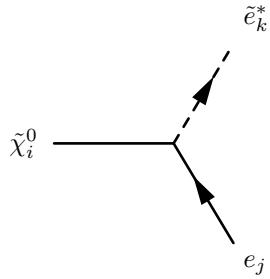
$$\begin{aligned} &+\frac{i}{2}\left(Z_{k1}^H\left(\left(g_1N_{i1}-g_2N_{i2}\right)N_{j3}+N_{i3}\left(g_1N_{j1}-g_2N_{j2}\right)\right)\right. \\ &+Z_{k2}^H\left(\left(-g_1N_{i1}+g_2N_{i2}\right)N_{j4}+N_{i4}\left(-g_1N_{j1}+g_2N_{j2}\right)\right)\left.\right)\left(\frac{1+\gamma_5}{2}\right) \end{aligned} \quad (301)$$


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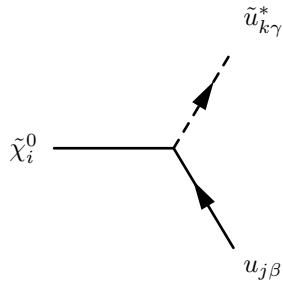
$$-\frac{i}{6}\delta_{\beta\gamma}\left(-3\sqrt{2}g_2N_{i2}^*\sum_{a=1}^3U_{L,ja}^{d,*}Z_{ka}^D+6N_{i3}^*\sum_{b=1}^3U_{L,jb}^{d,*}\sum_{a=1}^3Y_{d,ab}Z_{k3+a}^D+\sqrt{2}g_1N_{i1}^*\sum_{a=1}^3U_{L,ja}^{d,*}Z_{ka}^D\right)\left(\frac{1-\gamma_5}{2}\right) \quad (302)$$

$$+\frac{i}{3}\delta_{\beta\gamma}\left(3\sum_{b=1}^3\sum_{a=1}^3Y_{d,ab}^*U_{R,ja}^dZ_{kb}^DN_{i3}+\sqrt{2}g_1\sum_{a=1}^3Z_{k3+a}^DU_{R,ja}^dN_{i1}\right)\left(\frac{1+\gamma_5}{2}\right) \quad (303)$$



$$\frac{i}{2}\left(-2N_{i3}^*\sum_{b=1}^3U_{L,jb}^{e,*}\sum_{a=1}^3Y_{e,ab}Z_{k3+a}^E+\sqrt{2}g_1N_{i1}^*\sum_{a=1}^3U_{L,ja}^{e,*}Z_{ka}^E+\sqrt{2}g_2N_{i2}^*\sum_{a=1}^3U_{L,ja}^{e,*}Z_{ka}^E\right)\left(\frac{1-\gamma_5}{2}\right) \quad (304)$$

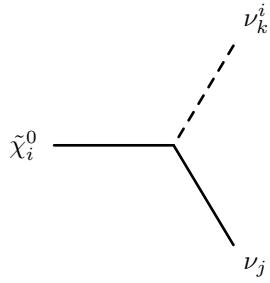
$$+ -i\left(\sqrt{2}g_1\sum_{a=1}^3Z_{k3+a}^EU_{R,ja}^eN_{i1}+\sum_{b=1}^3\sum_{a=1}^3Y_{e,ab}^*U_{R,ja}^eZ_{kb}^EN_{i3}\right)\left(\frac{1+\gamma_5}{2}\right) \quad (305)$$



$$-\frac{i}{6}\delta_{\beta\gamma}\left(3\sqrt{2}g_2N_{i2}^*\sum_{a=1}^3U_{L,ja}^{u,*}Z_{ka}^U+6N_{i4}^*\sum_{b=1}^3U_{L,jb}^{u,*}\sum_{a=1}^3Y_{u,ab}Z_{k3+a}^U+\sqrt{2}g_1N_{i1}^*\sum_{a=1}^3U_{L,ja}^{u,*}Z_{ka}^U\right)\left(\frac{1-\gamma_5}{2}\right) \quad (306)$$

$$+\frac{i}{3}\delta_{\beta\gamma}\left(2\sqrt{2}g_1\sum_{a=1}^3Z_{k3+a}^UU_{R,ja}^uN_{i1}-3\sum_{b=1}^3\sum_{a=1}^3Y_{u,ab}^*U_{R,ja}^uZ_{kb}^UN_{i4}\right)\left(\frac{1+\gamma_5}{2}\right) \quad (307)$$

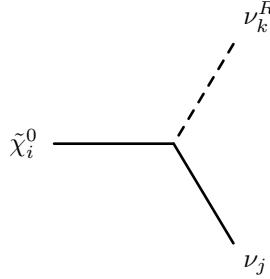

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$$\begin{aligned} & \frac{1}{2}\left(g_1N_{i1}^*\sum_{a=1}^3U_{ja}^{V,*}Z_{ka}^{i,*}-g_2N_{i2}^*\sum_{a=1}^3U_{ja}^{V,*}Z_{ka}^{i,*}\right. \\ & +v_uN_{i4}^*\left(\sum_{b=1}^3Z_{kb}^{i,*}\sum_{a=1}^3U_{ja}^{V,*}\kappa_{\nu,ab}+\sum_{b=1}^3U_{jb}^{V,*}\sum_{a=1}^3Z_{ka}^{i,*}\kappa_{\nu,ab}\right)\left.\right)\left(\frac{1-\gamma_5}{2}\right) \end{aligned} \quad (308)$$

$$\begin{aligned} & +\frac{1}{2}\left(\sum_{a=1}^3Z_{ka}^{i,*}U_{ja}^V\left(-g_1N_{i1}+g_2N_{i2}\right)\right. \\ & -v_u\left(\sum_{b=1}^3Z_{kb}^{i,*}\sum_{a=1}^3\kappa_{\nu,ab}^*U_{ja}^V+\sum_{b=1}^3\sum_{a=1}^3\kappa_{\nu,ab}^*Z_{ka}^{i,*}U_{jb}^V\right)N_{i4}\left.\right)\left(\frac{1+\gamma_5}{2}\right) \end{aligned} \quad (309)$$


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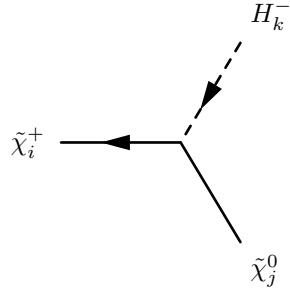


$$\begin{aligned} & \frac{i}{2}\left(g_1N_{i1}^*\sum_{a=1}^3U_{ja}^{V,*}Z_{ka}^{R,*}-g_2N_{i2}^*\sum_{a=1}^3U_{ja}^{V,*}Z_{ka}^{R,*}\right. \\ & \left.\right) \end{aligned}$$

$$-v_u N_{i4}^* \left( \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 U_{ja}^{V,*} \kappa_{\nu,ab} + \sum_{b=1}^3 U_{jb}^{V,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \right) \left( \frac{1-\gamma_5}{2} \right) \quad (310)$$

$$\begin{aligned} &+ \frac{i}{2} \left( \sum_{a=1}^3 Z_{ka}^{R,*} U_{ja}^V (g_1 N_{i1} - g_2 N_{i2}) \right. \\ &\left. - v_u \left( \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ab}^* U_{ja}^V + \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ab}^* Z_{ka}^{R,*} U_{jb}^V \right) N_{i4} \right) \left( \frac{1+\gamma_5}{2} \right) \end{aligned} \quad (311)$$

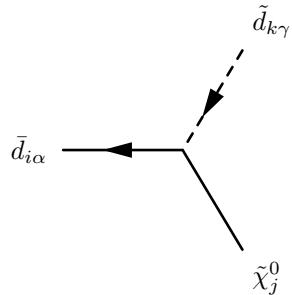

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$$- \frac{i}{2} \left( 2g_2 V_{i1}^* N_{j4}^* + \sqrt{2} V_{i2}^* (g_1 N_{j1}^* + g_2 N_{j2}^*) \right) Z_{k2}^+ \left( \frac{1-\gamma_5}{2} \right) \quad (312)$$

$$+ \frac{i}{2} \left( -2g_2 U_{i1} N_{j3} + \sqrt{2} U_{i2} (g_1 N_{j1} + g_2 N_{j2}) \right) Z_{k1}^+ \left( \frac{1+\gamma_5}{2} \right) \quad (313)$$

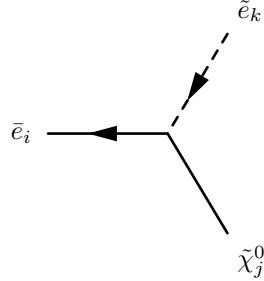

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$$- \frac{i}{3} \delta_{\alpha\gamma} \left( 3N_{j3}^* \sum_{b=1}^3 Z_{kb}^{D,*} \sum_{a=1}^3 U_{R,ia}^{d,*} Y_{d,ab} + \sqrt{2} g_1 N_{j1}^* \sum_{a=1}^3 Z_{k3+a}^{D,*} U_{R,ia}^{d,*} \right) \left( \frac{1-\gamma_5}{2} \right) \quad (314)$$

$$+ - \frac{i}{6} \delta_{\alpha\gamma} \left( 6 \sum_{b=1}^3 \sum_{a=1}^3 Y_{d,ab}^* Z_{k3+a}^{D,*} U_{L,ib}^d N_{j3} + \sqrt{2} \sum_{a=1}^3 Z_{ka}^{D,*} U_{L,ia}^d (-3g_2 N_{j2} + g_1 N_{j1}) \right) \left( \frac{1+\gamma_5}{2} \right) \quad (315)$$

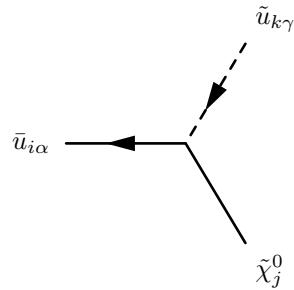

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$$-i\left(N_{j3}^* \sum_{b=1}^3 Z_{kb}^{E,*} \sum_{a=1}^3 U_{R,ia}^{e,*} Y_{e,ab} + \sqrt{2}g_1 N_{j1}^* \sum_{a=1}^3 Z_{k3+a}^{E,*} U_{R,ia}^{e,*}\right) \left(\frac{1-\gamma_5}{2}\right) \quad (316)$$

$$+ \frac{i}{2} \left( -2 \sum_{b=1}^3 \sum_{a=1}^3 Y_{e,ab}^* Z_{k3+a}^{E,*} U_{L,ib}^e N_{j3} + \sqrt{2} \sum_{a=1}^3 Z_{ka}^{E,*} U_{L,ia}^e (g_1 N_{j1} + g_2 N_{j2}) \right) \left(\frac{1+\gamma_5}{2}\right) \quad (317)$$

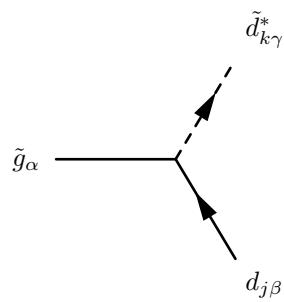

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$$\frac{i}{3} \delta_{\alpha\gamma} \left( 2\sqrt{2}g_1 N_{j1}^* \sum_{a=1}^3 Z_{k3+a}^{U,*} U_{R,ia}^{u,*} - 3N_{j4}^* \sum_{b=1}^3 Z_{kb}^{U,*} \sum_{a=1}^3 U_{R,ia}^{u,*} Y_{u,ab} \right) \left(\frac{1-\gamma_5}{2}\right) \quad (318)$$

$$+ -\frac{i}{6} \delta_{\alpha\gamma} \left( 6 \sum_{b=1}^3 \sum_{a=1}^3 Y_{u,ab}^* Z_{k3+a}^{U,*} U_{L,ib}^u N_{j4} + \sqrt{2} \sum_{a=1}^3 Z_{ka}^{U,*} U_{L,ia}^u (3g_2 N_{j2} + g_1 N_{j1}) \right) \left(\frac{1+\gamma_5}{2}\right) \quad (319)$$

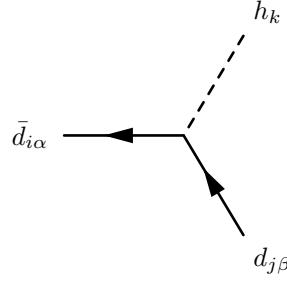

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$$- i \frac{1}{\sqrt{2}} g_3 \phi_{\tilde{g}} \lambda_{\gamma, \beta}^{\alpha} \sum_{a=1}^3 U_{L,ja}^{d,*} Z_{ka}^D \left( \frac{1 - \gamma_5}{2} \right) \quad (320)$$

$$+ i \frac{1}{\sqrt{2}} g_3 \phi_{\tilde{g}}^* \lambda_{\gamma, \beta}^{\alpha} \sum_{a=1}^3 Z_{k3+a}^D U_{R,ja}^d \left( \frac{1 + \gamma_5}{2} \right) \quad (321)$$

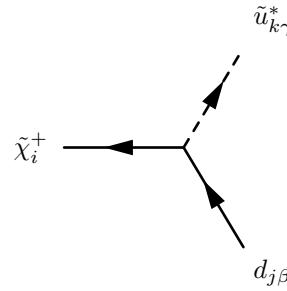

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$$- i \frac{1}{\sqrt{2}} \delta_{\alpha\beta} \sum_{b=1}^3 U_{L,jb}^{d,*} \sum_{a=1}^3 U_{R,ia}^{d,*} Y_{d,ab} Z_{k1}^H \left( \frac{1 - \gamma_5}{2} \right) \quad (322)$$

$$+ -i \frac{1}{\sqrt{2}} \delta_{\alpha\beta} \sum_{b=1}^3 \sum_{a=1}^3 Y_{d,ab}^* U_{R,ja}^d U_{L,ib}^d Z_{k1}^H \left( \frac{1 + \gamma_5}{2} \right) \quad (323)$$

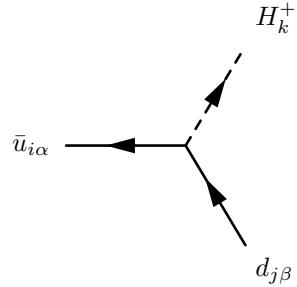

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$$- i \delta_{\beta\gamma} \left( g_2 V_{i1}^* \sum_{a=1}^3 U_{L,ja}^{d,*} Z_{ka}^U - V_{i2}^* \sum_{b=1}^3 U_{L,jb}^{d,*} \sum_{a=1}^3 Y_{u,ab} Z_{k3+a}^U \right) \left( \frac{1 - \gamma_5}{2} \right) \quad (324)$$

$$+ i \delta_{\beta\gamma} \sum_{b=1}^3 \sum_{a=1}^3 Y_{d,ab}^* U_{R,ja}^d Z_{kb}^U U_{i2} \left( \frac{1 + \gamma_5}{2} \right) \quad (325)$$

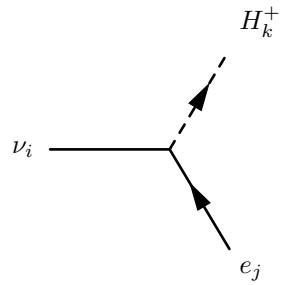

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$$i\delta_{\alpha\beta} \sum_{b=1}^3 U_{L,jb}^{d,*} \sum_{a=1}^3 U_{R,ia}^{u,*} Y_{u,ab} Z_{k2}^+ \left( \frac{1 - \gamma_5}{2} \right) \quad (326)$$

$$+ i\delta_{\alpha\beta} \sum_{b=1}^3 \sum_{a=1}^3 Y_{d,ab}^* U_{R,ja}^d U_{L,ib}^u Z_{k1}^+ \left( \frac{1 + \gamma_5}{2} \right) \quad (327)$$

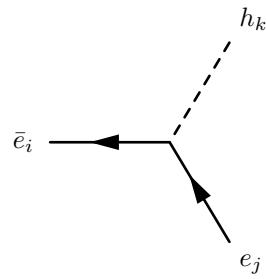

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$$\frac{i}{2} \frac{1}{\sqrt{2}} v_u \left( \sum_{b=1}^3 U_{L,jb}^{e,*} \sum_{a=1}^3 U_{ia}^{V,*} \kappa_{\nu,ab} + \sum_{b=1}^3 U_{ib}^{V,*} \sum_{a=1}^3 U_{L,ja}^{e,*} \kappa_{\nu,ab} \right) Z_{k2}^+ \left( \frac{1 - \gamma_5}{2} \right) \quad (328)$$

$$+ i \sum_{b=1}^3 \sum_{a=1}^3 Y_{e,ab}^* U_{R,ja}^e U_{ib}^V Z_{k1}^+ \left( \frac{1 + \gamma_5}{2} \right) \quad (329)$$

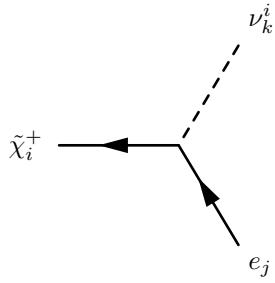

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$$-i\frac{1}{\sqrt{2}}\sum_{b=1}^3 U_{L,jb}^{e,*}\sum_{a=1}^3 U_{R,ia}^{e,*}Y_{e,ab}Z_{k1}^H\left(\frac{1-\gamma_5}{2}\right) \quad (330)$$

$$+ -i\frac{1}{\sqrt{2}}\sum_{b=1}^3 \sum_{a=1}^3 Y_{e,ab}^*U_{R,ja}^eU_{L,ib}^eZ_{k1}^H\left(\frac{1+\gamma_5}{2}\right) \quad (331)$$

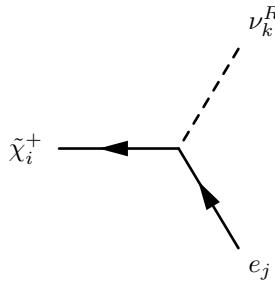

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$$\begin{aligned} & \frac{1}{4} \left( -2\sqrt{2}g_2 V_{i1}^* \sum_{a=1}^3 U_{L,ja}^{e,*} Z_{ka}^{i,*} \right. \\ & \left. - v_u V_{i2}^* \left( \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 U_{L,ja}^{e,*} \kappa_{\nu,ab} + \sum_{b=1}^3 U_{L,jb}^{e,*} \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,ab} \right) \right) \left( \frac{1-\gamma_5}{2} \right) \end{aligned} \quad (332)$$

$$+ \frac{1}{\sqrt{2}} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{e,ab}^* U_{R,ja}^e U_{i2} \left( \frac{1+\gamma_5}{2} \right) \quad (333)$$

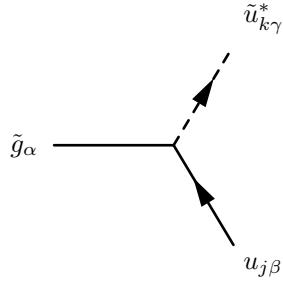

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$$\begin{aligned} & -\frac{i}{4} \left( 2\sqrt{2}g_2 V_{i1}^* \sum_{a=1}^3 U_{L,ja}^{e,*} Z_{ka}^{R,*} \right. \\ & \left. - v_u V_{i2}^* \left( \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 U_{L,ja}^{e,*} \kappa_{\nu,ab} + \sum_{b=1}^3 U_{L,jb}^{e,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \right) \right) \left( \frac{1-\gamma_5}{2} \right) \end{aligned} \quad (334)$$

$$+ i \frac{1}{\sqrt{2}} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{e,ab}^* U_{R,ja}^e U_{i2} \left( \frac{1+\gamma_5}{2} \right) \quad (335)$$

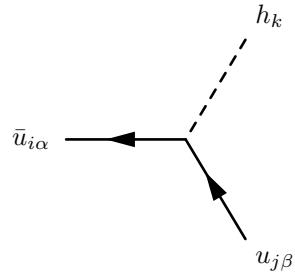

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$$- i \frac{1}{\sqrt{2}} g_3 \phi_{\tilde{g}} \lambda_{\gamma,\beta}^\alpha \sum_{a=1}^3 U_{L,ja}^{u,*} Z_{ka}^U \left( \frac{1-\gamma_5}{2} \right) \quad (336)$$

$$+ i \frac{1}{\sqrt{2}} g_3 \phi_{\tilde{g}}^* \lambda_{\gamma,\beta}^\alpha \sum_{a=1}^3 Z_{k3+a}^U U_{R,ja}^u \left( \frac{1+\gamma_5}{2} \right) \quad (337)$$

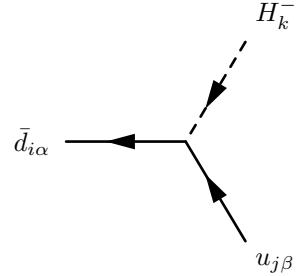

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$$- i \frac{1}{\sqrt{2}} \delta_{\alpha\beta} \sum_{b=1}^3 U_{L,jb}^{u,*} \sum_{a=1}^3 U_{R,ia}^{u,*} Y_{u,ab} Z_{k2}^H \left( \frac{1-\gamma_5}{2} \right) \quad (338)$$

$$+ -i \frac{1}{\sqrt{2}} \delta_{\alpha\beta} \sum_{b=1}^3 \sum_{a=1}^3 Y_{u,ab}^* U_{R,ja}^u U_{L,ib}^u Z_{k2}^H \left( \frac{1+\gamma_5}{2} \right) \quad (339)$$

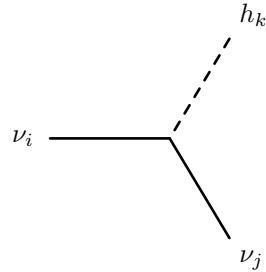

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$$i\delta_{\alpha\beta} \sum_{b=1}^3 U_{L,jb}^{u,*} \sum_{a=1}^3 U_{R,ia}^{d,*} Y_{d,ab} Z_{k1}^+ \left( \frac{1 - \gamma_5}{2} \right) \quad (340)$$

$$+ i\delta_{\alpha\beta} \sum_{b=1}^3 \sum_{a=1}^3 Y_{u,ab}^* U_{R,ja}^u U_{L,ib}^d Z_{k2}^+ \left( \frac{1 + \gamma_5}{2} \right) \quad (341)$$

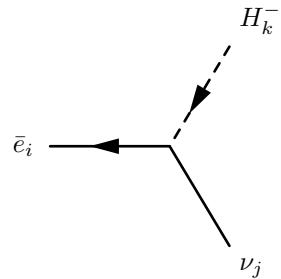

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$$- \frac{i}{2} v_u \left( \sum_{b=1}^3 U_{jb}^{V,*} \sum_{a=1}^3 U_{ia}^{V,*} \kappa_{\nu,ab} + \sum_{b=1}^3 U_{ib}^{V,*} \sum_{a=1}^3 U_{ja}^{V,*} \kappa_{\nu,ab} \right) Z_{k2}^H \left( \frac{1 - \gamma_5}{2} \right) \quad (342)$$

$$+ - \frac{i}{2} v_u \left( \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ab}^* U_{ja}^V U_{ib}^V + \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ab}^* U_{ia}^V U_{jb}^V \right) Z_{k2}^H \left( \frac{1 + \gamma_5}{2} \right) \quad (343)$$

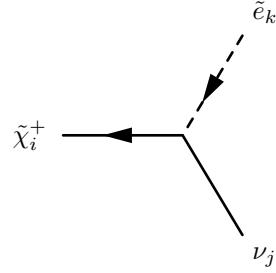

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$$i \sum_{b=1}^3 U_{jb}^{V,*} \sum_{a=1}^3 U_{R,ia}^{e,*} Y_{e,ab} Z_{k1}^+ \left( \frac{1 - \gamma_5}{2} \right) \quad (344)$$

$$+ \frac{i}{2} \frac{1}{\sqrt{2}} v_u \left( \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ab}^* U_{L,ia}^e U_{jb}^V + \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ab}^* U_{ja}^V U_{L,ib}^e \right) Z_{k2}^+ \left( \frac{1 + \gamma_5}{2} \right) \quad (345)$$

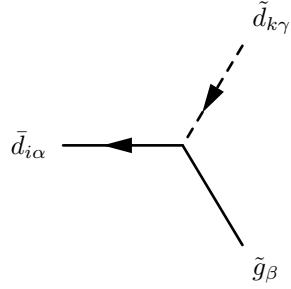

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$$\frac{i}{2} \frac{1}{\sqrt{2}} v_u V_{i2}^* \left( \sum_{b=1}^3 Z_{kb}^{E,*} \sum_{a=1}^3 U_{ja}^{V,*} \kappa_{\nu,ab} + \sum_{b=1}^3 U_{jb}^{V,*} \sum_{a=1}^3 Z_{ka}^{E,*} \kappa_{\nu,ab} \right) \left( \frac{1 - \gamma_5}{2} \right) \quad (346)$$

$$+ -i \left( g_2 \sum_{a=1}^3 Z_{ka}^{E,*} U_{ja}^V U_{i1} - \sum_{b=1}^3 \sum_{a=1}^3 Y_{e,ab}^* Z_{k3+a}^{E,*} U_{jb}^V U_{i2} \right) \left( \frac{1 + \gamma_5}{2} \right) \quad (347)$$

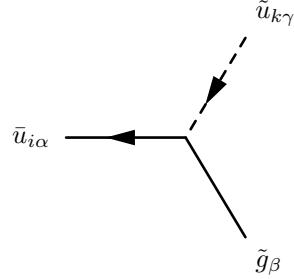

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$$i \frac{1}{\sqrt{2}} g_3 \phi_{\tilde{g}} \lambda_{\alpha,\gamma}^\beta \sum_{a=1}^3 Z_{k3+a}^{D,*} U_{R,ia}^{d,*} \left( \frac{1 - \gamma_5}{2} \right) \quad (348)$$

$$+ -i \frac{1}{\sqrt{2}} g_3 \phi_{\tilde{g}}^* \lambda_{\alpha,\gamma}^\beta \sum_{a=1}^3 Z_{ka}^{D,*} U_{L,ia}^d \left( \frac{1 + \gamma_5}{2} \right) \quad (349)$$

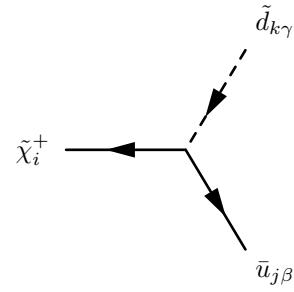

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$$i \frac{1}{\sqrt{2}} g_3 \phi_{\tilde{g}} \lambda_{\alpha,\gamma}^\beta \sum_{a=1}^3 Z_{k3+a}^{U,*} U_{R,ia}^u \left( \frac{1 - \gamma_5}{2} \right) \quad (350)$$

$$+ -i \frac{1}{\sqrt{2}} g_3 \phi_{\tilde{g}}^* \lambda_{\alpha,\gamma}^\beta \sum_{a=1}^3 Z_{ka}^{U,*} U_{L,ia}^u \left( \frac{1 + \gamma_5}{2} \right) \quad (351)$$


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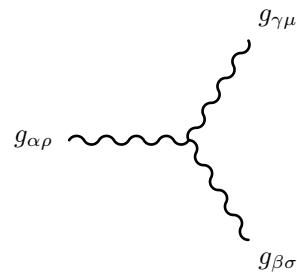


$$i V_{i2}^* \delta_{\beta\gamma} \sum_{b=1}^3 Z_{kb}^{D,*} \sum_{a=1}^3 U_{R,ja}^{u,*} Y_{u,ab} \left( \frac{1 - \gamma_5}{2} \right) \quad (352)$$

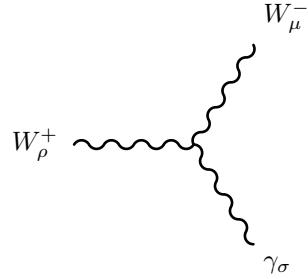
$$+ -i \delta_{\beta\gamma} \left( g_2 \sum_{a=1}^3 Z_{ka}^{D,*} U_{L,ja}^u U_{i1} - \sum_{b=1}^3 \sum_{a=1}^3 Y_{d,ab}^* Z_{k3+a}^{D,*} U_{L,jb}^u U_{i2} \right) \left( \frac{1 + \gamma_5}{2} \right) \quad (353)$$


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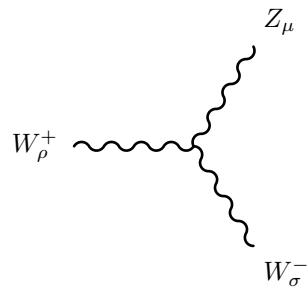
## 9.6 Three Vector Boson-Interaction



$$g_3 f_{\alpha,\beta,\gamma} \left( g_{\rho\mu} \left( -p_\sigma^{g_{\gamma\mu}} + p_\sigma^{g_{\alpha\rho}} \right) + g_{\rho\sigma} \left( -p_\mu^{g_{\alpha\rho}} + p_\mu^{g_{\beta\sigma}} \right) + g_{\sigma\mu} \left( -p_\rho^{g_{\beta\sigma}} + p_\rho^{g_{\gamma\mu}} \right) \right) \quad (354)$$

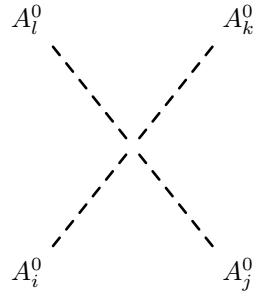


$$ig_2 \sin \Theta_W \left( g_{\rho\mu} \left( -p_\sigma^{W_\mu^-} + p_\sigma^{W_\rho^+} \right) + g_{\rho\sigma} \left( -p_\mu^{W_\rho^+} + p_\mu^{\gamma_\sigma} \right) + g_{\sigma\mu} \left( -p_\rho^{\gamma_\sigma} + p_\rho^{W_\mu^-} \right) \right) \quad (355)$$



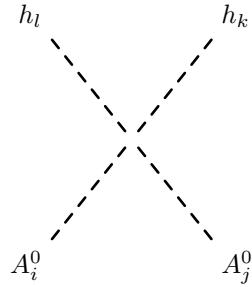
$$-ig_2 \cos \Theta_W \left( g_{\rho\mu} \left( -p_\sigma^{Z_\mu} + p_\sigma^{W_\rho^+} \right) + g_{\rho\sigma} \left( -p_\mu^{W_\rho^+} + p_\mu^{W_\sigma^-} \right) + g_{\sigma\mu} \left( -p_\rho^{W_\sigma^-} + p_\rho^{Z_\mu} \right) \right) \quad (356)$$

## 9.7 Four Scalar-Interaction



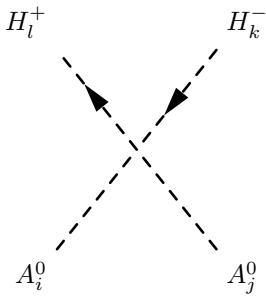
$$\begin{aligned} & \frac{i}{4} \left( g_1^2 + g_2^2 \right) \left( Z_{i2}^A \left( Z_{j1}^A \left( Z_{k1}^A Z_{l2}^A + Z_{k2}^A Z_{l1}^A \right) + Z_{j2}^A \left( -3Z_{k2}^A Z_{l2}^A + Z_{k1}^A Z_{l1}^A \right) \right) \right. \\ & \left. + Z_{i1}^A \left( Z_{j1}^A \left( -3Z_{k1}^A Z_{l1}^A + Z_{k2}^A Z_{l2}^A \right) + Z_{j2}^A \left( Z_{k1}^A Z_{l2}^A + Z_{k2}^A Z_{l1}^A \right) \right) \right) \end{aligned} \quad (357)$$


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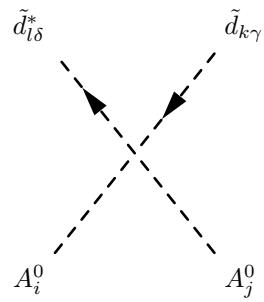
$$- \frac{i}{4} \left( g_1^2 + g_2^2 \right) \left( Z_{i1}^A Z_{j1}^A - Z_{i2}^A Z_{j2}^A \right) \left( Z_{k1}^H Z_{l1}^H - Z_{k2}^H Z_{l2}^H \right) \quad (358)$$


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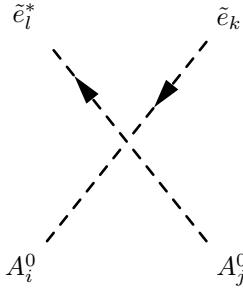
$$\begin{aligned} & \frac{i}{4} \left( Z_{i1}^A \left( g_2^2 Z_{j2}^A \left( Z_{k1}^+ Z_{l2}^+ + Z_{k2}^+ Z_{l1}^+ \right) - Z_{j1}^A \left( \left( g_1^2 + g_2^2 \right) Z_{k1}^+ Z_{l1}^+ + \left( -g_1^2 + g_2^2 \right) Z_{k2}^+ Z_{l2}^+ \right) \right) \right. \\ & \left. + Z_{i2}^A \left( g_2^2 Z_{j1}^A \left( Z_{k1}^+ Z_{l2}^+ + Z_{k2}^+ Z_{l1}^+ \right) + Z_{j2}^A \left( - \left( g_1^2 + g_2^2 \right) Z_{k2}^+ Z_{l2}^+ + \left( -g_2^2 + g_1^2 \right) Z_{k1}^+ Z_{l1}^+ \right) \right) \right) \end{aligned} \quad (359)$$


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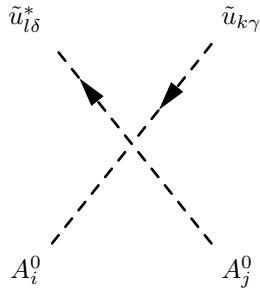
$$\begin{aligned}
& \frac{i}{12} \delta_{\gamma\delta} \left( \left( 3g_2^2 + g_1^2 \right) \sum_{a=1}^3 Z_{ka}^{D,*} Z_{la}^D \left( Z_{i1}^A Z_{j1}^A - Z_{i2}^A Z_{j2}^A \right) \right. \\
& + 2 \left( -6 \left( \sum_{c=1}^3 Z_{k3+c}^{D,*} \sum_{b=1}^3 \sum_{a=1}^3 Y_{d,ca}^* Y_{d,ba} Z_{l3+b}^D + \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{D,*} \sum_{a=1}^3 Y_{d,ac}^* Y_{d,ab} Z_{lc}^D \right) Z_{i1}^A Z_{j1}^A \right. \\
& \left. \left. + g_1^2 \sum_{a=1}^3 Z_{k3+a}^{D,*} Z_{l3+a}^D \left( Z_{i1}^A Z_{j1}^A - Z_{i2}^A Z_{j2}^A \right) \right) \right) \tag{360}
\end{aligned}$$


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$$\begin{aligned}
& - \frac{i}{4} \left( 4 \left( \sum_{c=1}^3 Z_{k3+c}^{E,*} \sum_{b=1}^3 \sum_{a=1}^3 Y_{e,ca}^* Y_{e,ba} Z_{l3+b}^E + \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{E,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{e,ab} Z_{lc}^E \right) Z_{i1}^A Z_{j1}^A \right. \\
& + \left( -g_2^2 + g_1^2 \right) \sum_{a=1}^3 Z_{ka}^{E,*} Z_{la}^E \left( Z_{i1}^A Z_{j1}^A - Z_{i2}^A Z_{j2}^A \right) \\
& \left. + 2g_1^2 \sum_{a=1}^3 Z_{k3+a}^{E,*} Z_{l3+a}^E \left( -Z_{i1}^A Z_{j1}^A + Z_{i2}^A Z_{j2}^A \right) \right) \tag{361}
\end{aligned}$$

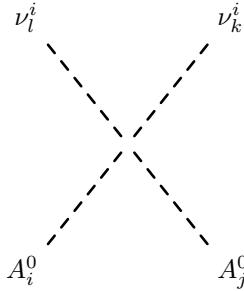

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$$\frac{i}{12} \delta_{\gamma\delta} \left( \left( -3g_2^2 + g_1^2 \right) \sum_{a=1}^3 Z_{ka}^{U,*} Z_{la}^U \left( Z_{i1}^A Z_{j1}^A - Z_{i2}^A Z_{j2}^A \right) \right)$$

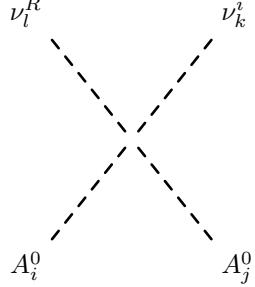
$$\begin{aligned}
& -4 \left( 3 \left( \sum_{c=1}^3 Z_{k3+c}^{U,*} \sum_{b=1}^3 \sum_{a=1}^3 Y_{u,ca}^* Y_{u,ba} Z_{l3+b}^U + \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{U,*} \sum_{a=1}^3 Y_{u,ac}^* Y_{u,ab} Z_{lc}^U \right) Z_{i2}^A Z_{j2}^A \right. \\
& \left. + g_1^2 \sum_{a=1}^3 Z_{k3+a}^{U,*} Z_{l3+a}^U \left( Z_{i1}^A Z_{j1}^A - Z_{i2}^A Z_{j2}^A \right) \right) \quad (362)
\end{aligned}$$


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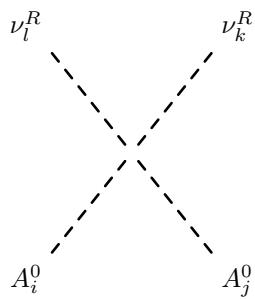


$$\begin{aligned}
& -\frac{i}{16} \left( \left( 4 \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab}^* + 4 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{la}^{i,*} Q_{\nu,ab}^* + 4 \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab} \right. \right. \\
& + 4 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{la}^{i,*} Q_{\nu,ab} + v_u^2 \sum_{c=1}^3 Z_{lc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} + v_u^2 \sum_{c=1}^3 Z_{lc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} + v_u^2 \sum_{c=1}^3 Z_{lc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} + v_u^2 \sum_{c=1}^3 Z_{lc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} \\
& \left. \left. + v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} + 8 \sum_{c=1}^3 Z_{lc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} \right. \right. \\
& + 8 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} \Big) Z_{i2}^A Z_{j2}^A \\
& \left. + 4 \left( g_1^2 + g_2^2 \right) \sum_{a=1}^3 Z_{ka}^{i,*} Z_{la}^{i,*} \left( Z_{i1}^A Z_{j1}^A - Z_{i2}^A Z_{j2}^A \right) \right) \quad (363)
\end{aligned}$$


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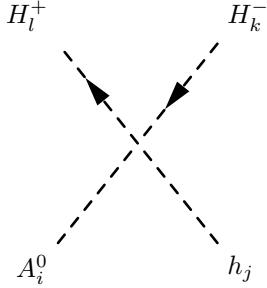
$$\begin{aligned}
& \frac{1}{16} \left( 4 \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab}^* + 4 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{la}^{R,*} Q_{\nu,ab}^* - 4 \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab} \right. \\
& - 4 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{la}^{R,*} Q_{\nu,ab} + v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} \\
& - v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} + v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} \\
& - v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} + v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} \\
& - v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} + v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} \\
& - v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} + 8 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} \\
& \left. - 8 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} \right) Z_{i2}^A Z_{j2}^A \tag{364}
\end{aligned}$$



$$-\frac{i}{16} \left( \left( -4 \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} Q_{\nu,ab}^* - 4 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{la}^{R,*} Q_{\nu,ab}^* - 4 \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} Q_{\nu,ab} \right. \right.$$

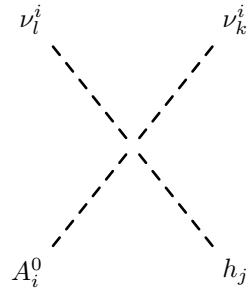
$$\begin{aligned}
& -4 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{la}^{R,*} Q_{\nu,ab} + v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} + v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} + v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} + v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} + 8 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} \\
& + 8 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} \Big) Z_{i2}^A Z_{j2}^A \\
& + 4 \left( g_1^2 + g_2^2 \right) \sum_{a=1}^3 Z_{ka}^{R,*} Z_{la}^{R,*} \left( Z_{i1}^A Z_{j2}^H + Z_{i2}^A Z_{j1}^H \right) \left( -Z_{k1}^+ Z_{l2}^+ + Z_{k2}^+ Z_{l1}^+ \right)
\end{aligned} \tag{365}$$


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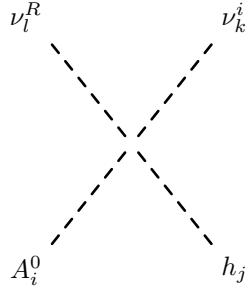
$$\frac{1}{4} g_2^2 \left( Z_{i1}^A Z_{j2}^H + Z_{i2}^A Z_{j1}^H \right) \left( -Z_{k1}^+ Z_{l2}^+ + Z_{k2}^+ Z_{l1}^+ \right) \tag{366}$$


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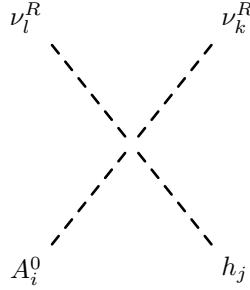


$$\begin{aligned}
& \frac{1}{16} \left( 4 \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab}^* + 4 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{la}^{i,*} Q_{\nu,ab}^* - 4 \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab} \right. \\
& - 4 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{la}^{i,*} Q_{\nu,ab} + v_u^2 \sum_{c=1}^3 Z_{lc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} + v_u^2 \sum_{c=1}^3 Z_{lc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} + v_u^2 \sum_{c=1}^3 Z_{lc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} + v_u^2 \sum_{c=1}^3 Z_{lc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} \\
& \left. + v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} \right) Z_{i2}^A Z_{j2}^H
\end{aligned} \tag{367}$$

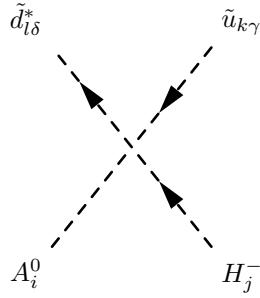

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$$\begin{aligned}
& \frac{i}{16} \left( 4 \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab}^* + 4 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{la}^{R,*} Q_{\nu,ab}^* + 4 \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab} \right. \\
& + 4 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{la}^{R,*} Q_{\nu,ab} + v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} \\
& - v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} + v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} \\
& - v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} + v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} \\
& - v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} + v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} \\
& \left. - v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} \right) Z_{i2}^A Z_{j2}^H
\end{aligned} \tag{368}$$



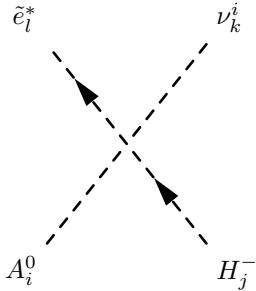
$$\begin{aligned}
& \frac{1}{16} \left( -4 \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} Q_{\nu,ab}^* - 4 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{la}^{R,*} Q_{\nu,ab}^* + 4 \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} Q_{\nu,ab} \right. \\
& + 4 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{la}^{R,*} Q_{\nu,ab} + v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} + v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} + v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} + v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} \\
& \left. + v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} \right) Z_{i2}^A Z_{j2}^H \tag{369}
\end{aligned}$$



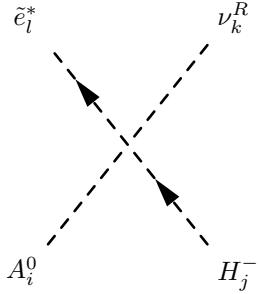
$$\frac{1}{2} \frac{1}{\sqrt{2}} \delta_{\gamma\delta} \left( g_2^2 \sum_{a=1}^3 Z_{ka}^{U,*} Z_{la}^D \left( -Z_{i1}^A Z_{j1}^+ + Z_{i2}^A Z_{j2}^+ \right) \right)$$

$$\begin{aligned}
& + 2 \left( \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{U,*} \sum_{a=1}^3 Y_{d,ac}^* Y_{d,ab} Z_{lc}^D Z_{i1}^A Z_{j1}^+ - \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{U,*} \sum_{a=1}^3 Y_{u,ac}^* Y_{u,ab} Z_{lc}^D Z_{i2}^A Z_{j2}^+ \right. \\
& \left. + \sum_{c=1}^3 Z_{k3+c}^{U,*} \sum_{b=1}^3 \sum_{a=1}^3 Y_{u,ca}^* Y_{d,ba} Z_{l3+b}^D \left( -Z_{i1}^A Z_{j2}^+ + Z_{i2}^A Z_{j1}^+ \right) \right) \tag{370}
\end{aligned}$$

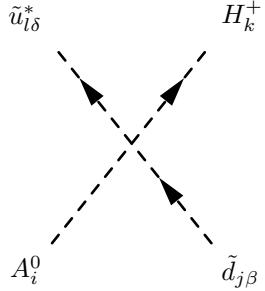

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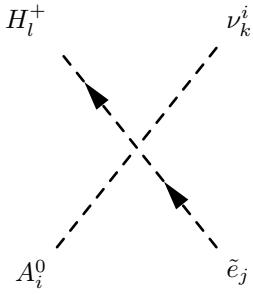
$$\begin{aligned}
& - \frac{i}{16} \left( -8 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{e,ab} Z_{lc}^E Z_{i1}^A Z_{j1}^+ \right. \\
& + 4\sqrt{2} v_u \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ac}^* Y_{e,ba} Z_{l3+b}^E Z_{i2}^A Z_{j1}^+ \\
& + 4\sqrt{2} v_u \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ca}^* Y_{e,ba} Z_{l3+b}^E Z_{i2}^A Z_{j1}^+ \\
& - 2\sqrt{2} v_u \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ac}^* Y_{e,ba} Z_{l3+b}^E Z_{i1}^A Z_{j2}^+ \\
& - 2\sqrt{2} v_u \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ca}^* Y_{e,ba} Z_{l3+b}^E Z_{i1}^A Z_{j2}^+ + 4 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Q_{\nu,ab}^* Z_{la}^E Z_{i2}^A Z_{j2}^+ \\
& + 4 \sum_{b=1}^3 \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab}^* Z_{lb}^E Z_{i2}^A Z_{j2}^+ + v_u^2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{lc}^E Z_{i2}^A Z_{j2}^+ \\
& + v_u^2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{lc}^E Z_{i2}^A Z_{j2}^+ \\
& + v_u^2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} Z_{lc}^E Z_{i2}^A Z_{j2}^+ \\
& + v_u^2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} Z_{lc}^E Z_{i2}^A Z_{j2}^+ \\
& \left. + 8 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} Z_{lc}^E Z_{i2}^A Z_{j2}^+ + 4g_2^2 \sum_{a=1}^3 Z_{ka}^E \left( Z_{i1}^A Z_{j1}^+ - Z_{i2}^A Z_{j2}^+ \right) \right) \tag{371}
\end{aligned}$$



$$\begin{aligned}
& \frac{1}{16} \left( 8 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{e,ab} Z_{lc}^E Z_{i1}^A Z_{j1}^+ \right. \\
& + 4\sqrt{2} v_u \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ac}^* Y_{e,ba} Z_{l3+b}^E Z_{i2}^A Z_{j1}^+ \\
& + 4\sqrt{2} v_u \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ca}^* Y_{e,ba} Z_{l3+b}^E Z_{i2}^A Z_{j1}^+ \\
& - 2\sqrt{2} v_u \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ac}^* Y_{e,ba} Z_{l3+b}^E Z_{i1}^A Z_{j2}^+ \\
& - 2\sqrt{2} v_u \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ca}^* Y_{e,ba} Z_{l3+b}^E Z_{i1}^A Z_{j2}^+ + 4 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Q_{\nu,ab}^* Z_{la}^E Z_{i2}^A Z_{j2}^+ \\
& + 4 \sum_{b=1}^3 \sum_{a=1}^3 Z_{ka}^{R,*} Q_{\nu,ab}^* Z_{lb}^E Z_{i2}^A Z_{j2}^+ - v_u^2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{lc}^E Z_{i2}^A Z_{j2}^+ \\
& - v_u^2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{lc}^E Z_{i2}^A Z_{j2}^+ \\
& - v_u^2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} Z_{lc}^E Z_{i2}^A Z_{j2}^+ \\
& - v_u^2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} Z_{lc}^E Z_{i2}^A Z_{j2}^+ \\
& \left. - 8 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} Z_{lc}^E Z_{i2}^A Z_{j2}^+ + 4g_2^2 \sum_{a=1}^3 Z_{ka}^{R,*} Z_{la}^E \left( -Z_{i1}^A Z_{j1}^+ + Z_{i2}^A Z_{j2}^+ \right) \right) \quad (372)
\end{aligned}$$

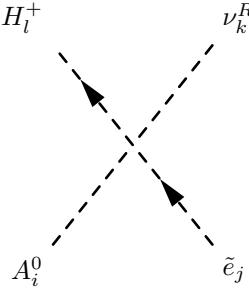


$$\begin{aligned}
& \frac{1}{2} \frac{1}{\sqrt{2}} \delta_{\beta\delta} \left( -2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{D,*} \sum_{a=1}^3 Y_{d,ac}^* Y_{d,ab} Z_{lc}^U Z_{i1}^A Z_{k1}^+ \right. \\
& - 2 \sum_{c=1}^3 Z_{j3+c}^{D,*} \sum_{b=1}^3 \sum_{a=1}^3 Y_{d,ca}^* Y_{u,ba} Z_{l3+b}^U Z_{i2}^A Z_{k1}^+ \\
& + 2 \sum_{c=1}^3 Z_{j3+c}^{D,*} \sum_{b=1}^3 \sum_{a=1}^3 Y_{d,ca}^* Y_{u,ba} Z_{l3+b}^U Z_{i1}^A Z_{k2}^+ \\
& \left. + 2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{D,*} \sum_{a=1}^3 Y_{u,ac}^* Y_{u,ab} Z_{lc}^U Z_{i2}^A Z_{k2}^+ + g_2^2 \sum_{a=1}^3 Z_{ja}^{D,*} Z_{la}^U (Z_{i1}^A Z_{k1}^+ - Z_{i2}^A Z_{k2}^+) \right) \tag{373}
\end{aligned}$$



$$\begin{aligned}
& - \frac{i}{16} \left( -8 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{e,ab} Z_{i1}^A Z_{l1}^+ \right. \\
& + 2\sqrt{2} v_u \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ab} Z_{i2}^A Z_{l1}^+ \\
& + 2\sqrt{2} v_u \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ba} Z_{i2}^A Z_{l1}^+ \\
& \left. - 2\sqrt{2} v_u \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ab} Z_{i1}^A Z_{l2}^+ + 4 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ja}^{E,*} Q_{\nu,ab} Z_{i2}^A Z_{l2}^+ \right)
\end{aligned}$$

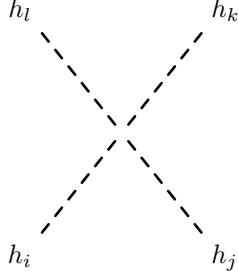
$$\begin{aligned}
& + 4 \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab} Z_{i2}^A Z_{l2}^+ - v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{i2}^A Z_{l2}^+ \\
& - v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{i2}^A Z_{l2}^+ \\
& + 2\sqrt{2}v_d \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ab} Z_{i2}^A Z_{l2}^+ \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} Z_{i2}^A Z_{l2}^+ \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} Z_{i2}^A Z_{l2}^+ \\
& + 2\sqrt{2}v_d \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ba} Z_{i2}^A Z_{l2}^+ \\
& + 8 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} Z_{i2}^A Z_{l2}^+ \\
& + 4g_2^2 \sum_{a=1}^3 Z_{ja}^{E,*} Z_{ka}^{i,*} (Z_{i1}^A Z_{l1}^+ - Z_{i2}^A Z_{l2}^+) \tag{374}
\end{aligned}$$



$$\begin{aligned}
& \frac{1}{16} \left( -8 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{\nu,ab} Z_{i1}^A Z_{l1}^+ \right. \\
& \left. - 2\sqrt{2}v_u \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ab} Z_{i2}^A Z_{l1}^+ \right. \\
& \left. - 2\sqrt{2}v_u \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ba} Z_{i2}^A Z_{l1}^+ \right. \\
& \left. + 2\sqrt{2}v_u \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ab} Z_{i1}^A Z_{l2}^+ - 4 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{E,*} Q_{\nu,ab} Z_{i2}^A Z_{l2}^+ \right)
\end{aligned}$$

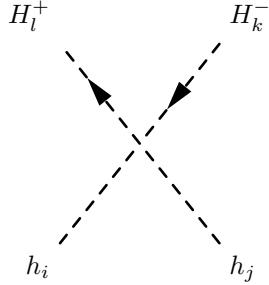
$$\begin{aligned}
& - 4 \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Z_{ka}^{R,*} Q_{\nu,ab} Z_{i2}^A Z_{l2}^+ - v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{i2}^A Z_{l2}^+ \\
& - v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{i2}^A Z_{l2}^+ \\
& - 2\sqrt{2}v_d \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ab} Z_{i2}^A Z_{l2}^+ \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} Z_{i2}^A Z_{l2}^+ \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} Z_{i2}^A Z_{l2}^+ \\
& - 2\sqrt{2}v_d \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ba} Z_{i2}^A Z_{l2}^+ \\
& + 8 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} Z_{i2}^A Z_{l2}^+ \\
& + 4g_2^2 \sum_{a=1}^3 Z_{ja}^{E,*} Z_{ka}^{R,*} (Z_{i1}^A Z_{l1}^+ - Z_{i2}^A Z_{l2}^+) \tag{375}
\end{aligned}$$


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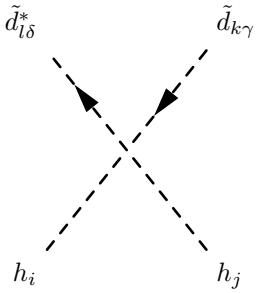
$$\begin{aligned}
& \frac{i}{4} (g_1^2 + g_2^2) \left( Z_{i2}^H \left( Z_{j1}^H \left( Z_{k1}^H Z_{l2}^H + Z_{k2}^H Z_{l1}^H \right) + Z_{j2}^H \left( -3Z_{k2}^H Z_{l2}^H + Z_{k1}^H Z_{l1}^H \right) \right) \right. \\
& \left. + Z_{i1}^H \left( Z_{j1}^H \left( -3Z_{k1}^H Z_{l1}^H + Z_{k2}^H Z_{l2}^H \right) + Z_{j2}^H \left( Z_{k1}^H Z_{l2}^H + Z_{k2}^H Z_{l1}^H \right) \right) \right) \tag{376}
\end{aligned}$$


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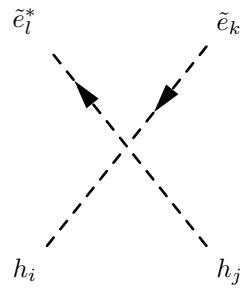
$$\begin{aligned}
& - \frac{i}{4} \left( Z_{i1}^H \left( g_2^2 Z_{j2}^H (Z_{k1}^+ Z_{l2}^+ + Z_{k2}^+ Z_{l1}^+) + Z_{j1}^H \left( (g_1^2 + g_2^2) Z_{k1}^+ Z_{l1}^+ + (-g_1^2 + g_2^2) Z_{k2}^+ Z_{l2}^+ \right) \right) \right. \\
& \left. + Z_{i2}^H \left( g_2^2 Z_{j1}^H (Z_{k1}^+ Z_{l2}^+ + Z_{k2}^+ Z_{l1}^+) + Z_{j2}^H \left( (-g_1^2 + g_2^2) Z_{k1}^+ Z_{l1}^+ + (g_1^2 + g_2^2) Z_{k2}^+ Z_{l2}^+ \right) \right) \right)
\end{aligned} \tag{377}$$


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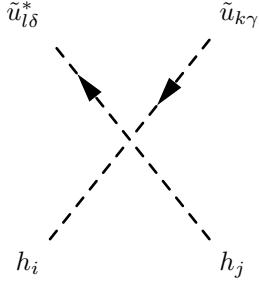
$$\begin{aligned}
& \frac{i}{12} \delta_{\gamma\delta} \left( (3g_2^2 + g_1^2) \sum_{a=1}^3 Z_{ka}^{D,*} Z_{la}^D (Z_{i1}^H Z_{j1}^H - Z_{i2}^H Z_{j2}^H) \right. \\
& + 2 \left( -6 \left( \sum_{c=1}^3 Z_{k3+c}^{D,*} \sum_{b=1}^3 \sum_{a=1}^3 Y_{d,ca}^* Y_{d,ba} Z_{l3+b}^D + \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{D,*} \sum_{a=1}^3 Y_{d,ac}^* Y_{d,ab} Z_{lc}^D \right) Z_{i1}^H Z_{j1}^H \right. \\
& \left. \left. + g_1^2 \sum_{a=1}^3 Z_{k3+a}^{D,*} Z_{l3+a}^D (Z_{i1}^H Z_{j1}^H - Z_{i2}^H Z_{j2}^H) \right) \right)
\end{aligned} \tag{378}$$


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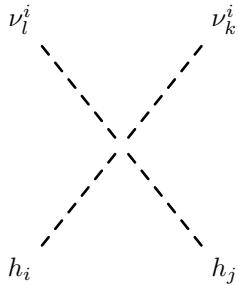
$$\begin{aligned}
& -\frac{i}{4} \left( 4 \left( \sum_{c=1}^3 Z_{k3+c}^{E,*} \sum_{b=1}^3 \sum_{a=1}^3 Y_{e,ca}^* Y_{e,ba} Z_{l3+b}^E + \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{E,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{e,ab} Z_{lc}^E \right) Z_{i1}^H Z_{j1}^H \right. \\
& + \left( -g_2^2 + g_1^2 \right) \sum_{a=1}^3 Z_{ka}^{E,*} Z_{la}^E \left( Z_{i1}^H Z_{j1}^H - Z_{i2}^H Z_{j2}^H \right) \\
& \left. + 2g_1^2 \sum_{a=1}^3 Z_{k3+a}^{E,*} Z_{l3+a}^E \left( -Z_{i1}^H Z_{j1}^H + Z_{i2}^H Z_{j2}^H \right) \right) \tag{379}
\end{aligned}$$


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$$\begin{aligned}
& \frac{i}{12} \delta_{\gamma\delta} \left( \left( -3g_2^2 + g_1^2 \right) \sum_{a=1}^3 Z_{ka}^{U,*} Z_{la}^U \left( Z_{i1}^H Z_{j1}^H - Z_{i2}^H Z_{j2}^H \right) \right. \\
& - 4 \left( 3 \left( \sum_{c=1}^3 Z_{k3+c}^{U,*} \sum_{b=1}^3 \sum_{a=1}^3 Y_{u,ca}^* Y_{u,ba} Z_{l3+b}^U + \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{U,*} \sum_{a=1}^3 Y_{u,ac}^* Y_{u,ab} Z_{lc}^U \right) Z_{i2}^H Z_{j2}^H \right. \\
& \left. \left. + g_1^2 \sum_{a=1}^3 Z_{k3+a}^{U,*} Z_{l3+a}^U \left( Z_{i1}^H Z_{j1}^H - Z_{i2}^H Z_{j2}^H \right) \right) \right) \tag{380}
\end{aligned}$$

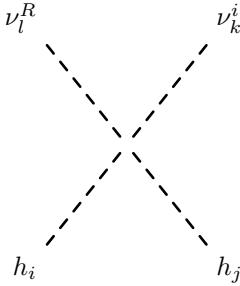

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$$-\frac{i}{16} \left( \left( -4 \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab}^* - 4 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{la}^{i,*} Q_{\nu,ab}^* - 4 \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab} \right) \right.$$

$$\begin{aligned}
& -4 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{la}^{i,*} Q_{\nu,ab} + 3v_u^2 \sum_{c=1}^3 Z_{lc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} \\
& + 3v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} + 3v_u^2 \sum_{c=1}^3 Z_{lc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} \\
& + 3v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} + 3v_u^2 \sum_{c=1}^3 Z_{lc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} \\
& + 3v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} + 3v_u^2 \sum_{c=1}^3 Z_{lc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} \\
& + 3v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} + 8 \sum_{c=1}^3 Z_{lc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} \\
& + 8 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} \Big) Z_{i2}^H Z_{j2}^H \\
& + 4 \left( g_1^2 + g_2^2 \right) \sum_{a=1}^3 Z_{ka}^{i,*} Z_{la}^{i,*} \left( Z_{i1}^H Z_{j1}^H - Z_{i2}^H Z_{j2}^H \right) \quad (381)
\end{aligned}$$

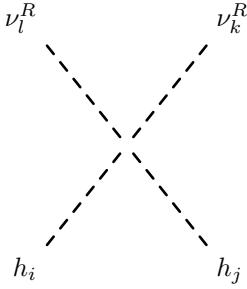

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$$\begin{aligned}
& \frac{1}{16} \left( -4 \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab}^* - 4 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{la}^{R,*} Q_{\nu,ab}^* + 4 \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab} \right. \\
& + 4 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{la}^{R,*} Q_{\nu,ab} + 3v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} \\
& - 3v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} + 3v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} \\
& - 3v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} + 3v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} \\
& \left. - 3v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} + 3v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} \right)
\end{aligned}$$

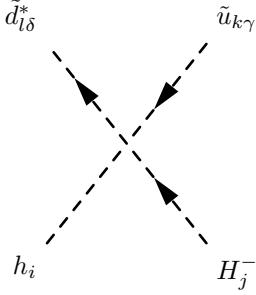
$$\begin{aligned}
& -3v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} + 8 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} \\
& - 8 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} \Big) Z_{i2}^H Z_{j2}^H
\end{aligned} \tag{382}$$


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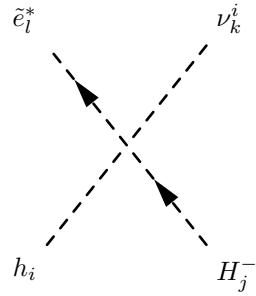
$$\begin{aligned}
& -\frac{i}{16} \left( \left( 4 \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} Q_{\nu,ab}^* + 4 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{la}^{R,*} Q_{\nu,ab}^* + 4 \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} Q_{\nu,ab} \right. \right. \\
& + 4 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{la}^{R,*} Q_{\nu,ab} + 3v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} \\
& + 3v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} + 3v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} \\
& + 3v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} + 3v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} \\
& + 3v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} + 3v_u^2 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} \\
& + 3v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} + 8 \sum_{c=1}^3 Z_{lc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} \\
& \left. \left. + 8 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} \right) Z_{i2}^H Z_{j2}^H \right. \\
& + 4 \left( g_1^2 + g_2^2 \right) \sum_{a=1}^3 Z_{ka}^{R,*} Z_{la}^{R,*} \left( Z_{i1}^H Z_{j1}^H - Z_{i2}^H Z_{j2}^H \right)
\end{aligned} \tag{383}$$


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$$\begin{aligned}
& -\frac{i}{2}\frac{1}{\sqrt{2}}\delta_{\gamma\delta}\left(g_2^2\sum_{a=1}^3 Z_{ka}^{U,*}Z_{la}^D\left(Z_{i1}^HZ_{j1}^+ + Z_{i2}^HZ_{j2}^+\right)\right. \\
& -2\left(\sum_{c=1}^3\sum_{b=1}^3 Z_{kb}^{U,*}\sum_{a=1}^3 Y_{d,ac}^*Y_{d,ab}Z_{lc}^DZ_{i1}^HZ_{j1}^+ + \sum_{c=1}^3\sum_{b=1}^3 Z_{kb}^{U,*}\sum_{a=1}^3 Y_{u,ac}^*Y_{u,ab}Z_{lc}^DZ_{i2}^HZ_{j2}^+\right. \\
& \left.\left. + \sum_{c=1}^3 Z_{k3+c}^{U,*}\sum_{b=1}^3\sum_{a=1}^3 Y_{u,ca}^*Y_{d,ba}Z_{l3+b}^D\left(Z_{i1}^HZ_{j2}^+ + Z_{i2}^HZ_{j1}^+\right)\right)\right) \tag{384}
\end{aligned}$$

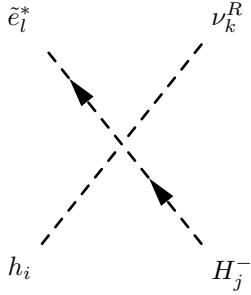

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$$\begin{aligned}
& \frac{1}{16}\left(-8\sum_{c=1}^3\sum_{b=1}^3 Z_{kb}^{i,*}\sum_{a=1}^3 Y_{e,ac}^*Y_{e,ab}Z_{lc}^E Z_{i1}^HZ_{j1}^+\right. \\
& +4\sqrt{2}v_u\sum_{c=1}^3 Z_{kc}^{i,*}\sum_{b=1}^3\sum_{a=1}^3 \kappa_{\nu,ac}^*Y_{e,ba}Z_{l3+b}^EZ_{i2}^HZ_{j1}^+ \\
& +4\sqrt{2}v_u\sum_{c=1}^3 Z_{kc}^{i,*}\sum_{b=1}^3\sum_{a=1}^3 \kappa_{\nu,ca}^*Y_{e,ba}Z_{l3+b}^EZ_{i2}^HZ_{j1}^+ \\
& +2\sqrt{2}v_u\sum_{c=1}^3 Z_{kc}^{i,*}\sum_{b=1}^3\sum_{a=1}^3 \kappa_{\nu,ac}^*Y_{e,ba}Z_{l3+b}^EZ_{i1}^HZ_{j2}^+ \\
& \left.+2\sqrt{2}v_u\sum_{c=1}^3 Z_{kc}^{i,*}\sum_{b=1}^3\sum_{a=1}^3 \kappa_{\nu,ca}^*Y_{e,ba}Z_{l3+b}^EZ_{i1}^HZ_{j2}^+ + 4\sum_{b=1}^3 Z_{kb}^{i,*}\sum_{a=1}^3 Q_{\nu,ab}^*Z_{la}^EZ_{i2}^HZ_{j2}^+\right)
\end{aligned}$$

$$\begin{aligned}
& + 4 \sum_{b=1}^3 \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab}^* Z_{lb}^E Z_{i2}^H Z_{j2}^+ - v_u^2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{lc}^E Z_{i2}^H Z_{j2}^+ \\
& - v_u^2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{lc}^E Z_{i2}^H Z_{j2}^+ \\
& - v_u^2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} Z_{lc}^E Z_{i2}^H Z_{j2}^+ \\
& - v_u^2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} Z_{lc}^E Z_{i2}^H Z_{j2}^+ \\
& - 8 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} Z_{lc}^E Z_{i2}^H Z_{j2}^+ + 4g_2^2 \sum_{a=1}^3 Z_{ka}^{i,*} Z_{la}^E (Z_{i1}^H Z_{j1}^+ + Z_{i2}^H Z_{j2}^+) \quad (385)
\end{aligned}$$

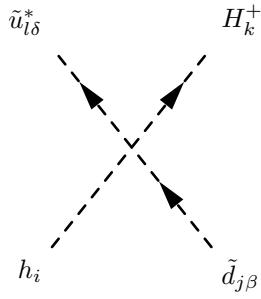

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$$\begin{aligned}
& \frac{i}{16} \left( 8 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{e,ab} Z_{lc}^E Z_{i1}^H Z_{j1}^+ \right. \\
& + 4\sqrt{2}v_u \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ac}^* Y_{e,ba} Z_{l3+b}^E Z_{i2}^H Z_{j1}^+ \\
& + 4\sqrt{2}v_u \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ca}^* Y_{e,ba} Z_{l3+b}^E Z_{i2}^H Z_{j1}^+ \\
& + 2\sqrt{2}v_u \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ac}^* Y_{e,ba} Z_{l3+b}^E Z_{i1}^H Z_{j2}^+ \\
& + 2\sqrt{2}v_u \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ca}^* Y_{e,ba} Z_{l3+b}^E Z_{i1}^H Z_{j2}^+ + 4 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Q_{\nu,ab}^* Z_{la}^E Z_{i2}^H Z_{j2}^+ \\
& + 4 \sum_{b=1}^3 \sum_{a=1}^3 Z_{ka}^{R,*} Q_{\nu,ab}^* Z_{lb}^E Z_{i2}^H Z_{j2}^+ + v_u^2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{lc}^E Z_{i2}^H Z_{j2}^+ \\
& \left. + v_u^2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{lc}^E Z_{i2}^H Z_{j2}^+ \right)
\end{aligned}$$

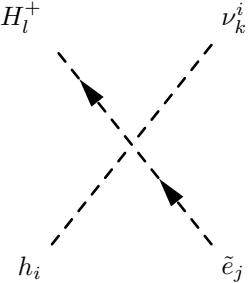
$$\begin{aligned}
& + v_u^2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} Z_{lc}^E Z_{i2}^H Z_{j2}^+ \\
& + v_u^2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} Z_{lc}^E Z_{i2}^H Z_{j2}^+ \\
& + 8 \sum_{c=1}^3 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} Z_{lc}^E Z_{i2}^H Z_{j2}^+ - 4g_2^2 \sum_{a=1}^3 Z_{ka}^{R,*} Z_{la}^E (Z_{i1}^H Z_{j1}^+ + Z_{i2}^H Z_{j2}^+) \tag{386}
\end{aligned}$$


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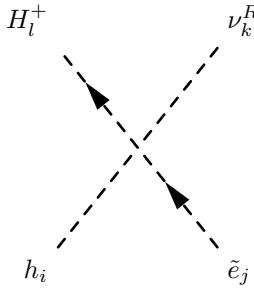
$$\begin{aligned}
& - \frac{i}{2} \frac{1}{\sqrt{2}} \delta_{\beta\delta} \left( g_2^2 \sum_{a=1}^3 Z_{ja}^{D,*} Z_{la}^U (Z_{i1}^H Z_{k1}^+ + Z_{i2}^H Z_{k2}^+) \right. \\
& - 2 \left( \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{D,*} \sum_{a=1}^3 Y_{d,ac}^* Y_{d,ab} Z_{lc}^U Z_{i1}^H Z_{k1}^+ + \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{D,*} \sum_{a=1}^3 Y_{u,ac}^* Y_{u,ab} Z_{lc}^U Z_{i2}^H Z_{k2}^+ \right. \\
& \left. \left. + \sum_{c=1}^3 Z_{j3+c}^{D,*} \sum_{b=1}^3 \sum_{a=1}^3 Y_{d,ca}^* Y_{u,ba} Z_{l3+b}^U (Z_{i1}^H Z_{k2}^+ + Z_{i2}^H Z_{k1}^+) \right) \right) \tag{387}
\end{aligned}$$


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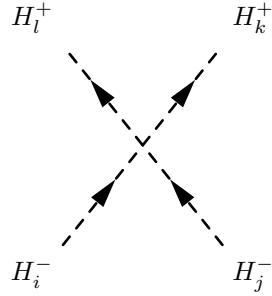
$$\frac{1}{16} \left( 8 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{e,ab} Z_{i1}^H Z_{l1}^+ \right.$$

$$\begin{aligned}
& -2\sqrt{2}v_u \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ab} Z_{i2}^H Z_{l1}^+ \\
& -2\sqrt{2}v_u \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ba} Z_{i2}^H Z_{l1}^+ \\
& -2\sqrt{2}v_u \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ab} Z_{i1}^H Z_{l2}^+ \\
& -4 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ja}^{E,*} Q_{\nu,ab} Z_{i2}^H Z_{l2}^+ - 4 \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Z_{ka}^{i,*} Q_{\nu,ab} Z_{i2}^H Z_{l2}^+ \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{i2}^H Z_{l2}^+ \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{i2}^H Z_{l2}^+ \\
& -2\sqrt{2}v_d \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ab} Z_{i2}^H Z_{l2}^+ \\
& + 3v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} Z_{i2}^H Z_{l2}^+ \\
& + 3v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} Z_{i2}^H Z_{l2}^+ \\
& -2\sqrt{2}v_d \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ba} Z_{i2}^H Z_{l2}^+ \\
& + 8 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} Z_{i2}^H Z_{l2}^+ - 4g_2^2 \sum_{a=1}^3 Z_{ja}^{E,*} Z_{ka}^{i,*} (Z_{i1}^H Z_{l1}^+ + Z_{i2}^H Z_{l2}^+) \tag{388}
\end{aligned}$$

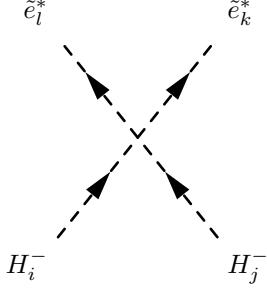


$$\frac{i}{16} \left( 8 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{e,ab} Z_{i1}^H Z_{l1}^+ \right.$$

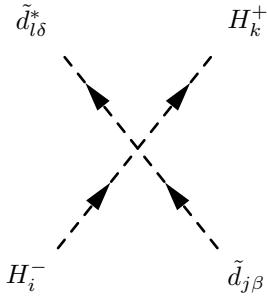
$$\begin{aligned}
& + 2\sqrt{2}v_u \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ab} Z_{i2}^H Z_{l1}^+ \\
& + 2\sqrt{2}v_u \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ba} Z_{i2}^H Z_{l1}^+ \\
& + 2\sqrt{2}v_u \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ab} Z_{i1}^H Z_{l2}^+ + 4 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{E,*} Q_{\nu,ab} Z_{i2}^H Z_{l2}^+ \\
& + 4 \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Z_{ka}^{R,*} Q_{\nu,ab} Z_{i2}^H Z_{l2}^+ + v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{i2}^H Z_{l2}^+ \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{i2}^H Z_{l2}^+ \\
& + 2\sqrt{2}v_d \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ab} Z_{i2}^H Z_{l2}^+ \\
& + 3v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} Z_{i2}^H Z_{l2}^+ \\
& + 3v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} Z_{i2}^H Z_{l2}^+ \\
& + 2\sqrt{2}v_d \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ba} Z_{i2}^H Z_{l2}^+ \\
& + 8 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} Z_{i2}^H Z_{l2}^+ - 4g_2^2 \sum_{a=1}^3 Z_{ja}^{E,*} Z_{ka}^{R,*} (Z_{i1}^H Z_{l1}^+ + Z_{i2}^H Z_{l2}^+) \tag{389}
\end{aligned}$$



$$\begin{aligned}
& - \frac{i}{4} (g_1^2 + g_2^2) \left( -Z_{i2}^+ \left( -2Z_{j2}^+ Z_{k2}^+ Z_{l2}^+ + Z_{j1}^+ (Z_{k1}^+ Z_{l2}^+ + Z_{k2}^+ Z_{l1}^+) \right) \right. \\
& \left. + Z_{i1}^+ (2Z_{j1}^+ Z_{k1}^+ Z_{l1}^+ - Z_{j2}^+ (Z_{k1}^+ Z_{l2}^+ + Z_{k2}^+ Z_{l1}^+)) \right) \tag{390}
\end{aligned}$$



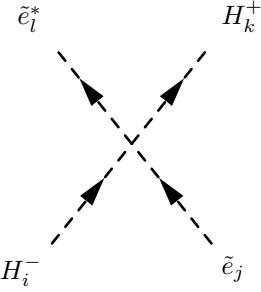
$$\begin{aligned}
& -\frac{i}{4} \left( \sqrt{2} v_u \sum_{c=1}^3 \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ac}^* Y_{e,ba} Z_{k3+b}^E Z_{lc}^E Z_{i2}^+ Z_{j1}^+ \right. \\
& + \sqrt{2} v_u \sum_{c=1}^3 \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ca}^* Y_{e,ba} Z_{k3+b}^E Z_{lc}^E Z_{i2}^+ Z_{j1}^+ \\
& + \sqrt{2} v_u \sum_{c=1}^3 \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ac}^* Y_{e,ba} Z_{k3+b}^E Z_{lc}^E Z_{i1}^+ Z_{j2}^+ \\
& + \sqrt{2} v_u \sum_{c=1}^3 \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ca}^* Y_{e,ba} Z_{k3+b}^E Z_{lc}^E Z_{i1}^+ Z_{j2}^+ + 4 \sum_{b=1}^3 \sum_{a=1}^3 Q_{\nu,ab}^* Z_{la}^E Z_{kb}^E Z_{i2}^+ Z_{j2}^+ \\
& + 4 \sum_{b=1}^3 \sum_{a=1}^3 Q_{\nu,ab}^* Z_{ka}^E Z_{lb}^E Z_{i2}^+ Z_{j2}^+ \\
& \left. + \sqrt{2} v_u \sum_{c=1}^3 \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ac}^* Y_{e,ba} Z_{l3+b}^E Z_{kc}^E (Z_{i1}^+ Z_{j2}^+ + Z_{i2}^+ Z_{j1}^+) \right. \\
& \left. + \sqrt{2} v_u \sum_{c=1}^3 \sum_{b=1}^3 \sum_{a=1}^3 \kappa_{\nu,ca}^* Y_{e,ba} Z_{l3+b}^E Z_{kc}^E (Z_{i1}^+ Z_{j2}^+ + Z_{i2}^+ Z_{j1}^+) \right) \quad (391)
\end{aligned}$$



$$\frac{i}{12} \delta_{\beta\delta} \left( (-3g_2^2 + g_1^2) \sum_{a=1}^3 Z_{ja}^{D,*} Z_{la}^D (Z_{i1}^+ Z_{k1}^+ - Z_{i2}^+ Z_{k2}^+) \right)$$

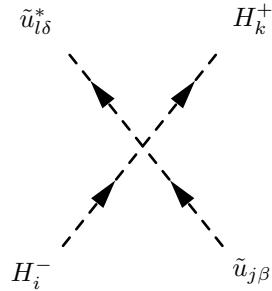
$$\begin{aligned}
& + 2 \left( g_1^2 \sum_{a=1}^3 Z_{j3+a}^{D,*} Z_{l3+a}^D \left( Z_{i1}^+ Z_{k1}^+ - Z_{i2}^+ Z_{k2}^+ \right) \right. \\
& \left. - 6 \left( \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{D,*} \sum_{a=1}^3 Y_{u,ac}^* Y_{u,ab} Z_{lc}^D Z_{i2}^+ Z_{k2}^+ + \sum_{c=1}^3 Z_{j3+c}^{D,*} \sum_{b=1}^3 \sum_{a=1}^3 Y_{d,ca}^* Y_{d,ba} Z_{l3+b}^D Z_{i1}^+ Z_{k1}^+ \right) \right) \quad (392)
\end{aligned}$$


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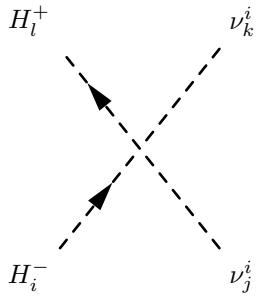
$$\begin{aligned}
& - \frac{i}{8} \left( 8 \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 \sum_{a=1}^3 Y_{e,ca}^* Y_{e,ba} Z_{l3+b}^E Z_{i1}^+ Z_{k1}^+ \right. \\
& + v_u^2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ba} Z_{lc}^E Z_{i2}^+ Z_{k2}^+ \\
& + v_u^2 \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ba} Z_{lc}^E Z_{i2}^+ Z_{k2}^+ \\
& + 8 \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Y_{\nu,ac}^* Y_{\nu,ab} Z_{lc}^E Z_{i2}^+ Z_{k2}^+ \\
& + 2 \left( g_1^2 + g_2^2 \right) \sum_{a=1}^3 Z_{ja}^{E,*} Z_{la}^E \left( Z_{i1}^+ Z_{k1}^+ - Z_{i2}^+ Z_{k2}^+ \right) \\
& \left. + 4g_1^2 \sum_{a=1}^3 Z_{j3+a}^{E,*} Z_{l3+a}^E \left( -Z_{i1}^+ Z_{k1}^+ + Z_{i2}^+ Z_{k2}^+ \right) \right) \quad (393)
\end{aligned}$$


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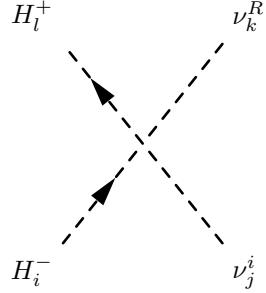
$$\begin{aligned}
& \frac{i}{12} \delta_{\beta\delta} \left( \left( 3g_2^2 + g_1^2 \right) \sum_{a=1}^3 Z_{ja}^{U,*} Z_{la}^U \left( Z_{i1}^+ Z_{k1}^+ - Z_{i2}^+ Z_{k2}^+ \right) \right. \\
& - 4 \left( g_1^2 \sum_{a=1}^3 Z_{j3+a}^{U,*} Z_{l3+a}^U \left( Z_{i1}^+ Z_{k1}^+ - Z_{i2}^+ Z_{k2}^+ \right) \right. \\
& \left. \left. + 3 \left( \sum_{c=1}^3 \sum_{b=1}^3 Z_{jb}^{U,*} \sum_{a=1}^3 Y_{d,ac}^* Y_{d,ab} Z_{lc}^U Z_{i1}^+ Z_{k1}^+ + \sum_{c=1}^3 Z_{j3+c}^{U,*} \sum_{b=1}^3 \sum_{a=1}^3 Y_{u,ca}^* Y_{u,ba} Z_{l3+b}^U Z_{i2}^+ Z_{k2}^+ \right) \right) \right) \quad (394)
\end{aligned}$$


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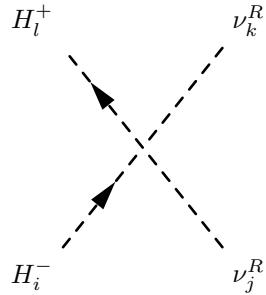
$$\begin{aligned}
& - \frac{i}{16} \left( 8 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{e,ab} Z_{i1}^+ Z_{l1}^+ \right. \\
& + 8 \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{e,ab} Z_{i1}^+ Z_{l1}^+ \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{i2}^+ Z_{l2}^+ \\
& + v_u^2 \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{i2}^+ Z_{l2}^+ \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{i2}^+ Z_{l2}^+ \\
& + v_u^2 \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{i2}^+ Z_{l2}^+ \\
& \left. + 4 \left( -g_2^2 + g_1^2 \right) \sum_{a=1}^3 Z_{ja}^{i,*} Z_{ka}^{i,*} \left( Z_{i1}^+ Z_{l1}^+ - Z_{i2}^+ Z_{l2}^+ \right) \right) \quad (395)
\end{aligned}$$


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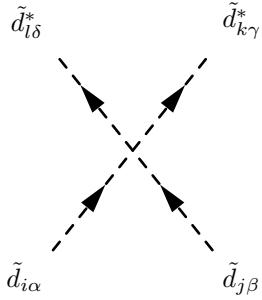
$$\begin{aligned}
& \frac{1}{16} \left( 8 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{e,ab} Z_{i1}^+ Z_{l1}^+ \right. \\
& - 8 \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{e,ab} Z_{i1}^+ Z_{l1}^+ \\
& + v_u^2 \left( \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} - \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} \right. \\
& \left. + \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} - \sum_{c=1}^3 Z_{jc}^{i,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} \right) Z_{i2}^+ Z_{l2}^+ \quad (396)
\end{aligned}$$


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$$\begin{aligned}
& - \frac{i}{16} \left( 8 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{e,ab} Z_{i1}^+ Z_{l1}^+ \right. \\
& + 8 \sum_{c=1}^3 Z_{jc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{e,ac}^* Y_{e,ab} Z_{i1}^+ Z_{l1}^+ \\
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{i2}^+ Z_{l2}^+ \\
& \left. + v_u^2 \sum_{c=1}^3 Z_{jc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ac}^* \kappa_{\nu,ab} Z_{i2}^+ Z_{l2}^+ \right)
\end{aligned}$$

$$\begin{aligned}
& + v_u^2 \sum_{c=1}^3 Z_{kc}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{i2}^+ Z_{l2}^+ \\
& + v_u^2 \sum_{c=1}^3 Z_{jc}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 \kappa_{\nu,ca}^* \kappa_{\nu,ab} Z_{i2}^+ Z_{l2}^+ \\
& + 4(-g_2^2 + g_1^2) \sum_{a=1}^3 Z_{ja}^{R,*} Z_{ka}^{R,*} (Z_{i1}^+ Z_{l1}^+ - Z_{i2}^+ Z_{l2}^+) \tag{397}
\end{aligned}$$

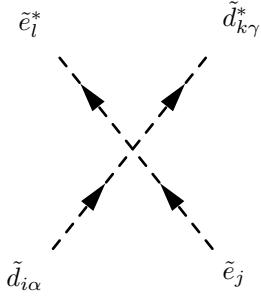


$$\begin{aligned}
& - \frac{i}{72} \left( \delta_{\alpha\delta} \delta_{\beta\gamma} \left( g_1^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{la}^D \sum_{b=1}^3 Z_{jb}^{D,*} Z_{kb}^D + 9g_2^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{la}^D \sum_{b=1}^3 Z_{jb}^{D,*} Z_{kb}^D \right. \right. \\
& \left. \left. - 6g_3^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{la}^D \sum_{b=1}^3 Z_{jb}^{D,*} Z_{kb}^D + 2g_1^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{l3+a}^D \sum_{b=1}^3 Z_{jb}^{D,*} Z_{kb}^D \right. \right. \\
& \left. \left. + 6g_3^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{l3+a}^D \sum_{b=1}^3 Z_{jb}^{D,*} Z_{kb}^D \right. \right. \\
& \left. \left. + 18g_3^2 \sum_{a=1}^3 Z_{ja}^{D,*} Z_{la}^D \left( - \sum_{b=1}^3 Z_{i3+b}^{D,*} Z_{k3+b}^D + \sum_{b=1}^3 Z_{ib}^{D,*} Z_{kb}^D \right) \right. \right. \\
& \left. \left. - 18g_3^2 \sum_{a=1}^3 Z_{j3+a}^{D,*} Z_{l3+a}^D \left( - \sum_{b=1}^3 Z_{i3+b}^{D,*} Z_{k3+b}^D + \sum_{b=1}^3 Z_{ib}^{D,*} Z_{kb}^D \right) \right. \right. \\
& \left. \left. + 2g_1^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{la}^D \sum_{b=1}^3 Z_{j3+b}^{D,*} Z_{k3+b}^D + 6g_3^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{la}^D \sum_{b=1}^3 Z_{j3+b}^{D,*} Z_{k3+b}^D \right. \right. \\
& \left. \left. + 4g_1^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{l3+a}^D \sum_{b=1}^3 Z_{j3+b}^{D,*} Z_{k3+b}^D - 6g_3^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{l3+a}^D \sum_{b=1}^3 Z_{j3+b}^{D,*} Z_{k3+b}^D \right. \right. \\
& \left. \left. + g_1^2 \sum_{a=1}^3 Z_{ja}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{ib}^{D,*} Z_{lb}^D + 9g_2^2 \sum_{a=1}^3 Z_{ja}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{ib}^{D,*} Z_{lb}^D \right. \right. \\
& \left. \left. - 6g_3^2 \sum_{a=1}^3 Z_{ja}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{ib}^{D,*} Z_{lb}^D + 2g_1^2 \sum_{a=1}^3 Z_{j3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{ib}^{D,*} Z_{lb}^D \right) \right)
\end{aligned}$$

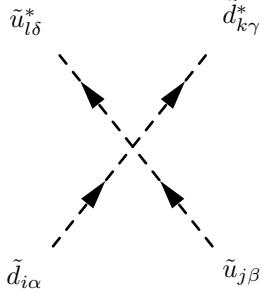
$$\begin{aligned}
& + 6g_3^2 \sum_{a=1}^3 Z_{j3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{ib}^{D,*} Z_{lb}^D + 18g_3^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{jb}^{D,*} Z_{lb}^D \\
& - 18g_3^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{jb}^{D,*} Z_{lb}^D + 2g_1^2 \sum_{a=1}^3 Z_{ja}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{i3+b}^{D,*} Z_{l3+b}^D \\
& + 6g_3^2 \sum_{a=1}^3 Z_{ja}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{i3+b}^{D,*} Z_{l3+b}^D + 4g_1^2 \sum_{a=1}^3 Z_{j3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{i3+b}^{D,*} Z_{l3+b}^D \\
& - 6g_3^2 \sum_{a=1}^3 Z_{j3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{i3+b}^{D,*} Z_{l3+b}^D - 18g_3^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{j3+b}^{D,*} Z_{l3+b}^D \\
& + 18g_3^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{j3+b}^{D,*} Z_{l3+b}^D \\
& + 72 \sum_{b=1}^3 Z_{ib}^{D,*} \sum_{a=1}^3 Y_{d,ab} Z_{l3+a}^D \sum_{d=1}^3 \sum_{c=1}^3 Y_{d,cd}^* Z_{j3+c}^{D,*} Z_{kd}^D \\
& + 72 \sum_{b=1}^3 Z_{jb}^{D,*} \sum_{a=1}^3 Y_{d,ab} Z_{k3+a}^D \sum_{d=1}^3 \sum_{c=1}^3 Y_{d,cd}^* Z_{i3+c}^{D,*} Z_{ld}^D \Big) \\
& + \delta_{\alpha\gamma} \delta_{\beta\delta} \left( 18g_3^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{la}^D \sum_{b=1}^3 Z_{jb}^{D,*} Z_{kb}^D - 18g_3^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{l3+a}^D \sum_{b=1}^3 Z_{jb}^{D,*} Z_{kb}^D \right. \\
& \left. + 2 \sum_{a=1}^3 Z_{j3+a}^{D,*} Z_{l3+a}^D \left( (2g_1^2 - 3g_3^2) \sum_{b=1}^3 Z_{i3+b}^{D,*} Z_{k3+b}^D + (3g_3^2 + g_1^2) \sum_{b=1}^3 Z_{ib}^{D,*} Z_{kb}^D \right) \right. \\
& \left. + \sum_{a=1}^3 Z_{ja}^{D,*} Z_{la}^D \left( 2(3g_3^2 + g_1^2) \sum_{b=1}^3 Z_{i3+b}^{D,*} Z_{k3+b}^D + (-6g_3^2 + 9g_2^2 + g_1^2) \sum_{b=1}^3 Z_{ib}^{D,*} Z_{kb}^D \right) \right. \\
& \left. - 18g_3^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{la}^D \sum_{b=1}^3 Z_{j3+b}^{D,*} Z_{k3+b}^D + 18g_3^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{l3+a}^D \sum_{b=1}^3 Z_{j3+b}^{D,*} Z_{k3+b}^D \right. \\
& \left. + 18g_3^2 \sum_{a=1}^3 Z_{ja}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{ib}^{D,*} Z_{lb}^D - 18g_3^2 \sum_{a=1}^3 Z_{j3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{ib}^{D,*} Z_{lb}^D \right. \\
& \left. + g_1^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{jb}^{D,*} Z_{lb}^D + 9g_2^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{jb}^{D,*} Z_{lb}^D \right. \\
& \left. - 6g_3^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{jb}^{D,*} Z_{lb}^D + 2g_1^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{jb}^{D,*} Z_{lb}^D \right. \\
& \left. + 6g_3^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{jb}^{D,*} Z_{lb}^D - 18g_3^2 \sum_{a=1}^3 Z_{ja}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{i3+b}^{D,*} Z_{l3+b}^D \right)
\end{aligned}$$

$$\begin{aligned}
& + 18g_3^2 \sum_{a=1}^3 Z_{j3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{i3+b}^{D,*} Z_{l3+b}^D + 2g_1^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{j3+b}^{D,*} Z_{l3+b}^D \\
& + 6g_3^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{j3+b}^{D,*} Z_{l3+b}^D + 4g_1^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{j3+b}^{D,*} Z_{l3+b}^D \\
& - 6g_3^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{j3+b}^{D,*} Z_{l3+b}^D \\
& + 72 \sum_{b=1}^3 Z_{jb}^{D,*} \sum_{a=1}^3 Y_{d,ab} Z_{l3+a}^D \sum_{d=1}^3 \sum_{c=1}^3 Y_{d,cd}^* Z_{i3+c}^{D,*} Z_{kd}^D \\
& + 72 \sum_{b=1}^3 Z_{ib}^{D,*} \sum_{a=1}^3 Y_{d,ab} Z_{k3+a}^D \sum_{d=1}^3 \sum_{c=1}^3 Y_{d,cd}^* Z_{j3+c}^{D,*} Z_{ld}^D \Big) \Big) \tag{398}
\end{aligned}$$


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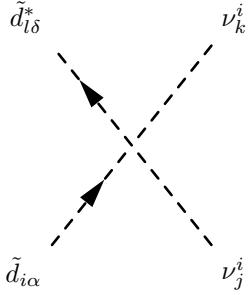
$$\begin{aligned}
& \frac{i}{24} \delta_{\alpha\gamma} \Big( -2g_1^2 \sum_{a=1}^3 Z_{j3+a}^{E,*} Z_{l3+a}^E \Big( 2 \sum_{b=1}^3 Z_{i3+b}^{D,*} Z_{k3+b}^D + \sum_{b=1}^3 Z_{ib}^{D,*} Z_{kb}^D \Big) \\
& + \sum_{a=1}^3 Z_{ja}^{E,*} Z_{la}^E \Big( 2g_1^2 \sum_{b=1}^3 Z_{i3+b}^{D,*} Z_{k3+b}^D + (-3g_2^2 + g_1^2) \sum_{b=1}^3 Z_{ib}^{D,*} Z_{kb}^D \Big) \\
& + g_1^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{jb}^{E,*} Z_{lb}^E - 3g_2^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{jb}^{E,*} Z_{lb}^E \\
& + 2g_1^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{jb}^{E,*} Z_{lb}^E - 2g_1^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{j3+b}^{E,*} Z_{l3+b}^E \\
& - 4g_1^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{j3+b}^{E,*} Z_{l3+b}^E \\
& - 24 \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Y_{e,ab} Z_{l3+a}^E \sum_{d=1}^3 \sum_{c=1}^3 Y_{d,cd}^* Z_{i3+c}^{D,*} Z_{kd}^D \\
& - 24 \sum_{b=1}^3 Z_{ib}^{D,*} \sum_{a=1}^3 Y_{d,ab} Z_{k3+a}^D \sum_{d=1}^3 \sum_{c=1}^3 Y_{e,cd}^* Z_{j3+c}^{E,*} Z_{ld}^E \Big) \tag{399}
\end{aligned}$$



$$\begin{aligned}
& -\frac{i}{72} \left( \delta_{\alpha\gamma} \delta_{\beta\delta} \left( \sum_{a=1}^3 Z_{ja}^{U,*} Z_{la}^U \left( 2(3g_3^2 + g_1^2) \sum_{b=1}^3 Z_{i3+b}^{D,*} Z_{k3+b}^D + (-6g_3^2 - 9g_2^2 + g_1^2) \sum_{b=1}^3 Z_{ib}^{D,*} Z_{kb}^D \right) \right. \right. \\
& - 2 \sum_{a=1}^3 Z_{j3+a}^{U,*} Z_{l3+a}^U \left( (2g_1^2 - 3g_3^2) \sum_{b=1}^3 Z_{ib}^{D,*} Z_{kb}^D + (3g_3^2 + 4g_1^2) \sum_{b=1}^3 Z_{i3+b}^{D,*} Z_{k3+b}^D \right) \\
& + g_1^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{jb}^{U,*} Z_{lb}^U - 9g_2^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{jb}^{U,*} Z_{lb}^U \\
& - 6g_3^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{jb}^{U,*} Z_{lb}^U + 2g_1^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{jb}^{U,*} Z_{lb}^U \\
& + 6g_3^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{jb}^{U,*} Z_{lb}^U - 4g_1^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{l3+b}^U \\
& + 6g_3^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{l3+b}^U - 8g_1^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{l3+b}^U \\
& - 6g_3^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{l3+b}^U \Big) \\
& + 18\delta_{\alpha\delta} \delta_{\beta\gamma} \left( g_2^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{la}^U \sum_{b=1}^3 Z_{jb}^{U,*} Z_{kb}^D + g_3^2 \sum_{a=1}^3 Z_{ja}^{U,*} Z_{la}^U \left( - \sum_{b=1}^3 Z_{i3+b}^{D,*} Z_{k3+b}^D + \sum_{b=1}^3 Z_{ib}^{D,*} Z_{kb}^D \right) \right. \\
& + g_3^2 \sum_{a=1}^3 Z_{j3+a}^{U,*} Z_{l3+a}^U \left( - \sum_{b=1}^3 Z_{ib}^{D,*} Z_{kb}^D + \sum_{b=1}^3 Z_{i3+b}^{D,*} Z_{k3+b}^D \right) \\
& + g_2^2 \sum_{a=1}^3 Z_{ja}^{U,*} Z_{ka}^D \sum_{b=1}^3 Z_{ib}^{D,*} Z_{lb}^U + g_3^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{jb}^{U,*} Z_{lb}^U \\
& \left. \left. - g_3^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{jb}^{U,*} Z_{lb}^U - g_3^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ka}^D \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{l3+b}^U \right) \right)
\end{aligned}$$

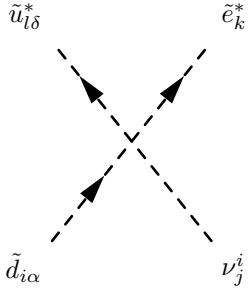
$$\begin{aligned}
& + g_3^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{k3+a}^D \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{l3+b}^U + 4 \sum_{b=1}^3 Z_{ib}^{D,*} \sum_{a=1}^3 Y_{u,ab} Z_{l3+a}^U \sum_{d=1}^3 \sum_{c=1}^3 Y_{u,cd}^* Z_{j3+c}^{U,*} Z_{kd}^D \\
& + 4 \sum_{b=1}^3 Z_{jb}^{U,*} \sum_{a=1}^3 Y_{d,ab} Z_{k3+a}^D \sum_{d=1}^3 \sum_{c=1}^3 Y_{d,cd}^* Z_{i3+c}^{D,*} Z_{ld}^U \Big) \Big) \tag{400}
\end{aligned}$$


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$$\begin{aligned}
& \frac{i}{24} \delta_{\alpha\delta} \left( \left( 3g_2^2 + g_1^2 \right) \sum_{a=1}^3 Z_{ia}^{D,*} Z_{la}^D \sum_{b=1}^3 Z_{jb}^{i,*} Z_{kb}^{i,*} + 2g_1^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{l3+a}^D \sum_{b=1}^3 Z_{jb}^{i,*} Z_{kb}^{i,*} \right. \\
& \left. + \sum_{a=1}^3 Z_{ja}^{i,*} Z_{ka}^{i,*} \left( 2g_1^2 \sum_{b=1}^3 Z_{i3+b}^{D,*} Z_{l3+b}^D + \left( 3g_2^2 + g_1^2 \right) \sum_{b=1}^3 Z_{ib}^{D,*} Z_{lb}^D \right) \right) \tag{401}
\end{aligned}$$

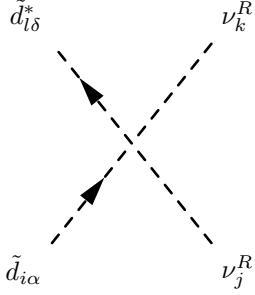

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$$\begin{aligned}
& \frac{1}{8} \delta_{\alpha\delta} \left( \sqrt{2} g_2^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{la}^U \sum_{b=1}^3 Z_{jb}^{i,*} Z_{kb}^E + \sqrt{2} g_2^2 \sum_{a=1}^3 Z_{ja}^{i,*} Z_{ka}^E \sum_{b=1}^3 Z_{ib}^{D,*} Z_{lb}^U \right. \\
& - 2v_u Z_{j1}^{i,*} \sum_{b=1}^3 Z_{ib}^{D,*} \sum_{a=1}^3 Y_{u,ab} Z_{l3+a}^U \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^E \\
& \left. + 4\sqrt{2} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Y_{e,ab} Z_{k3+a}^E \sum_{d=1}^3 \sum_{c=1}^3 Y_{d,cd}^* Z_{i3+c}^{D,*} Z_{ld}^U \right)
\end{aligned}$$

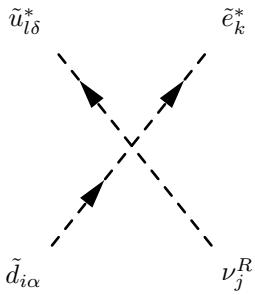
$$- 2v_u \sum_{b=1}^3 Z_{ib}^{D,*} \sum_{a=1}^3 Y_{u,ab} Z_{l3+a}^U \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} Z_{k1}^E \Big) \quad (402)$$


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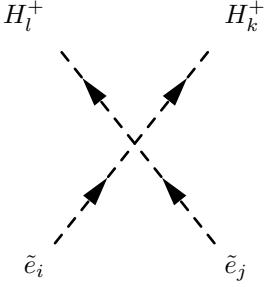
$$\begin{aligned} & \frac{i}{24} \delta_{\alpha\delta} \left( \left( 3g_2^2 + g_1^2 \right) \sum_{a=1}^3 Z_{ia}^{D,*} Z_{la}^D \sum_{b=1}^3 Z_{jb}^{R,*} Z_{kb}^{R,*} + 2g_1^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{l3+a}^D \sum_{b=1}^3 Z_{jb}^{R,*} Z_{kb}^{R,*} \right. \\ & \left. + \sum_{a=1}^3 Z_{ja}^{R,*} Z_{ka}^{R,*} \left( 2g_1^2 \sum_{b=1}^3 Z_{i3+b}^{D,*} Z_{l3+b}^D + \left( 3g_2^2 + g_1^2 \right) \sum_{b=1}^3 Z_{ib}^{D,*} Z_{lb}^D \right) \right) \end{aligned} \quad (403)$$


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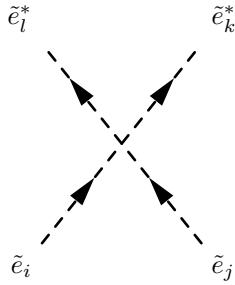


$$\begin{aligned} & - \frac{i}{8} \delta_{\alpha\delta} \left( \sqrt{2}g_2^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{la}^U \sum_{b=1}^3 Z_{jb}^{R,*} Z_{kb}^E + \sqrt{2}g_2^2 \sum_{a=1}^3 Z_{ja}^{R,*} Z_{ka}^E \sum_{b=1}^3 Z_{ib}^{D,*} Z_{lb}^U \right. \\ & + 2v_u Z_{j1}^{R,*} \sum_{b=1}^3 Z_{ib}^{D,*} \sum_{a=1}^3 Y_{u,ab} Z_{l3+a}^U \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^E \\ & + 4\sqrt{2} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Y_{e,ab} Z_{k3+a}^E \sum_{d=1}^3 \sum_{c=1}^3 Y_{d,cd}^* Z_{i3+c}^{D,*} Z_{ld}^U \\ & \left. + 2v_u \sum_{b=1}^3 Z_{ib}^{D,*} \sum_{a=1}^3 Y_{u,ab} Z_{l3+a}^U \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{R,*} Z_{k1}^E \right) \end{aligned} \quad (404)$$


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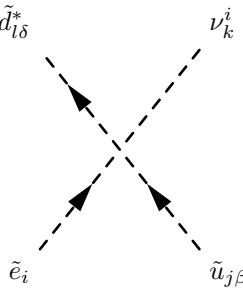


$$\begin{aligned}
& - \frac{i}{4} \left( 2 \left( 2 \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Z_{ia}^{E,*} Q_{\nu,ab} + 2 \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 Z_{ja}^{E,*} Q_{\nu,ab} \right) \right. \\
& + \sqrt{2} v_d \left( \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ab} + \sum_{c=1}^3 Z_{i3+c}^{E,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ab} \right) \Big) Z_{k2}^+ Z_{l2}^+ \\
& + \sqrt{2} \sum_{c=1}^3 Z_{j3+c}^{E,*} \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ba} \left( v_u Z_{k1}^+ Z_{l2}^+ + Z_{k2}^+ \left( 2v_d Z_{l2}^+ + v_u Z_{l1}^+ \right) \right) \\
& \left. + \sqrt{2} \sum_{c=1}^3 Z_{i3+c}^{E,*} \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Y_{e,ca}^* \kappa_{\nu,ba} \left( v_u Z_{k1}^+ Z_{l2}^+ + Z_{k2}^+ \left( 2v_d Z_{l2}^+ + v_u Z_{l1}^+ \right) \right) \right) \quad (405)
\end{aligned}$$



$$\begin{aligned}
& - \frac{i}{8} \left( g_1^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{la}^E \sum_{b=1}^3 Z_{jb}^{E,*} Z_{kb}^E + g_2^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{la}^E \sum_{b=1}^3 Z_{jb}^{E,*} Z_{kb}^E \right. \\
& - 2g_1^2 \sum_{a=1}^3 Z_{i3+a}^{E,*} Z_{l3+a}^E \sum_{b=1}^3 Z_{jb}^{E,*} Z_{kb}^E \\
& - 2g_1^2 \sum_{a=1}^3 Z_{j3+a}^{E,*} Z_{l3+a}^E \left( - 2 \sum_{b=1}^3 Z_{i3+b}^{E,*} Z_{k3+b}^E + \sum_{b=1}^3 Z_{ib}^{E,*} Z_{kb}^E \right) \\
& \left. + \sum_{a=1}^3 Z_{ja}^{E,*} Z_{la}^E \left( - 2g_1^2 \sum_{b=1}^3 Z_{i3+b}^{E,*} Z_{k3+b}^E + (g_1^2 + g_2^2) \sum_{b=1}^3 Z_{ib}^{E,*} Z_{kb}^E \right) \right)
\end{aligned}$$

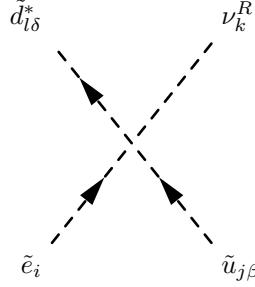
$$\begin{aligned}
& -2g_1^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{la}^E \sum_{b=1}^3 Z_{j3+b}^{E,*} Z_{k3+b}^E + 4g_1^2 \sum_{a=1}^3 Z_{i3+a}^{E,*} Z_{l3+a}^E \sum_{b=1}^3 Z_{j3+b}^{E,*} Z_{k3+b}^E \\
& + g_1^2 \sum_{a=1}^3 Z_{ja}^{E,*} Z_{ka}^E \sum_{b=1}^3 Z_{ib}^{E,*} Z_{lb}^E + g_2^2 \sum_{a=1}^3 Z_{ja}^{E,*} Z_{ka}^E \sum_{b=1}^3 Z_{ib}^{E,*} Z_{lb}^E \\
& - 2g_1^2 \sum_{a=1}^3 Z_{j3+a}^{E,*} Z_{k3+a}^E \sum_{b=1}^3 Z_{ib}^{E,*} Z_{lb}^E + g_1^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ka}^E \sum_{b=1}^3 Z_{jb}^{E,*} Z_{lb}^E \\
& + g_2^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ka}^E \sum_{b=1}^3 Z_{jb}^{E,*} Z_{lb}^E - 2g_1^2 \sum_{a=1}^3 Z_{i3+a}^{E,*} Z_{k3+a}^E \sum_{b=1}^3 Z_{jb}^{E,*} Z_{lb}^E \\
& - 2g_1^2 \sum_{a=1}^3 Z_{ja}^{E,*} Z_{ka}^E \sum_{b=1}^3 Z_{i3+b}^{E,*} Z_{l3+b}^E + 4g_1^2 \sum_{a=1}^3 Z_{j3+a}^{E,*} Z_{k3+a}^E \sum_{b=1}^3 Z_{i3+b}^{E,*} Z_{l3+b}^E \\
& - 2g_1^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ka}^E \sum_{b=1}^3 Z_{j3+b}^{E,*} Z_{l3+b}^E + 4g_1^2 \sum_{a=1}^3 Z_{i3+a}^{E,*} Z_{k3+a}^E \sum_{b=1}^3 Z_{j3+b}^{E,*} Z_{l3+b}^E \\
& + 8 \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Y_{e,ab} Z_{l3+a}^E \sum_{d=1}^3 \sum_{c=1}^3 Y_{e,cd}^* Z_{i3+c}^{E,*} Z_{kd}^E \\
& + 8 \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 Y_{e,ab} Z_{l3+a}^E \sum_{d=1}^3 \sum_{c=1}^3 Y_{e,cd}^* Z_{j3+c}^{E,*} Z_{kd}^E \\
& + 8 \sum_{b=1}^3 Z_{jb}^{E,*} \sum_{a=1}^3 Y_{e,ab} Z_{k3+a}^E \sum_{d=1}^3 \sum_{c=1}^3 Y_{e,cd}^* Z_{i3+c}^{E,*} Z_{ld}^E \\
& + 8 \sum_{b=1}^3 Z_{ib}^{E,*} \sum_{a=1}^3 Y_{e,ab} Z_{k3+a}^E \sum_{d=1}^3 \sum_{c=1}^3 Y_{e,cd}^* Z_{j3+c}^{E,*} Z_{ld}^E \Big) \tag{406}
\end{aligned}$$



$$\begin{aligned}
& -\frac{1}{8} \delta_{\beta\delta} \left( \sqrt{2} g_2^2 \sum_{a=1}^3 Z_{ja}^{U,*} Z_{la}^D \sum_{b=1}^3 Z_{ib}^{E,*} Z_{kb}^{i,*} + \sqrt{2} g_2^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ka}^{i,*} \sum_{b=1}^3 Z_{jb}^{U,*} Z_{lb}^D \right. \\
& \left. + 4\sqrt{2} \sum_{b=1}^3 Z_{jb}^{U,*} \sum_{a=1}^3 Y_{d,ab} Z_{l3+a}^D \sum_{d=1}^3 Z_{kd}^{i,*} \sum_{c=1}^3 Y_{e,cd}^* Z_{i3+c}^{E,*} \right)
\end{aligned}$$

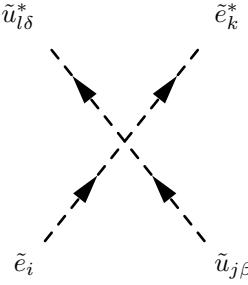
$$- 2v_u \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ia}^{E,*} \kappa_{\nu,ab} \sum_{c=1}^3 Y_{u,c1}^* Z_{j3+c}^{U,*} Z_{l1}^D \Big) \quad (407)$$


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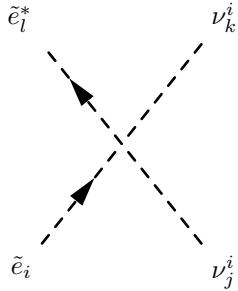
$$\begin{aligned} & - \frac{i}{8} \delta_{\beta\delta} \left( \sqrt{2} g_2^2 \sum_{a=1}^3 Z_{ja}^{U,*} Z_{la}^D \sum_{b=1}^3 Z_{ib}^{E,*} Z_{kb}^{R,*} + \sqrt{2} g_2^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ka}^{R,*} \sum_{b=1}^3 Z_{jb}^{U,*} Z_{lb}^D \right. \\ & + 4\sqrt{2} \sum_{b=1}^3 Z_{jb}^{U,*} \sum_{a=1}^3 Y_{d,ab} Z_{l3+a}^D \sum_{d=1}^3 Z_{kd}^{R,*} \sum_{c=1}^3 Y_{e,cd}^* Z_{i3+c}^{E,*} \\ & \left. + 2v_u \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ia}^{E,*} \kappa_{\nu,ab} \sum_{c=1}^3 Y_{u,c1}^* Z_{j3+c}^{U,*} Z_{l1}^D \right) \end{aligned} \quad (408)$$


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$$\begin{aligned} & \frac{i}{24} \delta_{\beta\delta} \left( -4g_1^2 \sum_{a=1}^3 Z_{j3+a}^{U,*} Z_{l3+a}^U \left( -2 \sum_{b=1}^3 Z_{i3+b}^{E,*} Z_{k3+b}^E + \sum_{b=1}^3 Z_{ib}^{E,*} Z_{kb}^E \right) \right. \\ & + \sum_{a=1}^3 Z_{ja}^{U,*} Z_{la}^U \left( -2g_1^2 \sum_{b=1}^3 Z_{i3+b}^{E,*} Z_{k3+b}^E + (3g_2^2 + g_1^2) \sum_{b=1}^3 Z_{ib}^{E,*} Z_{kb}^E \right) \\ & \left. + g_1^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ka}^E \sum_{b=1}^3 Z_{jb}^{U,*} Z_{lb}^U + 3g_2^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ka}^E \sum_{b=1}^3 Z_{jb}^{U,*} Z_{lb}^U \right) \end{aligned}$$

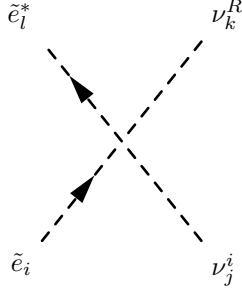
$$\begin{aligned}
& -2g_1^2 \sum_{a=1}^3 Z_{i3+a}^{E,*} Z_{k3+a}^E \sum_{b=1}^3 Z_{jb}^{U,*} Z_{lb}^U - 4g_1^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ka}^E \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{l3+b}^U \\
& + 8g_1^2 \sum_{a=1}^3 Z_{i3+a}^{E,*} Z_{k3+a}^E \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{l3+b}^U \Big)
\end{aligned} \tag{409}$$



$$\begin{aligned}
& -\frac{i}{16} \left( 2g_2^2 \sum_{a=1}^3 Z_{ka}^{i,*} Z_{la}^E \sum_{b=1}^3 Z_{ib}^{E,*} Z_{jb}^{i,*} + 2g_2^2 \sum_{a=1}^3 Z_{ja}^{i,*} Z_{la}^E \sum_{b=1}^3 Z_{ib}^{E,*} Z_{kb}^{i,*} \right. \\
& + 2g_1^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{la}^E \sum_{b=1}^3 Z_{jb}^{i,*} Z_{kb}^{i,*} - 2g_2^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{la}^E \sum_{b=1}^3 Z_{jb}^{i,*} Z_{kb}^{i,*} \\
& - 4g_1^2 \sum_{a=1}^3 Z_{i3+a}^{E,*} Z_{l3+a}^E \sum_{b=1}^3 Z_{jb}^{i,*} Z_{kb}^{i,*} + 2g_1^2 \sum_{a=1}^3 Z_{ja}^{i,*} Z_{ka}^E \sum_{b=1}^3 Z_{ib}^{E,*} Z_{lb}^E \\
& - 2g_2^2 \sum_{a=1}^3 Z_{ja}^{i,*} Z_{ka}^E \sum_{b=1}^3 Z_{ib}^{E,*} Z_{lb}^E + 2g_2^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ka}^E \sum_{b=1}^3 Z_{jb}^{i,*} Z_{lb}^E \\
& + 2g_2^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ja}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} Z_{lb}^E - 4g_1^2 \sum_{a=1}^3 Z_{ja}^{i,*} Z_{ka}^E \sum_{b=1}^3 Z_{i3+b}^{E,*} Z_{l3+b}^E \\
& + v_u^2 Z_{k1}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ia}^{E,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^E \\
& + v_u^2 Z_{j1}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ia}^{E,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^E \\
& + 8 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Y_{e,ab} Z_{l3+a}^E \sum_{d=1}^3 Z_{jd}^{i,*} \sum_{c=1}^3 Y_{e,cd}^* Z_{i3+c}^{E,*} \\
& + 8 \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Y_{e,ab} Z_{l3+a}^E \sum_{d=1}^3 Z_{kd}^{i,*} \sum_{c=1}^3 Y_{e,cd}^* Z_{i3+c}^{E,*} \\
& + v_u^2 \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ia}^{E,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} Z_{l1}^E
\end{aligned}$$

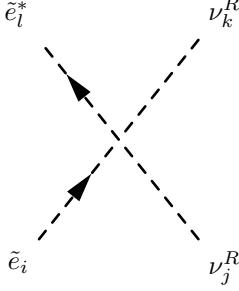
$$+ v_u^2 \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ia}^{E,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{i,*} Z_{l1}^E \Big) \quad (410)$$


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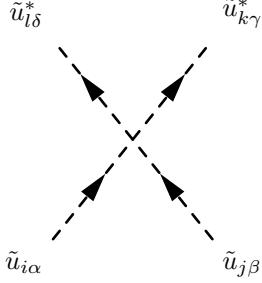


$$\begin{aligned} & \frac{1}{16} \Big( -2g_2^2 \sum_{a=1}^3 Z_{ka}^{R,*} Z_{la}^E \sum_{b=1}^3 Z_{ib}^{E,*} Z_{jb}^{i,*} + 2g_2^2 \sum_{a=1}^3 Z_{ja}^{i,*} Z_{la}^E \sum_{b=1}^3 Z_{ib}^{E,*} Z_{kb}^{R,*} \\ & + 2g_2^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ka}^{R,*} \sum_{b=1}^3 Z_{jb}^{i,*} Z_{lb}^E - 2g_2^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ja}^{i,*} \sum_{b=1}^3 Z_{kb}^{R,*} Z_{lb}^E \\ & + v_u^2 Z_{k1}^{R,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ia}^{E,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^E \\ & - v_u^2 Z_{j1}^{i,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ia}^{E,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^E \\ & - 8 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{e,ab} Z_{l3+a}^E \sum_{d=1}^3 Z_{jd}^{i,*} \sum_{c=1}^3 Y_{e,cd}^* Z_{i3+c}^{E,*} \\ & + 8 \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Y_{e,ab} Z_{l3+a}^E \sum_{d=1}^3 Z_{kd}^{R,*} \sum_{c=1}^3 Y_{e,cd}^* Z_{i3+c}^{E,*} \\ & - v_u^2 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ia}^{E,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} Z_{l1}^E \\ & + v_u^2 \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ia}^{E,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} Z_{l1}^E \Big) \end{aligned} \quad (411)$$


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$$\begin{aligned}
& -\frac{i}{16} \left( 2g_2^2 \sum_{a=1}^3 Z_{ka}^{R,*} Z_{la}^E \sum_{b=1}^3 Z_{ib}^{E,*} Z_{jb}^{R,*} + 2g_2^2 \sum_{a=1}^3 Z_{ja}^{R,*} Z_{la}^E \sum_{b=1}^3 Z_{ib}^{E,*} Z_{kb}^{R,*} \right. \\
& + 2g_1^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{la}^E \sum_{b=1}^3 Z_{jb}^{R,*} Z_{kb}^{R,*} - 2g_2^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{la}^E \sum_{b=1}^3 Z_{jb}^{R,*} Z_{kb}^{R,*} \\
& - 4g_1^2 \sum_{a=1}^3 Z_{i3+a}^{E,*} Z_{l3+a}^E \sum_{b=1}^3 Z_{jb}^{R,*} Z_{kb}^{R,*} + 2g_1^2 \sum_{a=1}^3 Z_{ja}^{R,*} Z_{ka}^{R,*} \sum_{b=1}^3 Z_{ib}^{E,*} Z_{lb}^E \\
& - 2g_2^2 \sum_{a=1}^3 Z_{ja}^{R,*} Z_{ka}^{R,*} \sum_{b=1}^3 Z_{ib}^{E,*} Z_{lb}^E + 2g_2^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ka}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} Z_{lb}^E \\
& + 2g_2^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ja}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} Z_{lb}^E - 4g_1^2 \sum_{a=1}^3 Z_{ja}^{R,*} Z_{ka}^{R,*} \sum_{b=1}^3 Z_{i3+b}^{E,*} Z_{l3+b}^E \\
& + v_u^2 Z_{k1}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ia}^{E,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^E \\
& + v_u^2 Z_{j1}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ia}^{E,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^E \\
& + 8 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Y_{e,ab} Z_{l3+a}^E \sum_{d=1}^3 Z_{jd}^{R,*} \sum_{c=1}^3 Y_{e,cd}^* Z_{i3+c}^{E,*} \\
& + 8 \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Y_{e,ab} Z_{l3+a}^E \sum_{d=1}^3 Z_{kd}^{R,*} \sum_{c=1}^3 Y_{e,cd}^* Z_{i3+c}^{E,*} \\
& + v_u^2 \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ia}^{E,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{R,*} Z_{l1}^E \\
& \left. + v_u^2 \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ia}^{E,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} Z_{l1}^E \right) \tag{412}
\end{aligned}$$

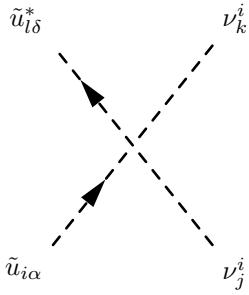


$$\begin{aligned}
& -\frac{i}{72} \left( \delta_{\alpha\delta} \delta_{\beta\gamma} \left( g_1^2 \sum_{a=1}^3 Z_{ia}^{U,*} Z_{la}^U \sum_{b=1}^3 Z_{jb}^{U,*} Z_{kb}^U + 9g_2^2 \sum_{a=1}^3 Z_{ia}^{U,*} Z_{la}^U \sum_{b=1}^3 Z_{jb}^{U,*} Z_{kb}^U \right. \right. \\
& - 6g_3^2 \sum_{a=1}^3 Z_{ia}^{U,*} Z_{la}^U \sum_{b=1}^3 Z_{jb}^{U,*} Z_{kb}^U - 4g_1^2 \sum_{a=1}^3 Z_{i3+a}^{U,*} Z_{l3+a}^U \sum_{b=1}^3 Z_{jb}^{U,*} Z_{kb}^U \\
& + 6g_3^2 \sum_{a=1}^3 Z_{i3+a}^{U,*} Z_{l3+a}^U \sum_{b=1}^3 Z_{jb}^{U,*} Z_{kb}^U \\
& \left. \left. + 18g_3^2 \sum_{a=1}^3 Z_{ja}^{U,*} Z_{la}^U \left( - \sum_{b=1}^3 Z_{i3+b}^{U,*} Z_{k3+b}^U + \sum_{b=1}^3 Z_{ib}^{U,*} Z_{kb}^U \right) \right. \right. \\
& - 18g_3^2 \sum_{a=1}^3 Z_{j3+a}^{U,*} Z_{l3+a}^U \left( - \sum_{b=1}^3 Z_{i3+b}^{U,*} Z_{k3+b}^U + \sum_{b=1}^3 Z_{ib}^{U,*} Z_{kb}^U \right) \\
& - 4g_1^2 \sum_{a=1}^3 Z_{ia}^{U,*} Z_{la}^U \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{k3+b}^U + 6g_3^2 \sum_{a=1}^3 Z_{ia}^{U,*} Z_{la}^U \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{k3+b}^U \\
& + 16g_1^2 \sum_{a=1}^3 Z_{i3+a}^{U,*} Z_{l3+a}^U \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{k3+b}^U - 6g_3^2 \sum_{a=1}^3 Z_{i3+a}^{U,*} Z_{l3+a}^U \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{k3+b}^U \\
& + g_1^2 \sum_{a=1}^3 Z_{ja}^{U,*} Z_{ka}^U \sum_{b=1}^3 Z_{ib}^{U,*} Z_{lb}^U + 9g_2^2 \sum_{a=1}^3 Z_{ja}^{U,*} Z_{ka}^U \sum_{b=1}^3 Z_{ib}^{U,*} Z_{lb}^U \\
& - 6g_3^2 \sum_{a=1}^3 Z_{ja}^{U,*} Z_{ka}^U \sum_{b=1}^3 Z_{ib}^{U,*} Z_{lb}^U - 4g_1^2 \sum_{a=1}^3 Z_{j3+a}^{U,*} Z_{k3+a}^U \sum_{b=1}^3 Z_{ib}^{U,*} Z_{lb}^U \\
& + 6g_3^2 \sum_{a=1}^3 Z_{j3+a}^{U,*} Z_{k3+a}^U \sum_{b=1}^3 Z_{ib}^{U,*} Z_{lb}^U + 18g_3^2 \sum_{a=1}^3 Z_{ia}^{U,*} Z_{ka}^U \sum_{b=1}^3 Z_{jb}^{U,*} Z_{lb}^U \\
& - 18g_3^2 \sum_{a=1}^3 Z_{i3+a}^{U,*} Z_{k3+a}^U \sum_{b=1}^3 Z_{jb}^{U,*} Z_{lb}^U - 4g_1^2 \sum_{a=1}^3 Z_{ja}^{U,*} Z_{ka}^U \sum_{b=1}^3 Z_{i3+b}^{U,*} Z_{l3+b}^U \\
& + 6g_3^2 \sum_{a=1}^3 Z_{ja}^{U,*} Z_{ka}^U \sum_{b=1}^3 Z_{i3+b}^{U,*} Z_{l3+b}^U + 16g_1^2 \sum_{a=1}^3 Z_{j3+a}^{U,*} Z_{k3+a}^U \sum_{b=1}^3 Z_{i3+b}^{U,*} Z_{l3+b}^U
\end{aligned}$$

$$\begin{aligned}
& - 6g_3^2 \sum_{a=1}^3 Z_{j3+a}^{U,*} Z_{k3+a}^U \sum_{b=1}^3 Z_{i3+b}^{U,*} Z_{l3+b}^U - 18g_3^2 \sum_{a=1}^3 Z_{ia}^{U,*} Z_{ka}^U \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{l3+b}^U \\
& + 18g_3^2 \sum_{a=1}^3 Z_{i3+a}^{U,*} Z_{k3+a}^U \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{l3+b}^U \\
& + 72 \sum_{b=1}^3 Z_{ib}^{U,*} \sum_{a=1}^3 Y_{u,ab} Z_{l3+a}^U \sum_{d=1}^3 \sum_{c=1}^3 Y_{u,cd}^* Z_{j3+c}^{U,*} Z_{kd}^U \\
& + 72 \sum_{b=1}^3 Z_{jb}^{U,*} \sum_{a=1}^3 Y_{u,ab} Z_{k3+a}^U \sum_{d=1}^3 \sum_{c=1}^3 Y_{u,cd}^* Z_{i3+c}^{U,*} Z_{ld}^U \\
& + \delta_{\alpha\gamma}\delta_{\beta\delta} \left( 18g_3^2 \sum_{a=1}^3 Z_{ia}^{U,*} Z_{la}^U \sum_{b=1}^3 Z_{jb}^{U,*} Z_{kb}^U - 18g_3^2 \sum_{a=1}^3 Z_{i3+a}^{U,*} Z_{l3+a}^U \sum_{b=1}^3 Z_{jb}^{U,*} Z_{kb}^U \right. \\
& \quad \left. + \sum_{a=1}^3 Z_{j3+a}^{U,*} Z_{l3+a}^U \left( 2(-3g_3^2 + 8g_1^2) \sum_{b=1}^3 Z_{i3+b}^{U,*} Z_{k3+b}^U + (-4g_1^2 + 6g_3^2) \sum_{b=1}^3 Z_{ib}^{U,*} Z_{kb}^U \right) \right. \\
& \quad \left. + \sum_{a=1}^3 Z_{ja}^{U,*} Z_{la}^U \left( 2(-2g_1^2 + 3g_3^2) \sum_{b=1}^3 Z_{i3+b}^{U,*} Z_{k3+b}^U + (-6g_3^2 + 9g_2^2 + g_1^2) \sum_{b=1}^3 Z_{ib}^{U,*} Z_{kb}^U \right) \right. \\
& \quad \left. - 18g_3^2 \sum_{a=1}^3 Z_{ia}^{U,*} Z_{la}^U \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{k3+b}^U + 18g_3^2 \sum_{a=1}^3 Z_{i3+a}^{U,*} Z_{l3+a}^U \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{k3+b}^U \right. \\
& \quad \left. + 18g_3^2 \sum_{a=1}^3 Z_{ja}^{U,*} Z_{ka}^U \sum_{b=1}^3 Z_{ib}^{U,*} Z_{lb}^U - 18g_3^2 \sum_{a=1}^3 Z_{j3+a}^{U,*} Z_{k3+a}^U \sum_{b=1}^3 Z_{ib}^{U,*} Z_{lb}^U \right. \\
& \quad \left. + g_1^2 \sum_{a=1}^3 Z_{ia}^{U,*} Z_{ka}^U \sum_{b=1}^3 Z_{jb}^{U,*} Z_{lb}^U + 9g_2^2 \sum_{a=1}^3 Z_{ia}^{U,*} Z_{ka}^U \sum_{b=1}^3 Z_{jb}^{U,*} Z_{lb}^U \right. \\
& \quad \left. - 6g_3^2 \sum_{a=1}^3 Z_{ia}^{U,*} Z_{ka}^U \sum_{b=1}^3 Z_{jb}^{U,*} Z_{lb}^U - 4g_1^2 \sum_{a=1}^3 Z_{i3+a}^{U,*} Z_{k3+a}^U \sum_{b=1}^3 Z_{jb}^{U,*} Z_{lb}^U \right. \\
& \quad \left. + 6g_3^2 \sum_{a=1}^3 Z_{i3+a}^{U,*} Z_{k3+a}^U \sum_{b=1}^3 Z_{jb}^{U,*} Z_{lb}^U - 18g_3^2 \sum_{a=1}^3 Z_{ja}^{U,*} Z_{ka}^U \sum_{b=1}^3 Z_{i3+b}^{U,*} Z_{l3+b}^U \right. \\
& \quad \left. + 18g_3^2 \sum_{a=1}^3 Z_{j3+a}^{U,*} Z_{k3+a}^U \sum_{b=1}^3 Z_{i3+b}^{U,*} Z_{l3+b}^U - 4g_1^2 \sum_{a=1}^3 Z_{ia}^{U,*} Z_{ka}^U \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{l3+b}^U \right. \\
& \quad \left. + 6g_3^2 \sum_{a=1}^3 Z_{ia}^{U,*} Z_{ka}^U \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{l3+b}^U + 16g_1^2 \sum_{a=1}^3 Z_{i3+a}^{U,*} Z_{k3+a}^U \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{l3+b}^U \right. \\
& \quad \left. - 6g_3^2 \sum_{a=1}^3 Z_{i3+a}^{U,*} Z_{k3+a}^U \sum_{b=1}^3 Z_{j3+b}^{U,*} Z_{l3+b}^U \right)
\end{aligned}$$

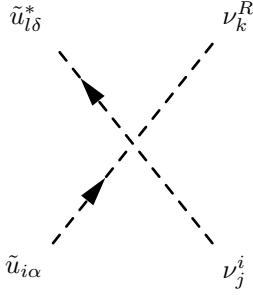
$$\begin{aligned}
& + 72 \sum_{b=1}^3 Z_{jb}^{U,*} \sum_{a=1}^3 Y_{u,ab} Z_{l3+a}^U \sum_{d=1}^3 \sum_{c=1}^3 Y_{u,cd}^* Z_{i3+c}^{U,*} Z_{kd}^U \\
& + 72 \sum_{b=1}^3 Z_{ib}^{U,*} \sum_{a=1}^3 Y_{u,ab} Z_{k3+a}^U \sum_{d=1}^3 \sum_{c=1}^3 Y_{u,cd}^* Z_{j3+c}^{U,*} Z_{ld}^U \Big) \Big) \tag{413}
\end{aligned}$$


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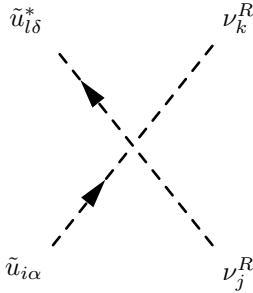
$$\begin{aligned}
& \frac{i}{24} \delta_{\alpha\delta} \left( \left( -3g_2^2 + g_1^2 \right) \sum_{a=1}^3 Z_{ia}^{U,*} Z_{la}^U \sum_{b=1}^3 Z_{jb}^{i,*} Z_{kb}^{i,*} - 4g_1^2 \sum_{a=1}^3 Z_{i3+a}^{U,*} Z_{l3+a}^U \sum_{b=1}^3 Z_{jb}^{i,*} Z_{kb}^{i,*} \right. \\
& + g_1^2 \sum_{a=1}^3 Z_{ja}^{i,*} Z_{ka}^{i,*} \sum_{b=1}^3 Z_{ib}^{U,*} Z_{lb}^U - 3g_2^2 \sum_{a=1}^3 Z_{ja}^{i,*} Z_{ka}^{i,*} \sum_{b=1}^3 Z_{ib}^{U,*} Z_{lb}^U \\
& - 4g_1^2 \sum_{a=1}^3 Z_{ja}^{i,*} Z_{ka}^{i,*} \sum_{b=1}^3 Z_{i3+b}^{U,*} Z_{l3+b}^U \\
& + 6\sqrt{2}v_u Z_{k1}^{i,*} \sum_{b=1}^3 Z_{ib}^{U,*} \sum_{a=1}^3 Y_{u,ab} Z_{l3+a}^U \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} \\
& + 6\sqrt{2}v_u Z_{j1}^{i,*} \sum_{b=1}^3 Z_{ib}^{U,*} \sum_{a=1}^3 Y_{u,ab} Z_{l3+a}^U \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{i,*} \\
& + 3\sqrt{2}v_u \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 Y_{u,c1}^* Z_{i3+c}^{U,*} Z_{l1}^U \\
& \left. + 3\sqrt{2}v_u \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 Y_{u,c1}^* Z_{i3+c}^{U,*} Z_{l1}^U \right) \tag{414}
\end{aligned}$$


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$$\begin{aligned}
& \frac{1}{4} \frac{1}{\sqrt{2}} v_u \delta_{\alpha\delta} \left( -2 Z_{k1}^{R,*} \sum_{b=1}^3 Z_{ib}^{U,*} \sum_{a=1}^3 Y_{u,ab} Z_{l3+a}^U \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} \right. \\
& - 2 Z_{j1}^{i,*} \sum_{b=1}^3 Z_{ib}^{U,*} \sum_{a=1}^3 Y_{u,ab} Z_{l3+a}^U \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} \\
& \left. + \left( \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} + \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \right) \sum_{c=1}^3 Y_{u,c1}^* Z_{i3+c}^{U,*} Z_{l1}^U \right) \tag{415}
\end{aligned}$$

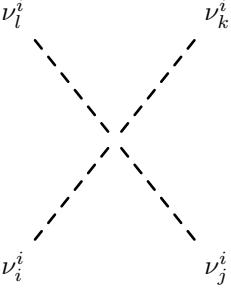

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$$\begin{aligned}
& \frac{i}{24} \delta_{\alpha\delta} \left( \left( -3g_2^2 + g_1^2 \right) \sum_{a=1}^3 Z_{ia}^{U,*} Z_{la}^U \sum_{b=1}^3 Z_{jb}^{R,*} Z_{kb}^{R,*} - 4g_1^2 \sum_{a=1}^3 Z_{i3+a}^{U,*} Z_{l3+a}^U \sum_{b=1}^3 Z_{jb}^{R,*} Z_{kb}^{R,*} \right. \\
& + g_1^2 \sum_{a=1}^3 Z_{ja}^{R,*} Z_{ka}^{R,*} \sum_{b=1}^3 Z_{ib}^{U,*} Z_{lb}^U - 3g_2^2 \sum_{a=1}^3 Z_{ja}^{R,*} Z_{ka}^{R,*} \sum_{b=1}^3 Z_{ib}^{U,*} Z_{lb}^U \\
& - 4g_1^2 \sum_{a=1}^3 Z_{ja}^{R,*} Z_{ka}^{R,*} \sum_{b=1}^3 Z_{i3+b}^{U,*} Z_{l3+b}^U \\
& - 6\sqrt{2} v_u Z_{k1}^{R,*} \sum_{b=1}^3 Z_{ib}^{U,*} \sum_{a=1}^3 Y_{u,ab} Z_{l3+a}^U \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{R,*} \\
& \left. - 6\sqrt{2} v_u Z_{j1}^{R,*} \sum_{b=1}^3 Z_{ib}^{U,*} \sum_{a=1}^3 Y_{u,ab} Z_{l3+a}^U \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} \right)
\end{aligned}$$

$$\begin{aligned}
& -3\sqrt{2}v_u \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 Y_{u,c1}^* Z_{i3+c}^{U,*} Z_{l1}^U \\
& - 3\sqrt{2}v_u \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 Y_{u,c1}^* Z_{i3+c}^{U,*} Z_{l1}^U
\end{aligned} \tag{416}$$


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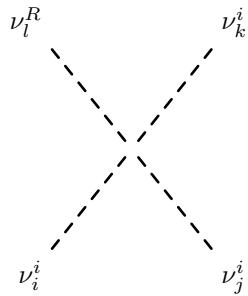


$$\begin{aligned}
& -\frac{i}{16} \left( 2(g_1^2 + g_2^2) \sum_{a=1}^3 Z_{ka}^{i,*} Z_{la}^{i,*} \sum_{b=1}^3 Z_{ib}^{i,*} Z_{jb}^{i,*} + 2(g_1^2 + g_2^2) \sum_{a=1}^3 Z_{ja}^{i,*} Z_{la}^{i,*} \sum_{b=1}^3 Z_{ib}^{i,*} Z_{kb}^{i,*} \right. \\
& + 2g_1^2 \sum_{a=1}^3 Z_{ia}^{i,*} Z_{la}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} Z_{kb}^{i,*} + 2g_2^2 \sum_{a=1}^3 Z_{ia}^{i,*} Z_{la}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} Z_{kb}^{i,*} \\
& + 2g_1^2 \sum_{a=1}^3 Z_{ja}^{i,*} Z_{ka}^{i,*} \sum_{b=1}^3 Z_{ib}^{i,*} Z_{lb}^{i,*} + 2g_2^2 \sum_{a=1}^3 Z_{ja}^{i,*} Z_{ka}^{i,*} \sum_{b=1}^3 Z_{ib}^{i,*} Z_{lb}^{i,*} \\
& + 2g_1^2 \sum_{a=1}^3 Z_{ia}^{i,*} Z_{ka}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} Z_{lb}^{i,*} + 2g_2^2 \sum_{a=1}^3 Z_{ia}^{i,*} Z_{ka}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} Z_{lb}^{i,*} \\
& + 2g_1^2 \sum_{a=1}^3 Z_{ia}^{i,*} Z_{ja}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} Z_{lb}^{i,*} + 2g_2^2 \sum_{a=1}^3 Z_{ia}^{i,*} Z_{ja}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} Z_{lb}^{i,*} \\
& + v_u^2 Z_{l1}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} \\
& + v_u^2 Z_{k1}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} \\
& + v_u^2 Z_{l1}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} \\
& + v_u^2 Z_{j1}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} \\
& + v_u^2 Z_{k1}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{la}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*}
\end{aligned}$$

$$\begin{aligned}
& + v_u^2 Z_{j1}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{la}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} \\
& + v_u^2 Z_{l1}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} \\
& + v_u^2 Z_{k1}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} \\
& + v_u^2 Z_{l1}^{i,*} \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} \\
& + v_u^2 Z_{i1}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} \\
& + v_u^2 Z_{k1}^{i,*} \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{la}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} \\
& + v_u^2 Z_{i1}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{la}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} \\
& + v_u^2 Z_{l1}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{i,*} \\
& + v_u^2 Z_{j1}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{i,*} \\
& + v_u^2 Z_{l1}^{i,*} \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{i,*} \\
& + v_u^2 Z_{i1}^{i,*} \sum_{b=1}^3 Z_{lb}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{i,*} \\
& + v_u^2 Z_{j1}^{i,*} \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{la}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{i,*} \\
& + v_u^2 Z_{i1}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{la}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{i,*} \\
& + v_u^2 Z_{k1}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{i,*} \\
& + v_u^2 Z_{j1}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{i,*}
\end{aligned}$$

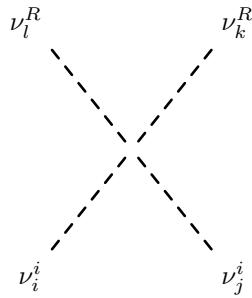
$$\begin{aligned}
& + v_u^2 Z_{k1}^{i,*} \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{i,*} \\
& + v_u^2 Z_{i1}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{i,*} \\
& + v_u^2 Z_{j1}^{i,*} \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{i,*} \\
& + v_u^2 Z_{i1}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{i,*} \Big) \tag{417}
\end{aligned}$$


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$$\begin{aligned}
& \frac{1}{16} v_u^2 \Big( - Z_{j1}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} \\
& - Z_{j1}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} \\
& - Z_{i1}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} \\
& - Z_{i1}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} \\
& - Z_{j1}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{i,*} \\
& - Z_{i1}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{i,*} \\
& - Z_{j1}^{i,*} \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{i,*} \\
& - Z_{i1}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{i,*}
\end{aligned}$$

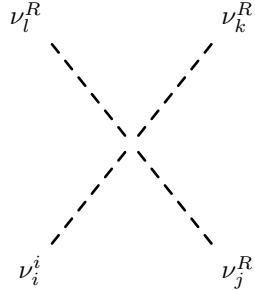
$$\begin{aligned}
& + Z_{l1}^{R,*} \left( \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} + \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} \right. \\
& + \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} + \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} \\
& \left. + \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{i,*} + \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{i,*} \right) \\
& + Z_{j1}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \\
& + Z_{i1}^{i,*} \sum_{b=1}^3 Z_{kb}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \\
& + Z_{j1}^{i,*} \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \\
& + Z_{i1}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \\
& - Z_{k1}^{i,*} \left( \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} + \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} \right. \\
& + \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} + \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} \\
& \left. - \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} - \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \right) \tag{418}
\end{aligned}$$



$$\begin{aligned}
& - \frac{i}{16} \left( 2(g_1^2 + g_2^2) \sum_{a=1}^3 Z_{ka}^{R,*} Z_{la}^{R,*} \sum_{b=1}^3 Z_{ib}^{i,*} Z_{jb}^{i,*} + 2(g_1^2 + g_2^2) \sum_{a=1}^3 Z_{ia}^{i,*} Z_{ja}^{i,*} \sum_{b=1}^3 Z_{kb}^{R,*} Z_{lb}^{R,*} \right. \\
& \left. + v_u^2 \left( -Z_{j1}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} \right. \right)
\end{aligned}$$

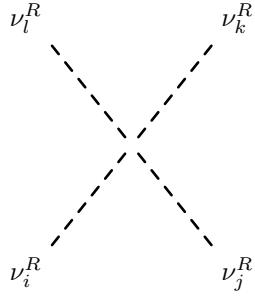
$$\begin{aligned}
& - Z_{j1}^{i,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} \\
& - Z_{i1}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} \\
& - Z_{i1}^{i,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} \\
& + Z_{j1}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} \\
& + Z_{i1}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} \\
& + Z_{j1}^{i,*} \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} \\
& + Z_{i1}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} \\
& + Z_{l1}^{R,*} \left( \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} + \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} \right. \\
& \quad \left. + \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} + \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} \right. \\
& \quad \left. - \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} - \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} \right) \\
& + Z_{j1}^{i,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \\
& + Z_{i1}^{i,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \\
& + Z_{j1}^{i,*} \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \\
& + Z_{i1}^{i,*} \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \\
& + Z_{k1}^{R,*} \left( \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} + \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} \right)
\end{aligned}$$

$$\begin{aligned}
& + \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} + \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{i,*} \\
& - \sum_{b=1}^3 Z_{jb}^{i,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} - \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{ja}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \Big) \Big) \Big) \Big)
\end{aligned} \tag{419}$$



$$\begin{aligned}
& \frac{1}{16} v_u^2 \Big( - Z_{j1}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} \\
& - Z_{j1}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} \\
& - Z_{i1}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{R,*} \\
& - Z_{i1}^{i,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{R,*} \\
& + Z_{j1}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} \\
& - Z_{i1}^{i,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} \\
& + Z_{j1}^{R,*} \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} \\
& - Z_{i1}^{i,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} \\
& + Z_{l1}^{R,*} \Big( - \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} - \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} \\
& + \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{R,*} + \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{R,*}
\end{aligned}$$

$$\begin{aligned}
& + \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} + \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} \Big) \\
& + Z_{j1}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \\
& - Z_{i1}^{i,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \\
& + Z_{j1}^{R,*} \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \\
& - Z_{i1}^{i,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \\
& + Z_{k1}^{R,*} \Big( - \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} - \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{i,*} \\
& + \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{R,*} + \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{R,*} \\
& + \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ia}^{i,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} + \sum_{b=1}^3 Z_{ib}^{i,*} \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \Big) \tag{420}
\end{aligned}$$

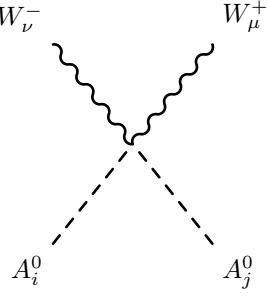


$$\begin{aligned}
& - \frac{i}{16} \left( 2(g_1^2 + g_2^2) \sum_{a=1}^3 Z_{ka}^{R,*} Z_{la}^{R,*} \sum_{b=1}^3 Z_{ib}^{R,*} Z_{jb}^{R,*} + 2(g_1^2 + g_2^2) \sum_{a=1}^3 Z_{ja}^{R,*} Z_{la}^{R,*} \sum_{b=1}^3 Z_{ib}^{R,*} Z_{kb}^{R,*} \right. \\
& + 2g_1^2 \sum_{a=1}^3 Z_{ia}^{R,*} Z_{la}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} Z_{kb}^{R,*} + 2g_2^2 \sum_{a=1}^3 Z_{ia}^{R,*} Z_{la}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} Z_{kb}^{R,*} \\
& + 2g_1^2 \sum_{a=1}^3 Z_{ja}^{R,*} Z_{ka}^{R,*} \sum_{b=1}^3 Z_{ib}^{R,*} Z_{lb}^{R,*} + 2g_2^2 \sum_{a=1}^3 Z_{ja}^{R,*} Z_{ka}^{R,*} \sum_{b=1}^3 Z_{ib}^{R,*} Z_{lb}^{R,*} \\
& \left. + 2g_1^2 \sum_{a=1}^3 Z_{ia}^{R,*} Z_{ka}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} Z_{lb}^{R,*} + 2g_2^2 \sum_{a=1}^3 Z_{ia}^{R,*} Z_{ka}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} Z_{lb}^{R,*} \right)
\end{aligned}$$

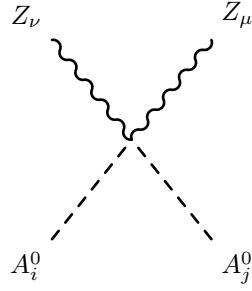
$$\begin{aligned}
& + 2g_1^2 \sum_{a=1}^3 Z_{ia}^{R,*} Z_{ja}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} Z_{lb}^{R,*} + 2g_2^2 \sum_{a=1}^3 Z_{ia}^{R,*} Z_{ja}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} Z_{lb}^{R,*} \\
& + v_u^2 Z_{l1}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{R,*} \\
& + v_u^2 Z_{kl}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{R,*} \\
& + v_u^2 Z_{kl}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{R,*} \\
& + v_u^2 Z_{j1}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{R,*} \\
& + v_u^2 Z_{k1}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{R,*} \\
& + v_u^2 Z_{j1}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{ic}^{R,*} \\
& + v_u^2 Z_{l1}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ia}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{R,*} \\
& + v_u^2 Z_{k1}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ia}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{R,*} \\
& + v_u^2 Z_{l1}^{R,*} \sum_{b=1}^3 Z_{ib}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{R,*} \\
& + v_u^2 Z_{i1}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{R,*} \\
& + v_u^2 Z_{k1}^{R,*} \sum_{b=1}^3 Z_{ib}^{R,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{R,*} \\
& + v_u^2 Z_{i1}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{jc}^{R,*} \\
& + v_u^2 Z_{l1}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ia}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} \\
& + v_u^2 Z_{j1}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ia}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*}
\end{aligned}$$

$$\begin{aligned}
& + v_u^2 Z_{l1}^{R,*} \sum_{b=1}^3 Z_{ib}^{R,*} \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} \\
& + v_u^2 Z_{i1}^{R,*} \sum_{b=1}^3 Z_{lb}^{R,*} \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} \\
& + v_u^2 Z_{j1}^{R,*} \sum_{b=1}^3 Z_{ib}^{R,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} \\
& + v_u^2 Z_{i1}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{la}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{kc}^{R,*} \\
& + v_u^2 Z_{k1}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ia}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \\
& + v_u^2 Z_{j1}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ia}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \\
& + v_u^2 Z_{k1}^{R,*} \sum_{b=1}^3 Z_{ib}^{R,*} \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \\
& + v_u^2 Z_{i1}^{R,*} \sum_{b=1}^3 Z_{kb}^{R,*} \sum_{a=1}^3 Z_{ja}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \\
& + v_u^2 Z_{j1}^{R,*} \sum_{b=1}^3 Z_{ib}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \\
& + v_u^2 Z_{i1}^{R,*} \sum_{b=1}^3 Z_{jb}^{R,*} \sum_{a=1}^3 Z_{ka}^{R,*} \kappa_{\nu,ab} \sum_{c=1}^3 \kappa_{\nu,c1}^* Z_{lc}^{R,*} \Big) \tag{421}
\end{aligned}$$

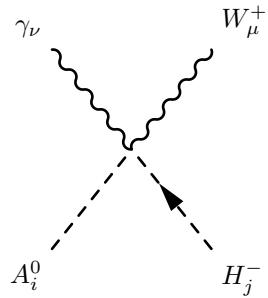
## 9.8 Two Scalar-Two Vector Boson-Interaction



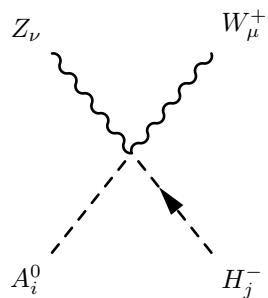
$$\frac{i}{2} g_2^2 \left( Z_{i1}^A Z_{j1}^A + Z_{i2}^A Z_{j2}^A \right) \left( g_{\mu\nu} \right) \tag{422}$$



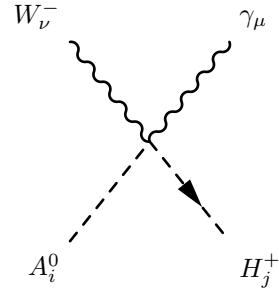
$$\frac{i}{2} \left( g_1 \sin \Theta_W + g_2 \cos \Theta_W \right)^2 \left( Z_{i1}^A Z_{j1}^A + Z_{i2}^A Z_{j2}^A \right) \left( g_{\mu\nu} \right) \quad (423)$$



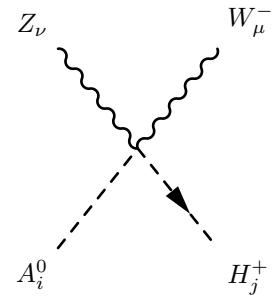
$$- \frac{1}{2} g_1 g_2 \cos \Theta_W \left( Z_{i1}^A Z_{j1}^+ + Z_{i2}^A Z_{j2}^+ \right) \left( g_{\mu\nu} \right) \quad (424)$$



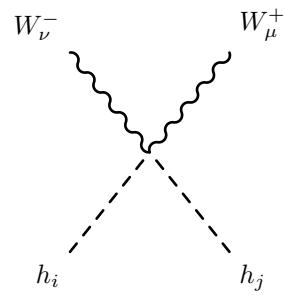
$$\frac{1}{2} g_1 g_2 \sin \Theta_W \left( Z_{i1}^A Z_{j1}^+ + Z_{i2}^A Z_{j2}^+ \right) \left( g_{\mu\nu} \right) \quad (425)$$



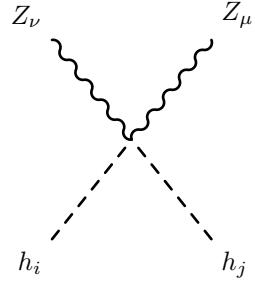
$$\frac{1}{2} g_1 g_2 \cos \Theta_W (Z_{i1}^A Z_{j1}^+ + Z_{i2}^A Z_{j2}^+) (g_{\mu\nu}) \quad (426)$$



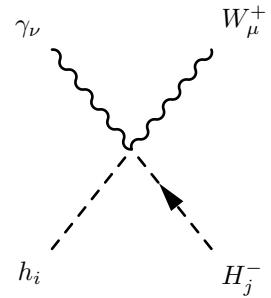
$$- \frac{1}{2} g_1 g_2 \sin \Theta_W (Z_{i1}^A Z_{j1}^+ + Z_{i2}^A Z_{j2}^+) (g_{\mu\nu}) \quad (427)$$



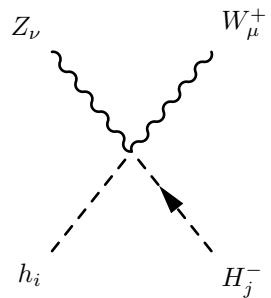
$$\frac{i}{2} g_2^2 (Z_{i1}^H Z_{j1}^H + Z_{i2}^H Z_{j2}^H) (g_{\mu\nu}) \quad (428)$$



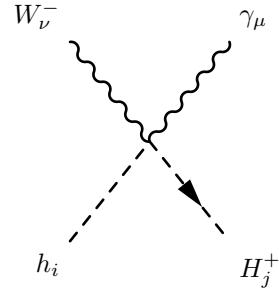
$$\frac{i}{2} \left( g_1 \sin \Theta_W + g_2 \cos \Theta_W \right)^2 \left( Z_{i1}^H Z_{j1}^H + Z_{i2}^H Z_{j2}^H \right) (g_{\mu\nu}) \quad (429)$$



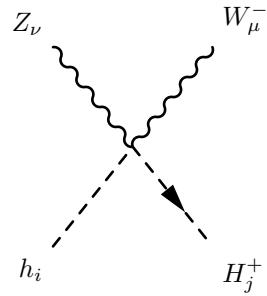
$$- \frac{i}{2} g_1 g_2 \cos \Theta_W \left( Z_{i1}^H Z_{j1}^+ - Z_{i2}^H Z_{j2}^+ \right) (g_{\mu\nu}) \quad (430)$$



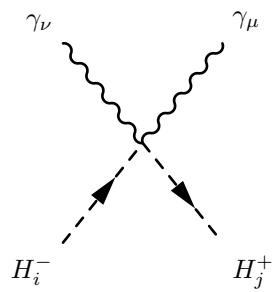
$$\frac{i}{2} g_1 g_2 \sin \Theta_W \left( Z_{i1}^H Z_{j1}^+ - Z_{i2}^H Z_{j2}^+ \right) (g_{\mu\nu}) \quad (431)$$



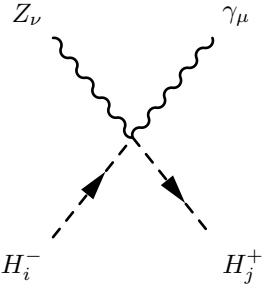
$$-\frac{i}{2} g_1 g_2 \cos \Theta_W \left( Z_{i1}^H Z_{j1}^+ - Z_{i2}^H Z_{j2}^+ \right) (g_{\mu\nu}) \quad (432)$$



$$\frac{i}{2} g_1 g_2 \sin \Theta_W \left( Z_{i1}^H Z_{j1}^+ - Z_{i2}^H Z_{j2}^+ \right) (g_{\mu\nu}) \quad (433)$$

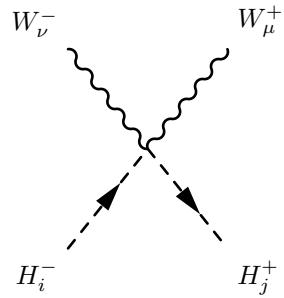


$$\frac{i}{2} \left( g_1 \cos \Theta_W + g_2 \sin \Theta_W \right)^2 \left( Z_{i1}^+ Z_{j1}^+ + Z_{i2}^+ Z_{j2}^+ \right) (g_{\mu\nu}) \quad (434)$$



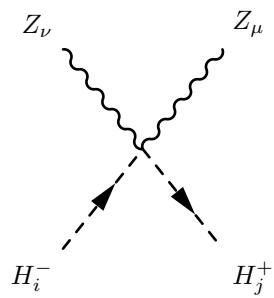
$$-\frac{i}{4} \left( -2g_1 g_2 \cos 2\Theta_W + \left( -g_2^2 + g_1^2 \right) \sin 2\Theta_W \right) \left( Z_{i1}^+ Z_{j1}^+ + Z_{i2}^+ Z_{j2}^+ \right) \left( g_{\mu\nu} \right) \quad (435)$$


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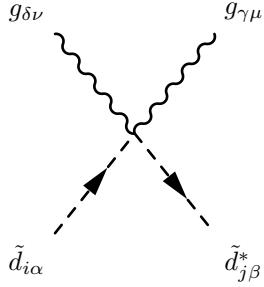
$$\frac{i}{2} g_2^2 \left( Z_{i1}^+ Z_{j1}^+ + Z_{i2}^+ Z_{j2}^+ \right) \left( g_{\mu\nu} \right) \quad (436)$$


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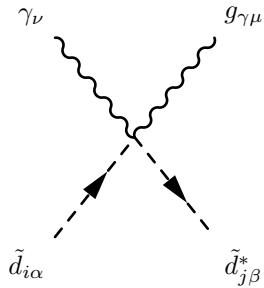
$$\frac{i}{2} \left( -g_1 \sin \Theta_W + g_2 \cos \Theta_W \right)^2 \left( Z_{i1}^+ Z_{j1}^+ + Z_{i2}^+ Z_{j2}^+ \right) \left( g_{\mu\nu} \right) \quad (437)$$


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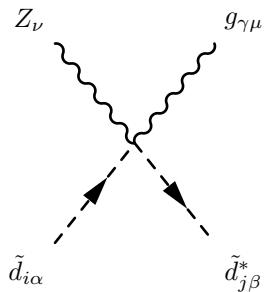
$$\frac{i}{4}g_3^2 \delta_{ij} \left( \sum_{a=1}^3 \lambda_{a,\alpha}^\gamma \lambda_{\beta,a}^\delta + \sum_{a=1}^3 \lambda_{\beta,a}^\gamma \lambda_{a,\alpha}^\delta \right) (g_{\mu\nu}) \quad (438)$$


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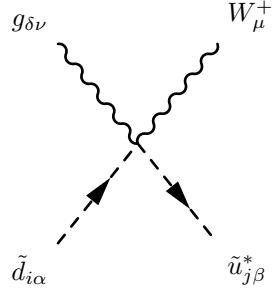
$$\frac{i}{6}g_3 \lambda_{\beta,\alpha}^\gamma \left( -2g_1 \cos \Theta_W \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{j3+a}^D + (-3g_2 \sin \Theta_W + g_1 \cos \Theta_W) \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ja}^D \right) (g_{\mu\nu}) \quad (439)$$


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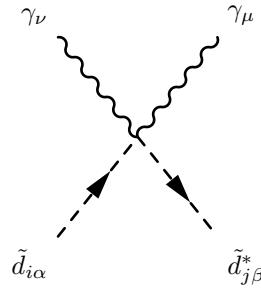
$$-\frac{i}{6}g_3 \lambda_{\beta,\alpha}^\gamma \left( -2g_1 \sin \Theta_W \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{j3+a}^D + (3g_2 \cos \Theta_W + g_1 \sin \Theta_W) \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ja}^D \right) (g_{\mu\nu}) \quad (440)$$


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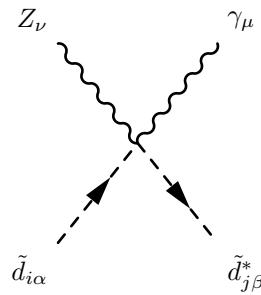
$$i \frac{1}{\sqrt{2}} g_2 g_3 \lambda_{\beta,\alpha}^\delta \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ja}^U(g_{\mu\nu}) \quad (441)$$


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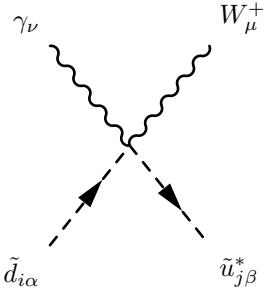
$$\frac{i}{18} \delta_{\alpha\beta} \left( \left( -3g_2 \sin \Theta_W + g_1 \cos \Theta_W \right)^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ja}^D + 4g_1^2 \cos \Theta_W^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{j3+a}^D \right) (g_{\mu\nu}) \quad (442)$$


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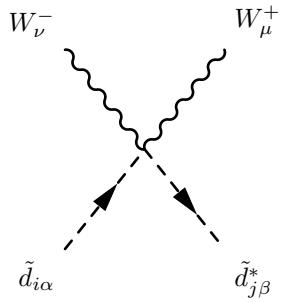
$$\begin{aligned} & - \frac{i}{36} \delta_{\alpha\beta} \left( \left( 6g_1 g_2 \cos 2\Theta_W + (-9g_2^2 + g_1^2) \sin 2\Theta_W \right) \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ja}^D \right. \\ & \left. + 4g_1^2 \sin 2\Theta_W \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{j3+a}^D \right) (g_{\mu\nu}) \end{aligned} \quad (443)$$


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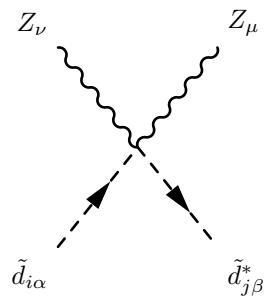
$$\frac{i}{3} \frac{1}{\sqrt{2}} g_1 g_2 \cos \Theta_W \delta_{\alpha\beta} \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ja}^U(g_{\mu\nu}) \quad (444)$$


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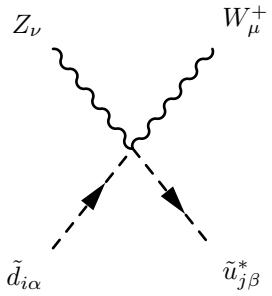
$$\frac{i}{2} g_2^2 \delta_{\alpha\beta} \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ja}^D(g_{\mu\nu}) \quad (445)$$


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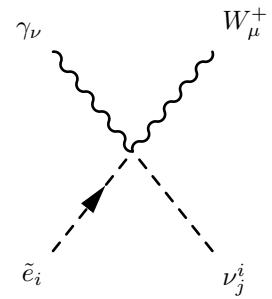
$$\frac{i}{18} \delta_{\alpha\beta} \left( \left( 3g_2 \cos \Theta_W + g_1 \sin \Theta_W \right)^2 \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ja}^D + 4g_1^2 \sin \Theta_W^2 \sum_{a=1}^3 Z_{i3+a}^{D,*} Z_{j3+a}^D \right) (g_{\mu\nu}) \quad (446)$$


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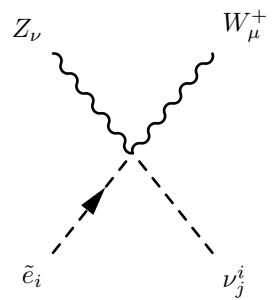
$$-\frac{i}{3} \frac{1}{\sqrt{2}} g_1 g_2 \delta_{\alpha\beta} \sin \Theta_W \sum_{a=1}^3 Z_{ia}^{D,*} Z_{ja}^U(g_{\mu\nu}) \quad (447)$$


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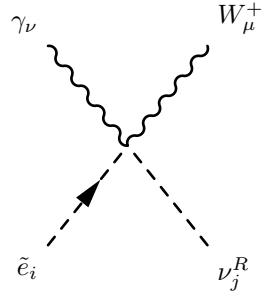
$$-\frac{1}{2} g_1 g_2 \cos \Theta_W \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ja}^{i,*}(g_{\mu\nu}) \quad (448)$$


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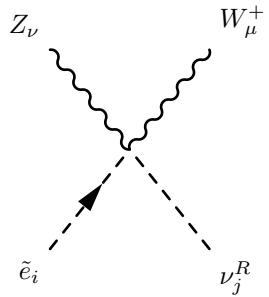
$$\frac{1}{2} g_1 g_2 \sin \Theta_W \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ja}^{i,*}(g_{\mu\nu}) \quad (449)$$


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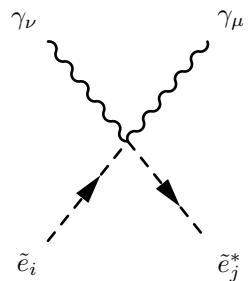
$$-\frac{i}{2}g_1g_2 \cos\Theta_W \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ja}^{R,*}(g_{\mu\nu}) \quad (450)$$


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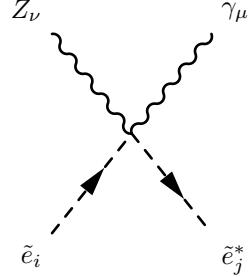
$$\frac{i}{2}g_1g_2 \sin\Theta_W \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ja}^{R,*}(g_{\mu\nu}) \quad (451)$$


---



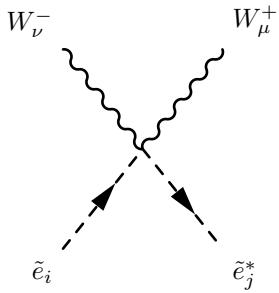
$$\frac{i}{2} \left( 4g_1^2 \cos\Theta_W^2 \sum_{a=1}^3 Z_{i3+a}^{E,*} Z_{j3+a}^E + (g_1 \cos\Theta_W + g_2 \sin\Theta_W)^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ja}^E \right) (g_{\mu\nu}) \quad (452)$$


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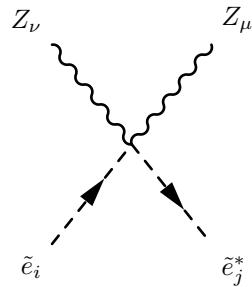
$$\begin{aligned}
& - \frac{i}{4} \left( \left( -2g_1 g_2 \cos 2\Theta_W + \left( -g_2^2 + g_1^2 \right) \sin 2\Theta_W \right) \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ja}^E \right. \\
& \left. + 4g_1^2 \sin 2\Theta_W \sum_{a=1}^3 Z_{i3+a}^{E,*} Z_{j3+a}^E \right) (g_{\mu\nu}) \tag{453}
\end{aligned}$$


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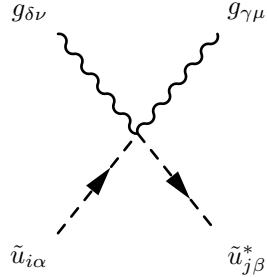
$$\frac{i}{2} g_2^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ja}^E (g_{\mu\nu}) \tag{454}$$


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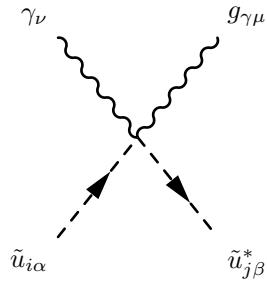
$$\frac{i}{2} \left( 4g_1^2 \sin \Theta_W^2 \sum_{a=1}^3 Z_{i3+a}^{E,*} Z_{j3+a}^E + \left( -g_1 \sin \Theta_W + g_2 \cos \Theta_W \right)^2 \sum_{a=1}^3 Z_{ia}^{E,*} Z_{ja}^E \right) (g_{\mu\nu}) \tag{455}$$


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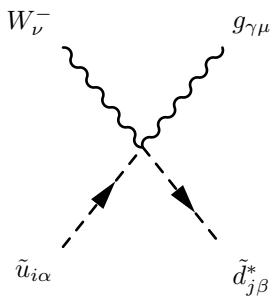
$$\frac{i}{4}g_3^2\delta_{ij}\left(\sum_{a=1}^3\lambda_{a,\alpha}^\gamma\lambda_{\beta,a}^\delta + \sum_{a=1}^3\lambda_{\beta,a}^\gamma\lambda_{a,\alpha}^\delta\right)\left(g_{\mu\nu}\right) \quad (456)$$


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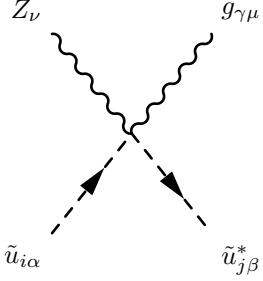
$$\frac{i}{6}g_3\lambda_{\beta,\alpha}^\gamma\left(\left(3g_2\sin\Theta_W + g_1\cos\Theta_W\right)\sum_{a=1}^3Z_{ia}^{U,*}Z_{ja}^U + 4g_1\cos\Theta_W\sum_{a=1}^3Z_{i3+a}^{U,*}Z_{j3+a}^U\right)\left(g_{\mu\nu}\right) \quad (457)$$


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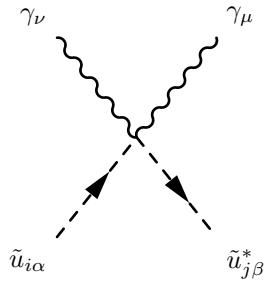
$$i\frac{1}{\sqrt{2}}g_2g_3\lambda_{\beta,\alpha}^\gamma\sum_{a=1}^3Z_{ia}^{U,*}Z_{ja}^D\left(g_{\mu\nu}\right) \quad (458)$$


---



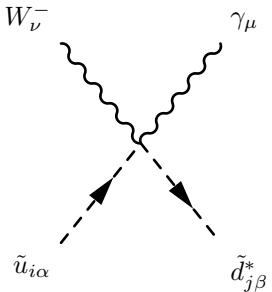
$$\frac{i}{6} g_3 \lambda_{\beta,\alpha}^\gamma \left( (3g_2 \cos \Theta_W - g_1 \sin \Theta_W) \sum_{a=1}^3 Z_{ia}^{U,*} Z_{ja}^U - 4g_1 \sin \Theta_W \sum_{a=1}^3 Z_{i3+a}^{U,*} Z_{j3+a}^U \right) (g_{\mu\nu}) \quad (459)$$


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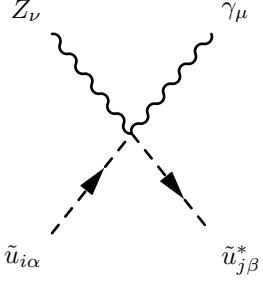
$$\frac{i}{18} \delta_{\alpha\beta} \left( 16g_1^2 \cos \Theta_W^2 \sum_{a=1}^3 Z_{i3+a}^{U,*} Z_{j3+a}^U + (3g_2 \sin \Theta_W + g_1 \cos \Theta_W)^2 \sum_{a=1}^3 Z_{ia}^{U,*} Z_{ja}^U \right) (g_{\mu\nu}) \quad (460)$$


---



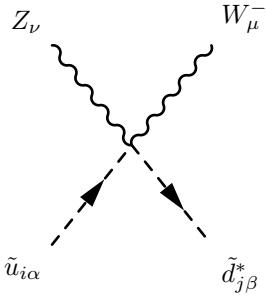
$$\frac{i}{3} \frac{1}{\sqrt{2}} g_1 g_2 \cos \Theta_W \delta_{\alpha\beta} \sum_{a=1}^3 Z_{ia}^{U,*} Z_{ja}^D (g_{\mu\nu}) \quad (461)$$


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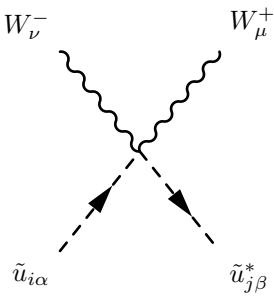
$$\begin{aligned}
& - \frac{i}{36} \delta_{\alpha\beta} \left( \left( -6g_1 g_2 \cos 2\Theta_W + \left( -9g_2^2 + g_1^2 \right) \sin 2\Theta_W \right) \sum_{a=1}^3 Z_{ia}^{U,*} Z_{ja}^U \right. \\
& \left. + 16g_1^2 \sin 2\Theta_W \sum_{a=1}^3 Z_{i3+a}^{U,*} Z_{j3+a}^U \right) (g_{\mu\nu}) \tag{462}
\end{aligned}$$


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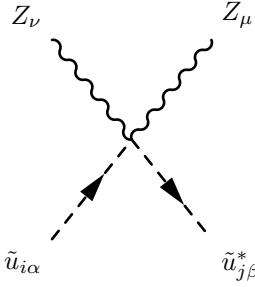
$$- \frac{i}{3} \frac{1}{\sqrt{2}} g_1 g_2 \delta_{\alpha\beta} \sin \Theta_W \sum_{a=1}^3 Z_{ia}^{U,*} Z_{ja}^D (g_{\mu\nu}) \tag{463}$$


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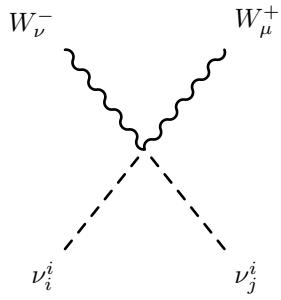
$$\frac{i}{2} g_2^2 \delta_{\alpha\beta} \sum_{a=1}^3 Z_{ia}^{U,*} Z_{ja}^U (g_{\mu\nu}) \tag{464}$$


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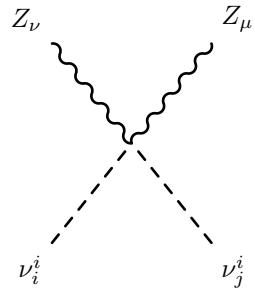
$$\frac{i}{18} \delta_{\alpha\beta} \left( 16g_1^2 \sin \Theta_W^2 \sum_{a=1}^3 Z_{i3+a}^{U,*} Z_{j3+a}^U + \left( -3g_2 \cos \Theta_W + g_1 \sin \Theta_W \right)^2 \sum_{a=1}^3 Z_{ia}^{U,*} Z_{ja}^U \right) (g_{\mu\nu}) \quad (465)$$


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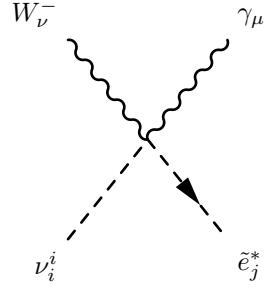
$$\frac{i}{2} g_2^2 \sum_{a=1}^3 Z_{ia}^{i,*} Z_{ja}^{i,*} (g_{\mu\nu}) \quad (466)$$


---



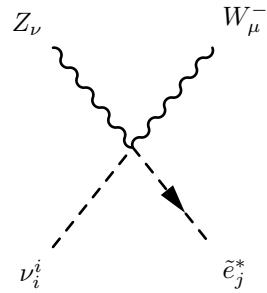
$$\frac{i}{2} \left( g_1 \sin \Theta_W + g_2 \cos \Theta_W \right)^2 \sum_{a=1}^3 Z_{ia}^{i,*} Z_{ja}^{i,*} (g_{\mu\nu}) \quad (467)$$


---



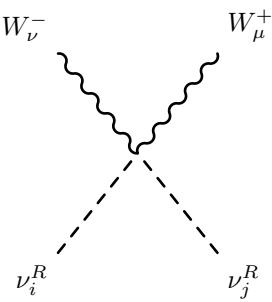
$$\frac{1}{2} g_1 g_2 \cos \Theta_W \sum_{a=1}^3 Z_{ia}^{i,*} Z_{ja}^E(g_{\mu\nu}) \quad (468)$$


---



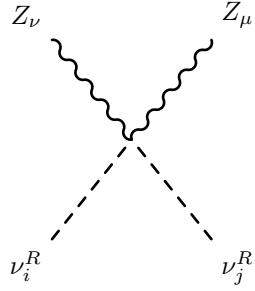
$$-\frac{1}{2} g_1 g_2 \sin \Theta_W \sum_{a=1}^3 Z_{ia}^{i,*} Z_{ja}^E(g_{\mu\nu}) \quad (469)$$


---



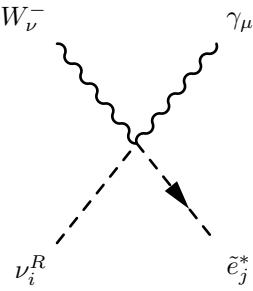
$$\frac{i}{2} g_2^2 \sum_{a=1}^3 Z_{ia}^{R,*} Z_{ja}^{R,*}(g_{\mu\nu}) \quad (470)$$


---



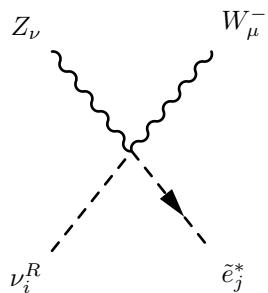
$$\frac{i}{2} \left( g_1 \sin \Theta_W + g_2 \cos \Theta_W \right)^2 \sum_{a=1}^3 Z_{ia}^{R,*} Z_{ja}^{R,*} \left( g_{\mu\nu} \right) \quad (471)$$


---



$$- \frac{i}{2} g_1 g_2 \cos \Theta_W \sum_{a=1}^3 Z_{ia}^{R,*} Z_{ja}^E \left( g_{\mu\nu} \right) \quad (472)$$

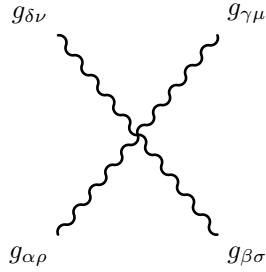

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$$\frac{i}{2} g_1 g_2 \sin \Theta_W \sum_{a=1}^3 Z_{ia}^{R,*} Z_{ja}^E \left( g_{\mu\nu} \right) \quad (473)$$


---

## 9.9 Four Vector Boson-Interaction

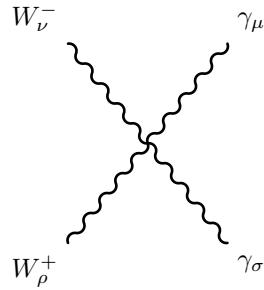


$$-ig_3^2 \left( \sum_{a=1}^8 f_{\alpha,\delta,a} f_{\beta,\gamma,a} + \sum_{a=1}^8 f_{\alpha,\gamma,a} f_{\beta,\delta,a} \right) (g_{\rho\sigma} g_{\mu\nu}) \quad (474)$$

$$+ ig_3^2 \left( - \sum_{a=1}^8 f_{\alpha,\beta,a} f_{\gamma,\delta,a} + \sum_{a=1}^8 f_{\alpha,\delta,a} f_{\beta,\gamma,a} \right) (g_{\rho\mu} g_{\sigma\nu}) \quad (475)$$

$$+ ig_3^2 \left( \sum_{a=1}^8 f_{\alpha,\gamma,a} f_{\beta,\delta,a} + \sum_{a=1}^8 f_{\alpha,\beta,a} f_{\gamma,\delta,a} \right) (g_{\rho\nu} g_{\sigma\mu}) \quad (476)$$


---

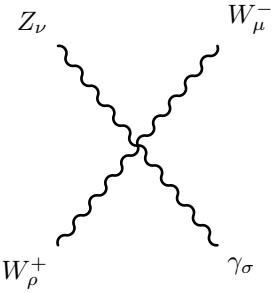


$$ig_2^2 \sin \Theta_W^2 (g_{\rho\sigma} g_{\mu\nu}) \quad (477)$$

$$+ ig_2^2 \sin \Theta_W^2 (g_{\rho\mu} g_{\sigma\nu}) \quad (478)$$

$$+ -2ig_2^2 \sin \Theta_W^2 (g_{\rho\nu} g_{\sigma\mu}) \quad (479)$$


---

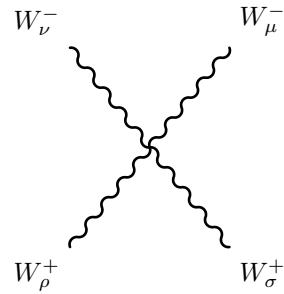


$$ig_2^2 \cos \Theta_W \sin \Theta_W (g_{\rho\sigma} g_{\mu\nu}) \quad (480)$$

$$+ -ig_2^2 \sin 2\Theta_W (g_{\rho\mu} g_{\sigma\nu}) \quad (481)$$

$$+ ig_2^2 \cos \Theta_W \sin \Theta_W (g_{\rho\nu} g_{\sigma\mu}) \quad (482)$$


---

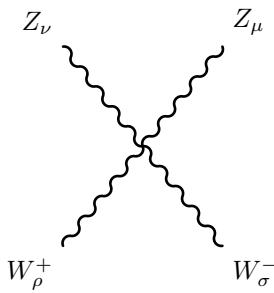


$$2ig_2^2 (g_{\rho\sigma} g_{\mu\nu}) \quad (483)$$

$$+ -ig_2^2 (g_{\rho\mu} g_{\sigma\nu}) \quad (484)$$

$$+ -ig_2^2 (g_{\rho\nu} g_{\sigma\mu}) \quad (485)$$


---



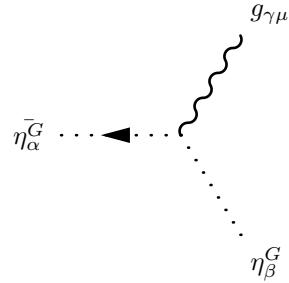
$$- 2ig_2^2 \cos \Theta_W^2 (g_{\rho\sigma} g_{\mu\nu}) \quad (486)$$

$$+ ig_2^2 \cos \Theta_W^2 (g_{\rho\mu} g_{\sigma\nu}) \quad (487)$$

$$+ ig_2^2 \cos \Theta_W^2 (g_{\rho\nu} g_{\sigma\mu}) \quad (488)$$

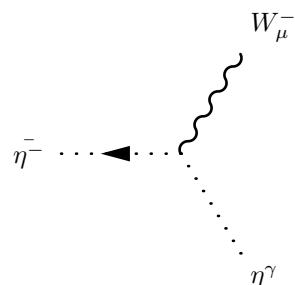

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## 9.10 Two Ghosts-One Vector Boson-Interaction



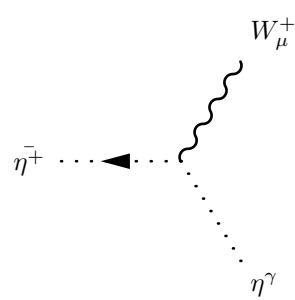
$$g_3 f_{\alpha,\beta,\gamma} (p_\mu^{\eta_\beta^G}) \quad (489)$$


---



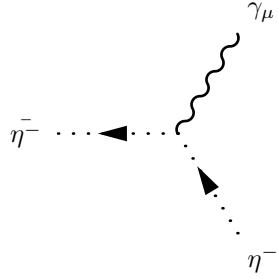
$$ig_2 \sin \Theta_W (p_\mu^{\eta^\gamma}) \quad (490)$$


---



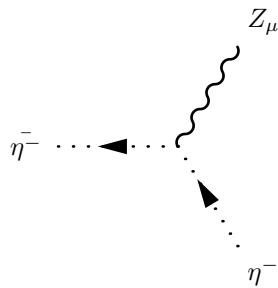
$$-ig_2 \sin \Theta_W \left( p_\mu^{\eta^\gamma} \right) \quad (491)$$


---



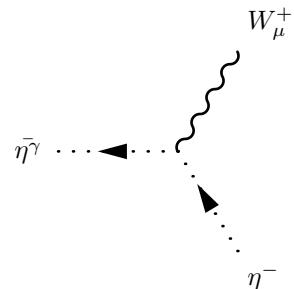
$$-ig_2 \sin \Theta_W \left( p_\mu^{\eta^-} \right) \quad (492)$$


---



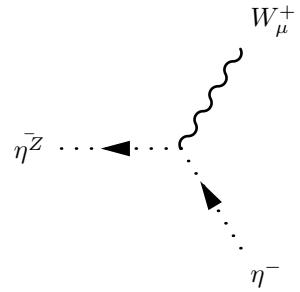
$$-ig_2 \cos \Theta_W \left( p_\mu^{\eta^-} \right) \quad (493)$$


---



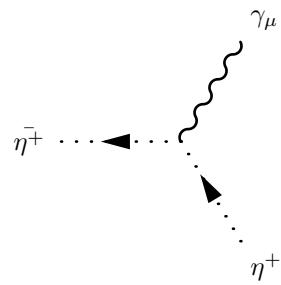
$$ig_2 \sin \Theta_W \left( p_\mu^{\eta^-} \right) \quad (494)$$


---



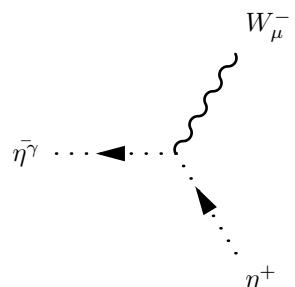
$$ig_2 \cos \Theta_W \left( p_\mu^{\eta^-} \right) \quad (495)$$


---



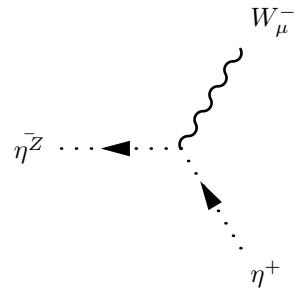
$$ig_2 \sin \Theta_W \left( p_\mu^{\eta^+} \right) \quad (496)$$


---



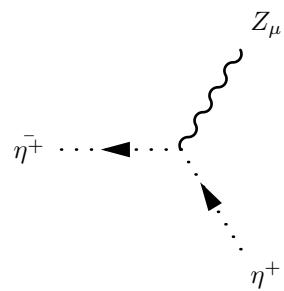
$$- ig_2 \sin \Theta_W \left( p_\mu^{\eta^+} \right) \quad (497)$$


---



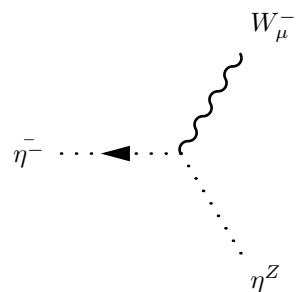
$$-ig_2 \cos \Theta_W \left( p_\mu^{\eta^+} \right) \quad (498)$$


---



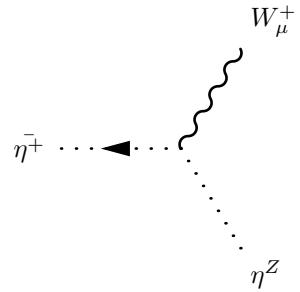
$$ig_2 \cos \Theta_W \left( p_\mu^{\eta^+} \right) \quad (499)$$


---



$$ig_2 \cos \Theta_W \left( p_\mu^{\eta^Z} \right) \quad (500)$$

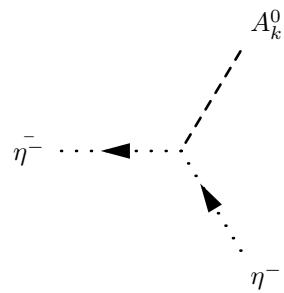

---



$$-ig_2 \cos \Theta_W \left( p_\mu^{\eta^Z} \right) \quad (501)$$

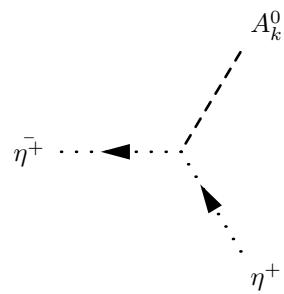

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### 9.11 Two Ghosts-One Scalar-Interaction



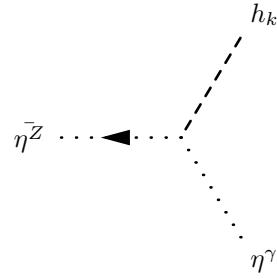
$$\frac{1}{4} g_2^2 \xi_{W^-} \left( v_d Z_{k1}^A - v_u Z_{k2}^A \right) \quad (502)$$


---



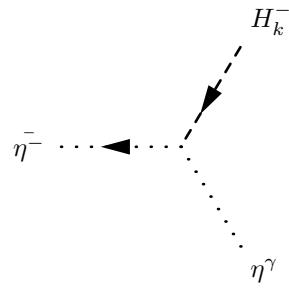
$$\frac{1}{4} g_2^2 \xi_{W^-} \left( -v_d Z_{k1}^A + v_u Z_{k2}^A \right) \quad (503)$$


---



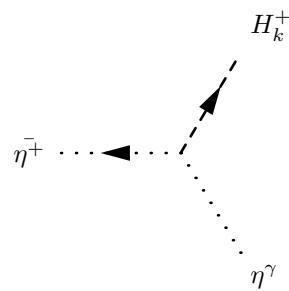
$$\frac{i}{8}\xi_Z \left( 2g_1g_2 \cos 2\Theta_W + \left( -g_2^2 + g_1^2 \right) \sin 2\Theta_W \right) \left( v_d Z_{k1}^H + v_u Z_{k2}^H \right) \quad (504)$$


---



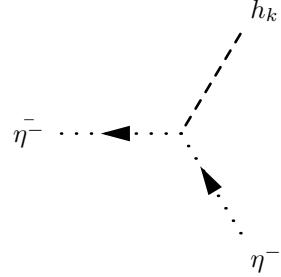
$$\frac{i}{4}g_2\xi_{W^-} \left( g_1 \cos \Theta_W + g_2 \sin \Theta_W \right) \left( v_d Z_{k1}^+ - v_u Z_{k2}^+ \right) \quad (505)$$


---



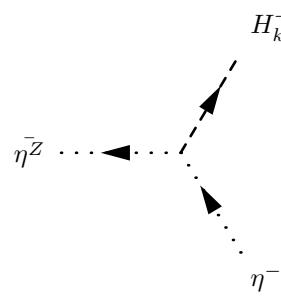
$$\frac{i}{4}g_2\xi_{W^-} \left( g_1 \cos \Theta_W + g_2 \sin \Theta_W \right) \left( v_d Z_{k1}^+ - v_u Z_{k2}^+ \right) \quad (506)$$


---



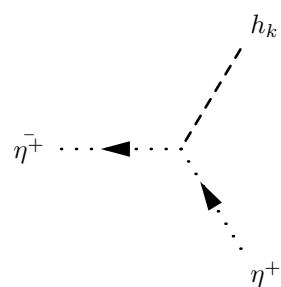
$$-\frac{i}{4}g_2^2\xi_{W^-}\left(v_dZ_{k1}^H+v_uZ_{k2}^H\right) \quad (507)$$


---



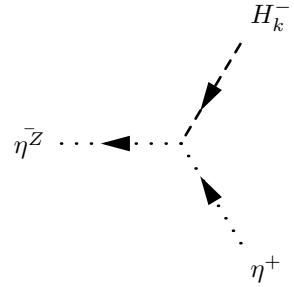
$$-\frac{i}{4}g_2\xi_Z\left(g_1\sin\Theta_W+g_2\cos\Theta_W\right)\left(v_dZ_{k1}^+-v_uZ_{k2}^+\right) \quad (508)$$


---



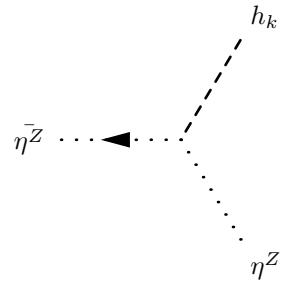
$$-\frac{i}{4}g_2^2\xi_{W^-}\left(v_dZ_{k1}^H+v_uZ_{k2}^H\right) \quad (509)$$


---



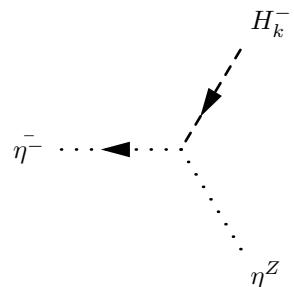
$$-\frac{i}{4}g_2\xi_Z\left(g_1 \sin \Theta_W + g_2 \cos \Theta_W\right)\left(v_d Z_{k1}^+ - v_u Z_{k2}^+\right) \quad (510)$$


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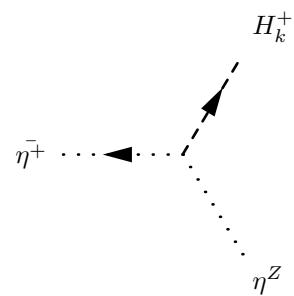
$$-\frac{i}{4}\xi_Z\left(g_1 \sin \Theta_W + g_2 \cos \Theta_W\right)^2\left(v_d Z_{k1}^H + v_u Z_{k2}^H\right) \quad (511)$$


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$$\frac{i}{4}g_2\xi_{W^-}\left(-g_1 \sin \Theta_W + g_2 \cos \Theta_W\right)\left(v_d Z_{k1}^+ - v_u Z_{k2}^+\right) \quad (512)$$


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$$\frac{i}{4} g_2 \xi_{W^-} \left( -g_1 \sin \Theta_W + g_2 \cos \Theta_W \right) \left( v_d Z_{k1}^+ - v_u Z_{k2}^+ \right) \quad (513)$$

## 10 Clebsch-Gordan Coefficients