

Singlet scalar Dark Matter  
Lagrangian, Rotations and Interactions for eigenstates 'EWSB'  
including Renormalization Group Equations  
including one-loop Self-Energies

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# 1 Fields

## 1.1 Gauge Fields

Name	$SU(N)$	Coupling	Name
$B$	$U(1)$	$g_1$	hypercharge
$W$	$SU(2)$	$g_2$	left
$g$	$SU(3)$	$g_3$	color

## 1.2 Matter Superfields

Name	Spin	Generations	$(U(1) \otimes SU(2) \otimes SU(3))$
$H$	0	1	$(\frac{1}{2}, \mathbf{2}, \mathbf{1})$
$S$	0	1	$(0, \mathbf{1}, \mathbf{1})$
$q$	$\frac{1}{2}$	3	$(\frac{1}{6}, \mathbf{2}, \mathbf{3})$
$l$	$\frac{1}{2}$	3	$(-\frac{1}{2}, \mathbf{2}, \mathbf{1})$
$d$	$\frac{1}{2}$	3	$(\frac{1}{3}, \mathbf{1}, \bar{\mathbf{3}})$
$u$	$\frac{1}{2}$	3	$(-\frac{2}{3}, \mathbf{1}, \bar{\mathbf{3}})$
$e$	$\frac{1}{2}$	3	$(1, \mathbf{1}, \mathbf{1})$

# 2 Lagrangian

## 2.1 Input Lagrangian for Eigenstates GaugeES

$$L = 0 \tag{1}$$

## 2.2 Gauge fixing terms

### 2.2.1 Gauge fixing terms for eigenstates 'GaugeES'

$$L_{GF} = -\frac{1}{2}|\partial_\mu B|^2 \xi_B^{-1} - \frac{1}{2}|\partial_\mu g|^2 \xi_g^{-1} - \frac{1}{2}|\partial_\mu W|^2 \xi_W^{-1} \tag{2}$$

### 2.2.2 Gauge fixing terms for eigenstates 'EWSB'

$$\begin{aligned}
L_{GF} = & -\frac{1}{2}|\partial_\mu g|^2 \xi_g^{-1} - \frac{1}{2}|\partial_\mu \gamma|^2 \xi_\gamma^{-1} - \left| -\frac{i}{2}g_2 H^+ v \xi_{W^+} + \partial_\mu W^+ \right|^2 \xi_{W^+}^{-1} \\
& - \frac{1}{2} \left| -\frac{1}{2}A^0 v \xi_Z \left( g_1 \sin \Theta_W + g_2 \cos \Theta_W \right) + \partial_\mu Z \right|^2 \xi_Z^{-1}
\end{aligned} \tag{3}$$

## 2.3 Fields integrated out

None

## 3 Renormalization Group Equations

### 3.1 Gauge Couplings

$$\beta_{g_1}^{(1)} = \frac{41}{10}g_1^3 \quad (4)$$

$$\beta_{g_1}^{(2)} = \frac{1}{50}g_1^3 \left( 135g_2^2 + 199g_1^2 - 25\text{Tr}(Y_d Y_d^\dagger) + 440g_3^2 - 75\text{Tr}(Y_e Y_e^\dagger) - 85\text{Tr}(Y_u Y_u^\dagger) \right) \quad (5)$$

$$\beta_{g_2}^{(1)} = -\frac{19}{6}g_2^3 \quad (6)$$

$$\beta_{g_2}^{(2)} = \frac{1}{30}g_2^3 \left( -15\text{Tr}(Y_e Y_e^\dagger) + 175g_2^2 + 27g_1^2 + 360g_3^2 - 45\text{Tr}(Y_d Y_d^\dagger) - 45\text{Tr}(Y_u Y_u^\dagger) \right) \quad (7)$$

$$\beta_{g_3}^{(1)} = -7g_3^3 \quad (8)$$

$$\beta_{g_3}^{(2)} = -\frac{1}{10}g_3^3 \left( -11g_1^2 + 20\text{Tr}(Y_d Y_d^\dagger) + 20\text{Tr}(Y_u Y_u^\dagger) + 260g_3^2 - 45g_2^2 \right) \quad (9)$$

### 3.2 Quartic scalar couplings

$$\beta_{LamS}^{(1)} = 4 \left( 9LamS^2 + LamSH^2 \right) \quad (10)$$

$$\beta_{LamS}^{(2)} = -\frac{8}{5} \left( -15g_2^2 LamSH^2 + 15LamSH^2 \text{Tr}(Y_d Y_d^\dagger) + 15LamSH^2 \text{Tr}(Y_u Y_u^\dagger) + 20LamSH^3 - 3g_1^2 LamSH^2 + 50LamSLamS \right) \quad (11)$$

$$\beta_{LamSH}^{(1)} = \frac{1}{10}LamSH \left( 120LamS + 20\text{Tr}(Y_e Y_e^\dagger) - 45g_2^2 + 60\lambda + 60\text{Tr}(Y_d Y_d^\dagger) + 60\text{Tr}(Y_u Y_u^\dagger) + 80LamSH - 9g_1^2 \right) \quad (12)$$

$$\begin{aligned} \beta_{LamSH}^{(2)} = & +\frac{1671}{400}g_1^4 LamSH + \frac{9}{8}g_1^2 g_2^2 LamSH - \frac{145}{16}g_2^4 LamSH + \frac{36}{5}g_1^2 \lambda LamSH + 36g_2^2 \lambda LamSH - 15\lambda^2 LamSH - 120LamS^2 LamSH \\ & - 144LamSLamSH^2 - 42LamSH^3 + \frac{1}{4} \left( -144\lambda + 160g_3^2 + 45g_2^2 + 5g_1^2 - 96LamSH \right) LamSH \text{Tr}(Y_d Y_d^\dagger) \\ & + \frac{1}{4} \left( 15g_1^2 + 15g_2^2 - 32LamSH - 48\lambda \right) LamSH \text{Tr}(Y_e Y_e^\dagger) + \frac{17}{4}g_1^2 LamSH \text{Tr}(Y_u Y_u^\dagger) + \frac{45}{4}g_2^2 LamSH \text{Tr}(Y_u Y_u^\dagger) \\ & + 40g_3^2 LamSH \text{Tr}(Y_u Y_u^\dagger) - 36\lambda LamSH \text{Tr}(Y_u Y_u^\dagger) - 24LamSH^2 \text{Tr}(Y_u Y_u^\dagger) - \frac{27}{2}LamSH \text{Tr}(Y_d Y_d^\dagger Y_d Y_d^\dagger) \\ & - 21LamSH \text{Tr}(Y_d Y_d^\dagger Y_u Y_u^\dagger) - \frac{9}{2}LamSH \text{Tr}(Y_e Y_e^\dagger Y_e Y_e^\dagger) - \frac{27}{2}LamSH \text{Tr}(Y_u Y_u^\dagger Y_u Y_u^\dagger) \end{aligned} \quad (13)$$

$$\begin{aligned} \beta_\lambda^{(1)} = & +\frac{27}{100}g_1^4 + \frac{9}{10}g_1^2 g_2^2 + \frac{9}{4}g_2^4 - \frac{9}{5}g_1^2 \lambda - 9g_2^2 \lambda + 12\lambda^2 + 4LamSH^2 + 12\lambda \text{Tr}(Y_d Y_d^\dagger) + 4\lambda \text{Tr}(Y_e Y_e^\dagger) \\ & + 12\lambda \text{Tr}(Y_u Y_u^\dagger) - 12\text{Tr}(Y_d Y_d^\dagger Y_d Y_d^\dagger) - 4\text{Tr}(Y_e Y_e^\dagger Y_e Y_e^\dagger) - 12\text{Tr}(Y_u Y_u^\dagger Y_u Y_u^\dagger) \end{aligned} \quad (14)$$

$$\begin{aligned}
\beta_\lambda^{(2)} = & -\frac{3411}{1000}g_1^6 - \frac{1677}{200}g_1^4g_2^2 - \frac{289}{40}g_1^2g_2^4 + \frac{305}{8}g_2^6 + \frac{1887}{200}g_1^4\lambda + \frac{117}{20}g_1^2g_2^2\lambda - \frac{73}{8}g_2^4\lambda + \frac{54}{5}g_1^2\lambda^2 + 54g_2^2\lambda^2 \\
& - 78\lambda^3 - 20\lambda LamSH^2 - 32LamSH^3 + \frac{1}{10}\left(225g_2^2\lambda - 45g_2^4 + 80(10g_3^2 - 9\lambda)\lambda + 9g_1^4 + g_1^2(25\lambda + 54g_2^2)\right)\text{Tr}(Y_dY_d^\dagger) \\
& - \frac{3}{10}\left(15g_1^4 + 5(16\lambda^2 - 5g_2^2\lambda + g_2^4) - g_1^2(22g_2^2 + 25\lambda)\right)\text{Tr}(Y_eY_e^\dagger) - \frac{171}{50}g_1^4\text{Tr}(Y_uY_u^\dagger) \\
& + \frac{63}{5}g_1^2g_2^2\text{Tr}(Y_uY_u^\dagger) - \frac{9}{2}g_2^4\text{Tr}(Y_uY_u^\dagger) + \frac{17}{2}g_1^2\lambda\text{Tr}(Y_uY_u^\dagger) + \frac{45}{2}g_2^2\lambda\text{Tr}(Y_uY_u^\dagger) \\
& + 80g_3^2\lambda\text{Tr}(Y_uY_u^\dagger) - 72\lambda^2\text{Tr}(Y_uY_u^\dagger) + \frac{8}{5}g_1^2\text{Tr}(Y_dY_d^\dagger Y_dY_d^\dagger) - 64g_3^2\text{Tr}(Y_dY_d^\dagger Y_dY_d^\dagger) \\
& - 3\lambda\text{Tr}(Y_dY_d^\dagger Y_dY_d^\dagger) - 42\lambda\text{Tr}(Y_dY_u^\dagger Y_uY_d^\dagger) - \frac{24}{5}g_1^2\text{Tr}(Y_eY_e^\dagger Y_eY_e^\dagger) - \lambda\text{Tr}(Y_eY_e^\dagger Y_eY_e^\dagger) \\
& - \frac{16}{5}g_1^2\text{Tr}(Y_uY_u^\dagger Y_uY_u^\dagger) - 64g_3^2\text{Tr}(Y_uY_u^\dagger Y_uY_u^\dagger) - 3\lambda\text{Tr}(Y_uY_u^\dagger Y_uY_u^\dagger) + 60\text{Tr}(Y_dY_d^\dagger Y_dY_d^\dagger Y_dY_d^\dagger) \\
& + 12\text{Tr}(Y_dY_d^\dagger Y_dY_u^\dagger Y_uY_d^\dagger) - 24\text{Tr}(Y_dY_u^\dagger Y_uY_d^\dagger Y_dY_d^\dagger) - 12\text{Tr}(Y_dY_u^\dagger Y_uY_u^\dagger Y_uY_d^\dagger) \\
& + 20\text{Tr}(Y_eY_e^\dagger Y_eY_e^\dagger Y_eY_e^\dagger) + 60\text{Tr}(Y_uY_u^\dagger Y_uY_u^\dagger Y_uY_u^\dagger)
\end{aligned} \tag{15}$$

### 3.3 Yukawa Couplings

$$\begin{aligned}
\beta_{Y_u}^{(1)} = & -\frac{3}{2}\left(-Y_uY_u^\dagger Y_u + Y_uY_d^\dagger Y_d\right) \\
& + Y_u\left(3\text{Tr}(Y_dY_d^\dagger) + 3\text{Tr}(Y_uY_u^\dagger) - 8g_3^2 - \frac{17}{20}g_1^2 - \frac{9}{4}g_2^2 + \text{Tr}(Y_eY_e^\dagger)\right)
\end{aligned} \tag{16}$$

$$\begin{aligned}
\beta_{Y_u}^{(2)} = & +\frac{1}{80}\left(20\left(11Y_uY_d^\dagger Y_dY_d^\dagger Y_d - 4Y_uY_u^\dagger Y_uY_d^\dagger Y_d + 6Y_uY_u^\dagger Y_uY_u^\dagger Y_u - Y_uY_d^\dagger Y_dY_u^\dagger Y_u\right)\right. \\
& + Y_uY_u^\dagger Y_u\left(1280g_3^2 - 180\text{Tr}(Y_eY_e^\dagger) + 223g_1^2 - 480\lambda - 540\text{Tr}(Y_dY_d^\dagger) - 540\text{Tr}(Y_uY_u^\dagger) + 675g_2^2\right) \\
& + Y_uY_d^\dagger Y_d\left(100\text{Tr}(Y_eY_e^\dagger) - 1280g_3^2 + 300\text{Tr}(Y_dY_d^\dagger) + 300\text{Tr}(Y_uY_u^\dagger) - 43g_1^2 + 45g_2^2\right) \\
& + Y_u\left(\frac{1187}{600}g_1^4 - \frac{9}{20}g_1^2g_2^2 - \frac{23}{4}g_2^4 + \frac{19}{15}g_1^2g_3^2 + 9g_2^2g_3^2 - 108g_3^4 + \frac{3}{2}\lambda^2 + LamSH^2\right. \\
& + \frac{5}{8}\left(32g_3^2 + 9g_2^2 + g_1^2\right)\text{Tr}(Y_dY_d^\dagger) + \frac{15}{8}\left(g_1^2 + g_2^2\right)\text{Tr}(Y_eY_e^\dagger) + \frac{17}{8}g_1^2\text{Tr}(Y_uY_u^\dagger) + \frac{45}{8}g_2^2\text{Tr}(Y_uY_u^\dagger) \\
& \left. + 20g_3^2\text{Tr}(Y_uY_u^\dagger) - \frac{27}{4}\text{Tr}(Y_dY_d^\dagger Y_dY_d^\dagger) + \frac{3}{2}\text{Tr}(Y_dY_u^\dagger Y_uY_d^\dagger) - \frac{9}{4}\text{Tr}(Y_eY_e^\dagger Y_eY_e^\dagger) - \frac{27}{4}\text{Tr}(Y_uY_u^\dagger Y_uY_u^\dagger)\right)
\end{aligned} \tag{17}$$

$$\begin{aligned}
\beta_{Y_d}^{(1)} = & \frac{1}{4}\left(6\left(-Y_dY_u^\dagger Y_u + Y_dY_d^\dagger Y_d\right)\right. \\
& \left.- Y_d\left(-12\text{Tr}(Y_dY_d^\dagger) - 12\text{Tr}(Y_uY_u^\dagger) + 32g_3^2 - 4\text{Tr}(Y_eY_e^\dagger) + 9g_2^2 + g_1^2\right)\right)
\end{aligned} \tag{18}$$

$$\begin{aligned}
\beta_{Y_d}^{(2)} = & +\frac{1}{80}\left(20\left(11Y_dY_u^\dagger Y_uY_u^\dagger Y_u - 4Y_dY_d^\dagger Y_dY_u^\dagger Y_u + 6Y_dY_d^\dagger Y_dY_d^\dagger Y_d - Y_dY_u^\dagger Y_uY_d^\dagger Y_d\right)\right. \\
& + Y_dY_d^\dagger Y_d\left(1280g_3^2 - 180\text{Tr}(Y_eY_e^\dagger) + 187g_1^2 - 480\lambda - 540\text{Tr}(Y_dY_d^\dagger) - 540\text{Tr}(Y_uY_u^\dagger) + 675g_2^2\right)
\end{aligned}$$

$$\begin{aligned}
& + Y_d Y_u^\dagger Y_u \left( 100 \text{Tr} \left( Y_e Y_e^\dagger \right) - 1280 g_3^2 + 300 \text{Tr} \left( Y_d Y_d^\dagger \right) + 300 \text{Tr} \left( Y_u Y_u^\dagger \right) + 45 g_2^2 - 79 g_1^2 \right) \\
& + Y_d \left( -\frac{127}{600} g_1^4 - \frac{27}{20} g_1^2 g_2^2 - \frac{23}{4} g_2^4 + \frac{31}{15} g_1^2 g_3^2 + 9 g_2^2 g_3^2 - 108 g_3^4 + \frac{3}{2} \lambda^2 + Lam SH^2 \right. \\
& + \frac{5}{8} (32 g_3^2 + 9 g_2^2 + g_1^2) \text{Tr} \left( Y_d Y_d^\dagger \right) + \frac{15}{8} (g_1^2 + g_2^2) \text{Tr} \left( Y_e Y_e^\dagger \right) + \frac{17}{8} g_1^2 \text{Tr} \left( Y_u Y_u^\dagger \right) + \frac{45}{8} g_2^2 \text{Tr} \left( Y_u Y_u^\dagger \right) \\
& \left. + 20 g_3^2 \text{Tr} \left( Y_u Y_u^\dagger \right) - \frac{27}{4} \text{Tr} \left( Y_d Y_d^\dagger Y_d Y_d^\dagger \right) + \frac{3}{2} \text{Tr} \left( Y_d Y_u^\dagger Y_u Y_d^\dagger \right) - \frac{9}{4} \text{Tr} \left( Y_e Y_e^\dagger Y_e Y_e^\dagger \right) - \frac{27}{4} \text{Tr} \left( Y_u Y_u^\dagger Y_u Y_u^\dagger \right) \right) \quad (19)
\end{aligned}$$

$$\beta_{Y_e}^{(1)} = \frac{3}{2} Y_e Y_e^\dagger Y_e + Y_e \left( 3 \text{Tr} \left( Y_d Y_d^\dagger \right) + 3 \text{Tr} \left( Y_u Y_u^\dagger \right) - \frac{9}{4} g_1^2 - \frac{9}{4} g_2^2 + \text{Tr} \left( Y_e Y_e^\dagger \right) \right) \quad (20)$$

$$\begin{aligned}
\beta_{Y_e}^{(2)} = & + \frac{3}{80} \left( 40 Y_e Y_e^\dagger Y_e Y_e^\dagger Y_e \right. \\
& + Y_e Y_e^\dagger Y_e \left( 129 g_1^2 - 160 \lambda - 180 \text{Tr} \left( Y_d Y_d^\dagger \right) - 180 \text{Tr} \left( Y_u Y_u^\dagger \right) + 225 g_2^2 - 60 \text{Tr} \left( Y_e Y_e^\dagger \right) \right) \\
& + \frac{1}{200} Y_e \left( 1371 g_1^4 + 270 g_1^2 g_2^2 - 1150 g_2^4 + 300 \lambda^2 + 200 Lam SH^2 + 125 (32 g_3^2 + 9 g_2^2 + g_1^2) \text{Tr} \left( Y_d Y_d^\dagger \right) \right. \\
& + 375 (g_1^2 + g_2^2) \text{Tr} \left( Y_e Y_e^\dagger \right) + 425 g_1^2 \text{Tr} \left( Y_u Y_u^\dagger \right) + 1125 g_2^2 \text{Tr} \left( Y_u Y_u^\dagger \right) + 4000 g_3^2 \text{Tr} \left( Y_u Y_u^\dagger \right) \\
& \left. - 1350 \text{Tr} \left( Y_d Y_d^\dagger Y_d Y_d^\dagger \right) + 300 \text{Tr} \left( Y_d Y_u^\dagger Y_u Y_d^\dagger \right) - 450 \text{Tr} \left( Y_e Y_e^\dagger Y_e Y_e^\dagger \right) - 1350 \text{Tr} \left( Y_u Y_u^\dagger Y_u Y_u^\dagger \right) \right) \quad (21)
\end{aligned}$$

### 3.4 Scalar Mass Terms

$$\beta_{M_S^2}^{(1)} = 12 Lam SM_S^2 + 8 Lam SH \mu^2 \quad (22)$$

$$\begin{aligned}
\beta_{M_S^2}^{(2)} = & -\frac{8}{5} \left( 75 Lam S^2 M_S^2 + 5 Lam SH^2 M_S^2 - 6 g_1^2 Lam SH \mu^2 - 30 g_2^2 Lam SH \mu^2 + 20 Lam SH^2 \mu^2 + 30 Lam SH \mu^2 \text{Tr} \left( Y_d Y_d^\dagger \right) + 10 Lam SH \mu^2 \text{Tr} \left( Y_e Y_e^\dagger \right) \right. \\
& \left. + 30 Lam SH \mu^2 \text{Tr} \left( Y_u Y_u^\dagger \right) \right) \quad (23)
\end{aligned}$$

$$\beta_{\mu^2}^{(1)} = 2 Lam SH M_S^2 + 2 \mu^2 \text{Tr} \left( Y_e Y_e^\dagger \right) + 6 \lambda \mu^2 + 6 \mu^2 \text{Tr} \left( Y_d Y_d^\dagger \right) + 6 \mu^2 \text{Tr} \left( Y_u Y_u^\dagger \right) - \frac{9}{10} g_1^2 \mu^2 - \frac{9}{2} g_2^2 \mu^2 \quad (24)$$

$$\begin{aligned}
\beta_{\mu^2}^{(2)} = & -8 Lam SH^2 M_S^2 + \frac{1671}{400} g_1^4 \mu^2 + \frac{9}{8} g_1^2 g_2^2 \mu^2 - \frac{145}{16} g_2^4 \mu^2 + \frac{36}{5} g_1^2 \lambda \mu^2 + 36 g_2^2 \lambda \mu^2 - 15 \lambda^2 \mu^2 - 2 Lam SH^2 \mu^2 \\
& + \frac{1}{4} \left( -144 \lambda + 160 g_3^2 + 45 g_2^2 + 5 g_1^2 \right) \mu^2 \text{Tr} \left( Y_d Y_d^\dagger \right) + \frac{3}{4} \left( -16 \lambda + 5 g_1^2 + 5 g_2^2 \right) \mu^2 \text{Tr} \left( Y_e Y_e^\dagger \right) \\
& + \frac{17}{4} g_1^2 \mu^2 \text{Tr} \left( Y_u Y_u^\dagger \right) + \frac{45}{4} g_2^2 \mu^2 \text{Tr} \left( Y_u Y_u^\dagger \right) + 40 g_3^2 \mu^2 \text{Tr} \left( Y_u Y_u^\dagger \right) - 36 \lambda \mu^2 \text{Tr} \left( Y_u Y_u^\dagger \right) \\
& - \frac{27}{2} \mu^2 \text{Tr} \left( Y_d Y_d^\dagger Y_d Y_d^\dagger \right) - 21 \mu^2 \text{Tr} \left( Y_d Y_u^\dagger Y_u Y_d^\dagger \right) - \frac{9}{2} \mu^2 \text{Tr} \left( Y_e Y_e^\dagger Y_e Y_e^\dagger \right) - \frac{27}{2} \mu^2 \text{Tr} \left( Y_u Y_u^\dagger Y_u Y_u^\dagger \right) \quad (25)
\end{aligned}$$

### 3.5 Vacuum expectation values

$$\beta_v^{(1)} = \frac{1}{20} v \left( 15 g_2^2 X_i - 20 \text{Tr} \left( Y_e Y_e^\dagger \right) + 3 g_1^2 X_i + 45 g_2^2 - 60 \text{Tr} \left( Y_d Y_d^\dagger \right) - 60 \text{Tr} \left( Y_u Y_u^\dagger \right) + 9 g_1^2 \right) \quad (26)$$

$$\begin{aligned}
\beta_v^{(2)} = & \frac{1}{800}v \left( -1293g_1^4 - 270g_1^2g_2^2 + 6775g_2^4 - 1200\lambda^2 - 800LamSH^2 + 18g_1^4Xi + 180g_1^2g_2^2Xi + 2250g_2^4Xi + 18g_1^4Xi^2 \right. \\
& + 180g_1^2g_2^2Xi^2 - 450g_2^4Xi^2 - 20 \left( 45g_2^2(2Xi + 5) + 800g_3^2 + g_1^2(18Xi + 25) \right) \text{Tr}(Y_dY_d^\dagger) \\
& - 60 \left( 5g_2^2(2Xi + 5) + g_1^2(2Xi + 25) \right) \text{Tr}(Y_eY_e^\dagger) - 1700g_1^2\text{Tr}(Y_uY_u^\dagger) - 4500g_2^2\text{Tr}(Y_uY_u^\dagger) \\
& - 16000g_3^2\text{Tr}(Y_uY_u^\dagger) - 360g_1^2Xi\text{Tr}(Y_uY_u^\dagger) - 1800g_2^2Xi\text{Tr}(Y_uY_u^\dagger) + 5400\text{Tr}(Y_dY_d^\dagger Y_dY_d^\dagger) \\
& \left. - 1200\text{Tr}(Y_dY_u^\dagger Y_uY_d^\dagger) + 1800\text{Tr}(Y_eY_e^\dagger Y_eY_e^\dagger) + 5400\text{Tr}(Y_uY_u^\dagger Y_uY_u^\dagger) \right) \quad (27)
\end{aligned}$$

## 4 Field Rotations

### 4.1 Rotations in gauge sector for eigenstates 'EWSB'

$$\begin{pmatrix} B_\rho \\ W_{3\rho} \end{pmatrix} = Z^{\gamma Z} \begin{pmatrix} \gamma_\rho \\ Z_\rho \end{pmatrix} \quad (28)$$

$$\begin{pmatrix} W_{1\rho} \\ W_{2\rho} \end{pmatrix} = Z^W \begin{pmatrix} W_\rho^+ \\ W_\rho^+ \end{pmatrix} \quad (29)$$

$$(30)$$

The mixing matrices are parametrized by

$$Z^{\gamma Z} = \begin{pmatrix} \cos \Theta_W & -\sin \Theta_W \\ \sin \Theta_W & \cos \Theta_W \end{pmatrix} \quad (31)$$

$$Z^W = \begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ i\frac{1}{\sqrt{2}} & -i\frac{1}{\sqrt{2}} \end{pmatrix} \quad (32)$$

$$(33)$$

### 4.2 Rotations in Mass sector for eigenstates 'EWSB'

#### 4.2.1 Mass Matrices for Scalars

- No Scalar Mixings

#### 4.2.2 Mass Matrices for Fermions

- Mass matrix for Down-Quarks, Basis:  $(d_{L,\alpha_1}), (d_{R,\beta_1}^*)$

$$m_d = \left( \frac{1}{\sqrt{2}}v\delta_{\alpha_1\beta_1}Y_d^T \right) \quad (34)$$



This matrix is diagonalized by  $U_L^d$  and  $U_R^d$

$$U_L^{d,*} m_d U_R^{d,\dagger} = m_d^{dia} \quad (35)$$

with

$$d_{L,i\alpha} = \sum_{t_2} U_{L,ji}^{d,*} D_{L,j\alpha} \quad (36)$$

$$d_{R,i\alpha} = \sum_{t_2} U_{R,ij}^d D_{R,j\alpha}^* \quad (37)$$

- **Mass matrix for Up-Quarks**, Basis:  $(u_{L,\alpha_1}), (u_{R,\beta_1}^*)$

$$m_u = \left( -\frac{1}{\sqrt{2}} v \delta_{\alpha_1 \beta_1} Y_u^T \right) \quad (38)$$

This matrix is diagonalized by  $U_L^u$  and  $U_R^u$

$$U_L^{u,*} m_u U_R^{u,\dagger} = m_u^{dia} \quad (39)$$

with

$$u_{L,i\alpha} = \sum_{t_2} U_{L,ji}^{u,*} U_{L,j\alpha} \quad (40)$$

$$u_{R,i\alpha} = \sum_{t_2} U_{R,ij}^u U_{R,j\alpha}^* \quad (41)$$

- **Mass matrix for Leptons**, Basis:  $(e_L), (e_R^*)$

$$m_e = \left( \frac{1}{\sqrt{2}} v Y_e^T \right) \quad (42)$$

This matrix is diagonalized by  $U_L^e$  and  $U_R^e$

$$U_L^{e,*} m_e U_R^{e,\dagger} = m_e^{dia} \quad (43)$$

with

$$e_{L,i} = \sum_{t_2} U_{L,ji}^{e,*} E_{L,j} \quad (44)$$

$$e_{R,i} = \sum_{t_2} U_{R,ij}^e E_{R,j}^* \quad (45)$$

## 5 Vacuum Expectation Values

$$H^0 = \frac{1}{\sqrt{2}} h + \frac{1}{\sqrt{2}} v + i \frac{1}{\sqrt{2}} A^0 \quad (46)$$

## 6 Tadpole Equations

$$\frac{\partial V}{\partial h} = \frac{1}{2}\lambda v^3 + \mu^2 v \quad (47)$$

## 7 Particle content for eigenstates 'EWSB'

Name	Type	complex/real	Generations	Indices
$H^+$	Scalar	complex	1	
$S$	Scalar	real	1	
$A^0$	Scalar	real	1	
$h$	Scalar	real	1	
$\nu$	Fermion	Dirac	3	generation, 3
$d$	Fermion	Dirac	3	generation, 3, color, 3
$u$	Fermion	Dirac	3	generation, 3, color, 3
$e$	Fermion	Dirac	3	generation, 3
$g$	Vector	real	1	color, 8, lorentz, 4
$\gamma$	Vector	real	1	lorentz, 4
$Z$	Vector	real	1	lorentz, 4
$W^+$	Vector	complex	1	lorentz, 4
$\eta^G$	Ghost	real	1	color, 8
$\eta^\gamma$	Ghost	real	1	
$\eta^Z$	Ghost	real	1	
$\eta^+$	Ghost	complex	1	
$\eta^-$	Ghost	complex	1	

## 8 One Loop Self-Energy and One Loop Tadpoles for eigenstates 'EWSB'

### 8.1 One Loop Self-Energy

- Self-Energy for Down-Quarks ( $d$ )

$$\Sigma_{i,j}^S(p^2) = + \sum_{a=1}^3 B_0(p^2, m_{d_a}^2, m_{A^0}^2) \Gamma_{\tilde{d}_j, d_a, A^0}^{L*} m_{d_a} \Gamma_{\tilde{d}_i, d_a, A^0}^R + \sum_{b=1}^3 B_0(p^2, m_{d_b}^2, m_h^2) \Gamma_{\tilde{d}_j, h, d_b}^{L*} m_{d_b} \Gamma_{\tilde{d}_i, h, d_b}^R$$

$$\begin{aligned}
& -\frac{16}{3} \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{d_b}^2, 0) \right) \Gamma_{\check{d}_j, g, d_b}^{R*} m_{d_b} \Gamma_{\check{d}_i, g, d_b}^L - 4 \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{d_b}^2, 0) \right) \Gamma_{\check{d}_j, \gamma, d_b}^{R*} m_{d_b} \Gamma_{\check{d}_i, \gamma, d_b}^L \\
& - 4 \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{d_b}^2, m_Z^2) \right) \Gamma_{\check{d}_j, Z, d_b}^{R*} m_{d_b} \Gamma_{\check{d}_i, Z, d_b}^L \\
& + \sum_{b=1}^3 B_0(p^2, m_{u_b}^2, m_{H^+}^2) \Gamma_{\check{d}_j, H^-, u_b}^{L*} m_{u_b} \Gamma_{\check{d}_i, H^-, u_b}^R \\
& - 4 \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{u_b}^2, m_{W^+}^2) \right) \Gamma_{\check{d}_j, W^-, u_b}^{R*} m_{u_b} \Gamma_{\check{d}_i, W^-, u_b}^L
\end{aligned} \tag{48}$$

$$\begin{aligned}
\Sigma_{i,j}^R(p^2) &= -\frac{1}{2} \sum_{a=1}^3 B_1(p^2, m_{d_a}^2, m_{A^0}^2) \Gamma_{\check{d}_j, d_a, A^0}^{R*} \Gamma_{\check{d}_i, d_a, A^0}^R - \frac{1}{2} \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_h^2) \Gamma_{\check{d}_j, h, d_b}^{R*} \Gamma_{\check{d}_i, h, d_b}^R \\
& - \frac{4}{3} \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, 0) \Gamma_{\check{d}_j, g, d_b}^{L*} \Gamma_{\check{d}_i, g, d_b}^L - \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, 0) \Gamma_{\check{d}_j, \gamma, d_b}^{L*} \Gamma_{\check{d}_i, \gamma, d_b}^L \\
& - \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_Z^2) \Gamma_{\check{d}_j, Z, d_b}^{L*} \Gamma_{\check{d}_i, Z, d_b}^L - \frac{1}{2} \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_{H^+}^2) \Gamma_{\check{d}_j, H^-, u_b}^{R*} \Gamma_{\check{d}_i, H^-, u_b}^R \\
& - \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_{W^+}^2) \Gamma_{\check{d}_j, W^-, u_b}^{L*} \Gamma_{\check{d}_i, W^-, u_b}^L
\end{aligned} \tag{49}$$

$$\begin{aligned}
\Sigma_{i,j}^L(p^2) &= -\frac{1}{2} \sum_{a=1}^3 B_1(p^2, m_{d_a}^2, m_{A^0}^2) \Gamma_{\check{d}_j, d_a, A^0}^{L*} \Gamma_{\check{d}_i, d_a, A^0}^L - \frac{1}{2} \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_h^2) \Gamma_{\check{d}_j, h, d_b}^{L*} \Gamma_{\check{d}_i, h, d_b}^L \\
& - \frac{4}{3} \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, 0) \Gamma_{\check{d}_j, g, d_b}^{R*} \Gamma_{\check{d}_i, g, d_b}^R - \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, 0) \Gamma_{\check{d}_j, \gamma, d_b}^{R*} \Gamma_{\check{d}_i, \gamma, d_b}^R \\
& - \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_Z^2) \Gamma_{\check{d}_j, Z, d_b}^{R*} \Gamma_{\check{d}_i, Z, d_b}^R - \frac{1}{2} \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_{H^+}^2) \Gamma_{\check{d}_j, H^-, u_b}^{L*} \Gamma_{\check{d}_i, H^-, u_b}^L \\
& - \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_{W^+}^2) \Gamma_{\check{d}_j, W^-, u_b}^{R*} \Gamma_{\check{d}_i, W^-, u_b}^R
\end{aligned} \tag{50}$$

• **Self-Energy for Up-Quarks** ( $u$ )

$$\begin{aligned}
\Sigma_{i,j}^S(p^2) &= + \sum_{a=1}^3 B_0(p^2, m_{u_a}^2, m_{A^0}^2) \Gamma_{\check{u}_j, u_a, A^0}^{L*} m_{u_a} \Gamma_{\check{u}_i, u_a, A^0}^R + \sum_{b=1}^3 B_0(p^2, m_{u_b}^2, m_h^2) \Gamma_{\check{u}_j, h, u_b}^{L*} m_{u_b} \Gamma_{\check{u}_i, h, u_b}^R \\
& + \sum_{b=1}^3 B_0(p^2, m_{d_b}^2, m_{H^+}^2) \Gamma_{\check{u}_j, H^+, d_b}^{L*} m_{d_b} \Gamma_{\check{u}_i, H^+, d_b}^R - \frac{16}{3} \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{u_b}^2, 0) \right) \Gamma_{\check{u}_j, g, u_b}^{R*} m_{u_b} \Gamma_{\check{u}_i, g, u_b}^L
\end{aligned}$$

$$\begin{aligned}
& -4 \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{u_b}^2, 0) \right) \Gamma_{\tilde{u}_j, \gamma, u_b}^{R*} m_{u_b} \Gamma_{\tilde{u}_i, \gamma, u_b}^L \\
& -4 \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{d_b}^2, m_{W^+}^2) \right) \Gamma_{\tilde{u}_j, W^+, d_b}^{R*} m_{d_b} \Gamma_{\tilde{u}_i, W^+, d_b}^L \\
& -4 \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{u_b}^2, m_Z^2) \right) \Gamma_{\tilde{u}_j, Z, u_b}^{R*} m_{u_b} \Gamma_{\tilde{u}_i, Z, u_b}^L
\end{aligned} \tag{51}$$

$$\begin{aligned}
\Sigma_{i,j}^R(p^2) = & -\frac{1}{2} \sum_{a=1}^3 B_1(p^2, m_{u_a}^2, m_{A^0}^2) \Gamma_{\tilde{u}_j, u_a, A^0}^{R*} \Gamma_{\tilde{u}_i, u_a, A^0}^R - \frac{1}{2} \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_h^2) \Gamma_{\tilde{u}_j, h, u_b}^{R*} \Gamma_{\tilde{u}_i, h, u_b}^R \\
& -\frac{1}{2} \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_{H^+}^2) \Gamma_{\tilde{u}_j, H^+, d_b}^{R*} \Gamma_{\tilde{u}_i, H^+, d_b}^R - \frac{4}{3} \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, 0) \Gamma_{\tilde{u}_j, g, u_b}^{L*} \Gamma_{\tilde{u}_i, g, u_b}^L \\
& -\sum_{b=1}^3 B_1(p^2, m_{u_b}^2, 0) \Gamma_{\tilde{u}_j, \gamma, u_b}^{L*} \Gamma_{\tilde{u}_i, \gamma, u_b}^L - \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_{W^+}^2) \Gamma_{\tilde{u}_j, W^+, d_b}^{L*} \Gamma_{\tilde{u}_i, W^+, d_b}^L \\
& -\sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_Z^2) \Gamma_{\tilde{u}_j, Z, u_b}^{L*} \Gamma_{\tilde{u}_i, Z, u_b}^L
\end{aligned} \tag{52}$$

$$\begin{aligned}
\Sigma_{i,j}^L(p^2) = & -\frac{1}{2} \sum_{a=1}^3 B_1(p^2, m_{u_a}^2, m_{A^0}^2) \Gamma_{\tilde{u}_j, u_a, A^0}^{L*} \Gamma_{\tilde{u}_i, u_a, A^0}^L - \frac{1}{2} \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_h^2) \Gamma_{\tilde{u}_j, h, u_b}^{L*} \Gamma_{\tilde{u}_i, h, u_b}^L \\
& -\frac{1}{2} \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_{H^+}^2) \Gamma_{\tilde{u}_j, H^+, d_b}^{L*} \Gamma_{\tilde{u}_i, H^+, d_b}^L - \frac{4}{3} \sum_{b=1}^3 B_1(p^2, m_{u_b}^2, 0) \Gamma_{\tilde{u}_j, g, u_b}^{R*} \Gamma_{\tilde{u}_i, g, u_b}^R \\
& -\sum_{b=1}^3 B_1(p^2, m_{u_b}^2, 0) \Gamma_{\tilde{u}_j, \gamma, u_b}^{R*} \Gamma_{\tilde{u}_i, \gamma, u_b}^R - \sum_{b=1}^3 B_1(p^2, m_{d_b}^2, m_{W^+}^2) \Gamma_{\tilde{u}_j, W^+, d_b}^{R*} \Gamma_{\tilde{u}_i, W^+, d_b}^R \\
& -\sum_{b=1}^3 B_1(p^2, m_{u_b}^2, m_Z^2) \Gamma_{\tilde{u}_j, Z, u_b}^{R*} \Gamma_{\tilde{u}_i, Z, u_b}^R
\end{aligned} \tag{53}$$

• **Self-Energy for Leptons ( $e$ )**

$$\begin{aligned}
\Sigma_{i,j}^S(p^2) = & + \sum_{a=1}^3 B_0(p^2, m_{e_a}^2, m_{A^0}^2) \Gamma_{\tilde{e}_j, e_a, A^0}^{L*} m_{e_a} \Gamma_{\tilde{e}_i, e_a, A^0}^R + \sum_{b=1}^3 B_0(p^2, m_{e_b}^2, m_h^2) \Gamma_{\tilde{e}_j, h, e_b}^{L*} m_{e_b} \Gamma_{\tilde{e}_i, h, e_b}^R \\
& -4 \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{e_b}^2, 0) \right) \Gamma_{\tilde{e}_j, \gamma, e_b}^{R*} m_{e_b} \Gamma_{\tilde{e}_i, \gamma, e_b}^L -4 \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{e_b}^2, m_Z^2) \right) \Gamma_{\tilde{e}_j, Z, e_b}^{R*} m_{e_b} \Gamma_{\tilde{e}_i, Z, e_b}^L \\
& + \sum_{b=1}^3 B_0(p^2, m_{\nu_b}^2, m_{H^+}^2) \Gamma_{\tilde{e}_j, H^-, \nu_b}^{L*} m_{\nu_b} \Gamma_{\tilde{e}_i, H^-, \nu_b}^R
\end{aligned}$$

$$-4 \sum_{b=1}^3 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{\nu_b}^2, m_{W^+}^2) \right) \Gamma_{\tilde{e}_j, W^-, \nu_b}^{R*} m_{\nu_b} \Gamma_{\tilde{e}_i, W^-, \nu_b}^L \quad (54)$$

$$\begin{aligned} \Sigma_{i,j}^R(p^2) = & -\frac{1}{2} \sum_{a=1}^3 B_1(p^2, m_{e_a}^2, m_{A^0}^2) \Gamma_{\tilde{e}_j, e_a, A^0}^{R*} \Gamma_{\tilde{e}_i, e_a, A^0}^R - \frac{1}{2} \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, m_h^2) \Gamma_{\tilde{e}_j, h, e_b}^{R*} \Gamma_{\tilde{e}_i, h, e_b}^R \\ & - \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, 0) \Gamma_{\tilde{e}_j, \gamma, e_b}^{L*} \Gamma_{\tilde{e}_i, \gamma, e_b}^L - \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, m_Z^2) \Gamma_{\tilde{e}_j, Z, e_b}^{L*} \Gamma_{\tilde{e}_i, Z, e_b}^L \\ & - \frac{1}{2} \sum_{b=1}^3 B_1(p^2, m_{\nu_b}^2, m_{H^+}^2) \Gamma_{\tilde{e}_j, H^-, \nu_b}^{R*} \Gamma_{\tilde{e}_i, H^-, \nu_b}^R - \sum_{b=1}^3 B_1(p^2, m_{\nu_b}^2, m_{W^+}^2) \Gamma_{\tilde{e}_j, W^-, \nu_b}^{L*} \Gamma_{\tilde{e}_i, W^-, \nu_b}^L \end{aligned} \quad (55)$$

$$\begin{aligned} \Sigma_{i,j}^L(p^2) = & -\frac{1}{2} \sum_{a=1}^3 B_1(p^2, m_{e_a}^2, m_{A^0}^2) \Gamma_{\tilde{e}_j, e_a, A^0}^{L*} \Gamma_{\tilde{e}_i, e_a, A^0}^L - \frac{1}{2} \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, m_h^2) \Gamma_{\tilde{e}_j, h, e_b}^{L*} \Gamma_{\tilde{e}_i, h, e_b}^L \\ & - \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, 0) \Gamma_{\tilde{e}_j, \gamma, e_b}^{R*} \Gamma_{\tilde{e}_i, \gamma, e_b}^R - \sum_{b=1}^3 B_1(p^2, m_{e_b}^2, m_Z^2) \Gamma_{\tilde{e}_j, Z, e_b}^{R*} \Gamma_{\tilde{e}_i, Z, e_b}^R \\ & - \frac{1}{2} \sum_{b=1}^3 B_1(p^2, m_{\nu_b}^2, m_{H^+}^2) \Gamma_{\tilde{e}_j, H^-, \nu_b}^{L*} \Gamma_{\tilde{e}_i, H^-, \nu_b}^L - \sum_{b=1}^3 B_1(p^2, m_{\nu_b}^2, m_{W^+}^2) \Gamma_{\tilde{e}_j, W^-, \nu_b}^{R*} \Gamma_{\tilde{e}_i, W^-, \nu_b}^R \end{aligned} \quad (56)$$

• **Self-Energy for Charged Higgs ( $H^+$ )**

$$\begin{aligned} \Pi(p^2) = & +4|\Gamma_{H^-, W^+, \gamma}|^2 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, 0, m_{W^+}^2) \right) + |\Gamma_{H^-, H^+, h}|^2 B_0(p^2, m_{H^+}^2, m_h^2) + 4|\Gamma_{H^-, Z, W^+}|^2 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{H^+}^2, m_Z^2) \right) \\ & - B_0(p^2, m_{\eta^+}^2, m_{\eta^-}^2) \Gamma_{H^+, \eta^-, \eta^+} \Gamma_{H^-, \eta^-, \eta^-} - B_0(p^2, m_{\eta^+}^2, m_{\eta^+}^2) \Gamma_{H^+, \eta^+, \eta^+} \Gamma_{H^-, \eta^+, \eta^+} \\ & - \frac{1}{2} A_0(m_{A^0}^2) \Gamma_{H^+, H^-, A^0, A^0} - \frac{1}{2} A_0(m_h^2) \Gamma_{H^+, H^-, h, h} - \frac{1}{2} A_0(m_S^2) \Gamma_{H^+, H^-, S, S} \\ & - A_0(m_{H^+}^2) \Gamma_{H^+, H^-, H^-, H^+} + |\Gamma_{H^-, W^+, A^0}|^2 F_0(p^2, m_{A^0}^2, m_{W^+}^2) + |\Gamma_{H^-, W^+, h}|^2 F_0(p^2, m_h^2, m_{W^+}^2) \\ & + |\Gamma_{H^-, \gamma, H^+}|^2 F_0(p^2, m_{H^+}^2, 0) + |\Gamma_{H^-, Z, H^+}|^2 F_0(p^2, m_{H^+}^2, m_Z^2) + 4\Gamma_{H^+, H^-, W^-, W^+} \left( -\frac{1}{2} \text{rMS} m_{W^+}^2 + A_0(m_{W^+}^2) \right) \\ & + 2\Gamma_{H^+, H^-, Z, Z} \left( -\frac{1}{2} \text{rMS} m_Z^2 + A_0(m_Z^2) \right) + 3 \sum_{a=1}^3 \sum_{b=1}^3 \left( |\Gamma_{H^-, \bar{d}_a, u_b}^L|^2 + |\Gamma_{H^-, \bar{d}_a, u_b}^R|^2 \right) G_0(p^2, m_{d_a}^2, m_{u_b}^2) \\ & + \sum_{a=1}^3 \sum_{b=1}^3 \left( |\Gamma_{H^-, \bar{e}_a, \nu_b}^L|^2 + |\Gamma_{H^-, \bar{e}_a, \nu_b}^R|^2 \right) G_0(p^2, m_{e_a}^2, m_{\nu_b}^2) \\ & - 6 \sum_{a=1}^3 m_{d_a} \sum_{b=1}^3 B_0(p^2, m_{d_a}^2, m_{u_b}^2) m_{u_b} \left( \Gamma_{H^-, \bar{d}_a, u_b}^{L*} \Gamma_{H^-, \bar{d}_a, u_b}^R + \Gamma_{H^-, \bar{d}_a, u_b}^{R*} \Gamma_{H^-, \bar{d}_a, u_b}^L \right) \\ & - 2 \sum_{a=1}^3 m_{e_a} \sum_{b=1}^3 B_0(p^2, m_{e_a}^2, m_{\nu_b}^2) m_{\nu_b} \left( \Gamma_{H^-, \bar{e}_a, \nu_b}^{L*} \Gamma_{H^-, \bar{e}_a, \nu_b}^R + \Gamma_{H^-, \bar{e}_a, \nu_b}^{R*} \Gamma_{H^-, \bar{e}_a, \nu_b}^L \right) \end{aligned} \quad (57)$$

• **Self-Energy for Singlet ( $S$ )**

$$\begin{aligned}\Pi(p^2) = & +|\Gamma_{S,S,h}|^2 B_0(p^2, m_S^2, m_h^2) - \frac{1}{2} A_0(m_{A^0}^2) \Gamma_{S,S,A^0,A^0} - \frac{1}{2} A_0(m_h^2) \Gamma_{S,S,h,h} - \frac{1}{2} A_0(m_S^2) \Gamma_{S,S,S,S} \\ & - A_0(m_{H^+}^2) \Gamma_{S,S,H^-,H^+}\end{aligned}\quad (58)$$

• **Self-Energy for Pseudo-Scalar Higgs ( $A^0$ )**

$$\begin{aligned}\Pi(p^2) = & +|\Gamma_{A^0,h,A^0}|^2 B_0(p^2, m_h^2, m_{A^0}^2) - B_0(p^2, m_{\eta^+}^2, m_{\eta^+}^2) \Gamma_{A^0,\eta^+,\eta^+}^2 - B_0(p^2, m_{\eta^-}^2, m_{\eta^-}^2) \Gamma_{A^0,\eta^-,\eta^-}^2 - \frac{1}{2} A_0(m_{A^0}^2) \Gamma_{A^0,A^0,A^0}, \\ & - \frac{1}{2} A_0(m_h^2) \Gamma_{A^0,A^0,h,h} - \frac{1}{2} A_0(m_S^2) \Gamma_{A^0,A^0,S,S} - A_0(m_{H^+}^2) \Gamma_{A^0,A^0,H^-,H^+} \\ & + |\Gamma_{A^0,Z,h}|^2 F_0(p^2, m_h^2, m_Z^2) + 2|\Gamma_{A^0,W^-,H^+}|^2 F_0(p^2, m_{H^+}^2, m_{W^+}^2) + 4\Gamma_{A^0,A^0,W^-,W^+} \left( -\frac{1}{2} \text{rMS} m_{W^+}^2 + A_0(m_{W^+}^2) \right) \\ & + 2\Gamma_{A^0,A^0,Z,Z} \left( -\frac{1}{2} \text{rMS} m_Z^2 + A_0(m_Z^2) \right) + 3 \sum_{a=1}^3 \sum_{b=1}^3 \left( |\Gamma_{A^0,\bar{d}_a,d_b}^L|^2 + |\Gamma_{A^0,\bar{d}_a,d_b}^R|^2 \right) G_0(p^2, m_{d_a}^2, m_{d_b}^2) \\ & + \sum_{a=1}^3 \sum_{b=1}^3 \left( |\Gamma_{A^0,\bar{e}_a,e_b}^L|^2 + |\Gamma_{A^0,\bar{e}_a,e_b}^R|^2 \right) G_0(p^2, m_{e_a}^2, m_{e_b}^2) \\ & + 3 \sum_{a=1}^3 \sum_{b=1}^3 \left( |\Gamma_{A^0,\bar{u}_a,u_b}^L|^2 + |\Gamma_{A^0,\bar{u}_a,u_b}^R|^2 \right) G_0(p^2, m_{u_a}^2, m_{u_b}^2) \\ & - 6 \sum_{a=1}^3 m_{d_a} \sum_{b=1}^3 B_0(p^2, m_{d_a}^2, m_{d_b}^2) m_{d_b} \left( \Gamma_{A^0,\bar{d}_a,d_b}^{L*} \Gamma_{A^0,\bar{d}_a,d_b}^R + \Gamma_{A^0,\bar{d}_a,d_b}^{R*} \Gamma_{A^0,\bar{d}_a,d_b}^L \right) \\ & - 2 \sum_{a=1}^3 m_{e_a} \sum_{b=1}^3 B_0(p^2, m_{e_a}^2, m_{e_b}^2) m_{e_b} \left( \Gamma_{A^0,\bar{e}_a,e_b}^{L*} \Gamma_{A^0,\bar{e}_a,e_b}^R + \Gamma_{A^0,\bar{e}_a,e_b}^{R*} \Gamma_{A^0,\bar{e}_a,e_b}^L \right) \\ & - 6 \sum_{a=1}^3 m_{u_a} \sum_{b=1}^3 B_0(p^2, m_{u_a}^2, m_{u_b}^2) m_{u_b} \left( \Gamma_{A^0,\bar{u}_a,u_b}^{L*} \Gamma_{A^0,\bar{u}_a,u_b}^R + \Gamma_{A^0,\bar{u}_a,u_b}^{R*} \Gamma_{A^0,\bar{u}_a,u_b}^L \right)\end{aligned}\quad (59)$$

• **Self-Energy for Higgs ( $h$ )**

$$\begin{aligned}\Pi(p^2) = & +\frac{1}{2} |\Gamma_{h,A^0,A^0}|^2 B_0(p^2, m_{A^0}^2, m_{A^0}^2) + \frac{1}{2} |\Gamma_{h,h,h}|^2 B_0(p^2, m_h^2, m_h^2) + |\Gamma_{h,H^-,H^+}|^2 B_0(p^2, m_{H^+}^2, m_{H^+}^2) + \frac{1}{2} |\Gamma_{h,S,S}|^2 B_0(p^2, \\ & + 4|\Gamma_{h,W^-,W^+}|^2 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_{W^+}^2, m_{W^+}^2) \right) + 2|\Gamma_{h,Z,Z}|^2 \left( -\frac{1}{2} \text{rMS} + B_0(p^2, m_Z^2, m_Z^2) \right) - B_0(p^2, m_{\eta^+}^2, m_{\eta^+}^2) \Gamma_{h,\eta^+,\eta^+}^2 \\ & - B_0(p^2, m_{\eta^-}^2, m_{\eta^-}^2) \Gamma_{h,\eta^-,\eta^-}^2 - B_0(p^2, m_{\eta^Z}^2, m_{\eta^Z}^2) \Gamma_{h,\eta^Z,\eta^Z}^2 - \frac{1}{2} A_0(m_{A^0}^2) \Gamma_{h,h,A^0,A^0} - \frac{1}{2} A_0(m_h^2) \Gamma_{h,h,h,h} \\ & - \frac{1}{2} A_0(m_S^2) \Gamma_{h,h,S,S} - A_0(m_{H^+}^2) \Gamma_{h,h,H^-,H^+} + |\Gamma_{h,Z,A^0}|^2 F_0(p^2, m_{A^0}^2, m_Z^2) \\ & + 2|\Gamma_{h,W^-,H^+}|^2 F_0(p^2, m_{H^+}^2, m_{W^+}^2) + 4\Gamma_{h,h,W^-,W^+} \left( -\frac{1}{2} \text{rMS} m_{W^+}^2 + A_0(m_{W^+}^2) \right) + 2\Gamma_{h,h,Z,Z} \left( -\frac{1}{2} \text{rMS} m_Z^2 + A_0(m_Z^2) \right)\end{aligned}$$

$$\begin{aligned}
& + 3 \sum_{a=1}^3 \sum_{b=1}^3 \left( |\Gamma_{h,\bar{d}_a,d_b}^L|^2 + |\Gamma_{h,\bar{d}_a,d_b}^R|^2 \right) G_0(p^2, m_{d_a}^2, m_{d_b}^2) \\
& + \sum_{a=1}^3 \sum_{b=1}^3 \left( |\Gamma_{h,\bar{e}_a,e_b}^L|^2 + |\Gamma_{h,\bar{e}_a,e_b}^R|^2 \right) G_0(p^2, m_{e_a}^2, m_{e_b}^2) \\
& + 3 \sum_{a=1}^3 \sum_{b=1}^3 \left( |\Gamma_{h,\bar{u}_a,u_b}^L|^2 + |\Gamma_{h,\bar{u}_a,u_b}^R|^2 \right) G_0(p^2, m_{u_a}^2, m_{u_b}^2) \\
& - 6 \sum_{a=1}^3 m_{d_a} \sum_{b=1}^3 B_0(p^2, m_{d_a}^2, m_{d_b}^2) m_{d_b} \left( \Gamma_{h,\bar{d}_a,d_b}^{L*} \Gamma_{h,\bar{d}_a,d_b}^R + \Gamma_{h,\bar{d}_a,d_b}^{R*} \Gamma_{h,\bar{d}_a,d_b}^L \right) \\
& - 2 \sum_{a=1}^3 m_{e_a} \sum_{b=1}^3 B_0(p^2, m_{e_a}^2, m_{e_b}^2) m_{e_b} \left( \Gamma_{h,\bar{e}_a,e_b}^{L*} \Gamma_{h,\bar{e}_a,e_b}^R + \Gamma_{h,\bar{e}_a,e_b}^{R*} \Gamma_{h,\bar{e}_a,e_b}^L \right) \\
& - 6 \sum_{a=1}^3 m_{u_a} \sum_{b=1}^3 B_0(p^2, m_{u_a}^2, m_{u_b}^2) m_{u_b} \left( \Gamma_{h,\bar{u}_a,u_b}^{L*} \Gamma_{h,\bar{u}_a,u_b}^R + \Gamma_{h,\bar{u}_a,u_b}^{R*} \Gamma_{h,\bar{u}_a,u_b}^L \right)
\end{aligned} \tag{60}$$

• **Self-Energy for Z-Boson** ( $Z$ )

$$\begin{aligned}
\Pi(p^2) = & + 2|\Gamma_{Z,W^-,H^+}|^2 B_0(p^2, m_{W^+}^2, m_{H^+}^2) + |\Gamma_{Z,Z,h}|^2 B_0(p^2, m_Z^2, m_h^2) - 4|\Gamma_{Z,h,A^0}|^2 B_{00}(p^2, m_{A^0}^2, m_h^2) \\
& + |\Gamma_{Z,\eta^+,\eta^+}|^2 B_{00}(p^2, m_{\eta^+}^2, m_{\eta^+}^2) + |\Gamma_{Z,\eta^+,\eta^-}|^2 B_{00}(p^2, m_{\eta^-}^2, m_{\eta^-}^2) \\
& - 4|\Gamma_{Z,H^-,H^+}|^2 B_{00}(p^2, m_{H^+}^2, m_{H^+}^2) + \frac{1}{2} A_0(m_{A^0}^2) \Gamma_{Z,Z,A^0,A^0} + \frac{1}{2} A_0(m_h^2) \Gamma_{Z,Z,h,h} \\
& + A_0(m_{H^+}^2) \Gamma_{Z,Z,H^-,H^+} \\
& - |\Gamma_{Z,W^-,W^+}|^2 \left( 10 B_{00}(p^2, m_{W^+}^2, m_{W^+}^2) + 2 A_0(m_{W^+}^2) - 2 \text{rMS} \left( 2 m_{W^+}^2 - \frac{1}{3} p^2 \right) + B_0(p^2, m_{W^+}^2, m_{W^+}^2) (2 m_{W^+}^2 + 4 p^2) \right) \\
& + 3 \sum_{a=1}^3 \sum_{b=1}^3 \left[ \left( |\Gamma_{Z,\bar{d}_a,d_b}^L|^2 + |\Gamma_{Z,\bar{d}_a,d_b}^R|^2 \right) H_0(p^2, m_{d_a}^2, m_{d_b}^2) \right. \\
& \left. + 4 B_0(p^2, m_{d_a}^2, m_{d_b}^2) m_{d_a} m_{d_b} \Re \left( \Gamma_{Z,\bar{d}_a,d_b}^{L*} \Gamma_{Z,\bar{d}_a,d_b}^R \right) \right] \\
& + \sum_{a=1}^3 \sum_{b=1}^3 \left[ \left( |\Gamma_{Z,\bar{e}_a,e_b}^L|^2 + |\Gamma_{Z,\bar{e}_a,e_b}^R|^2 \right) H_0(p^2, m_{e_a}^2, m_{e_b}^2) \right. \\
& \left. + 4 B_0(p^2, m_{e_a}^2, m_{e_b}^2) m_{e_a} m_{e_b} \Re \left( \Gamma_{Z,\bar{e}_a,e_b}^{L*} \Gamma_{Z,\bar{e}_a,e_b}^R \right) \right] \\
& + 3 \sum_{a=1}^3 \sum_{b=1}^3 \left[ \left( |\Gamma_{Z,\bar{u}_a,u_b}^L|^2 + |\Gamma_{Z,\bar{u}_a,u_b}^R|^2 \right) H_0(p^2, m_{u_a}^2, m_{u_b}^2) \right. \\
& \left. + 4 B_0(p^2, m_{u_a}^2, m_{u_b}^2) m_{u_a} m_{u_b} \Re \left( \Gamma_{Z,\bar{u}_a,u_b}^{L*} \Gamma_{Z,\bar{u}_a,u_b}^R \right) \right]
\end{aligned}$$

$$\begin{aligned}
& + \sum_{a=1}^3 \sum_{b=1}^3 \left[ \left( |\Gamma_{Z,\bar{\nu}_a,\nu_b}^L|^2 + |\Gamma_{Z,\bar{\nu}_a,\nu_b}^R|^2 \right) H_0(p^2, m_{\nu_a}^2, m_{\nu_b}^2) \right. \\
& + 4B_0(p^2, m_{\nu_a}^2, m_{\nu_b}^2) m_{\nu_a} m_{\nu_b} \Re \left( \Gamma_{Z,\bar{\nu}_a,\nu_b}^{L*} \Gamma_{Z,\bar{\nu}_a,\nu_b}^R \right) \left. \right] + 2\text{rMS} m_{W^+}^2 \Gamma_{Z,Z,W^-,W^+}^1 \\
& - A_0(m_{W^+}^2) \left( 4\Gamma_{Z,Z,W^-,W^+}^1 + \Gamma_{Z,Z,W^-,W^+}^2 + \Gamma_{Z,Z,W^-,W^+}^3 \right)
\end{aligned} \tag{61}$$

• **Self-Energy for  $W^+$  - Boson ( $W^+$ )**

$$\begin{aligned}
\Pi(p^2) &= 2\text{rMS} m_{W^+}^2 \Gamma_{W^+,W^-,W^-,W^+}^1 + 3 \sum_{a=1}^3 \sum_{b=1}^3 \left[ \left( |\Gamma_{W^-, \bar{d}_a, u_b}^L|^2 + |\Gamma_{W^-, \bar{d}_a, u_b}^R|^2 \right) H_0(p^2, m_{d_a}^2, m_{u_b}^2) \right. \\
& + 4B_0(p^2, m_{d_a}^2, m_{u_b}^2) m_{d_a} m_{u_b} \Re \left( \Gamma_{W^-, \bar{d}_a, u_b}^{L*} \Gamma_{W^-, \bar{d}_a, u_b}^R \right) \left. \right] - 4|\Gamma_{W^-, H^+, A^0}|^2 B_{00}(p^2, m_{A^0}^2, m_{H^+}^2) - 4|\Gamma_{W^-, H^+, h}|^2 B_{00}(p^2, m_h^2, m_{H^+}^2) \\
& + 4B_0(p^2, m_{e_a}^2, m_{\nu_b}^2) m_{e_a} m_{\nu_b} \Re \left( \Gamma_{W^-, \bar{e}_a, \nu_b}^{L*} \Gamma_{W^-, \bar{e}_a, \nu_b}^R \right)
\end{aligned} \tag{62}$$

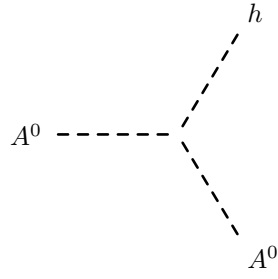
## 8.2 Tadpoles

$$\begin{aligned}
\delta t_h^{(1)} &= -\frac{1}{2} A_0(m_{A^0}^2) \Gamma_{h,A^0,A^0} - \frac{1}{2} A_0(m_h^2) \Gamma_{h,h,h} - \frac{1}{2} A_0(m_S^2) \Gamma_{h,S,S} + A_0(m_{\eta^+}^2) \Gamma_{h,\eta^+, \eta^+} \\
& + A_0(m_{\eta^-}^2) \Gamma_{h,\eta^-, \eta^-} + A_0(m_{\eta^Z}^2) \Gamma_{h,\eta^Z, \eta^Z} - A_0(m_{H^+}^2) \Gamma_{h,H^-, H^+} \\
& + 4\Gamma_{h,W^-,W^+} \left( -\frac{1}{2} \text{rMS} m_{W^+}^2 + A_0(m_{W^+}^2) \right) + 2\Gamma_{h,Z,Z} \left( -\frac{1}{2} \text{rMS} m_Z^2 + A_0(m_Z^2) \right) \\
& + 6 \sum_{a=1}^3 A_0(m_{d_a}^2) m_{d_a} \left( \Gamma_{h,\bar{d}_a,d_a}^L + \Gamma_{h,\bar{d}_a,d_a}^R \right) \\
& + 2 \sum_{a=1}^3 A_0(m_{e_a}^2) m_{e_a} \left( \Gamma_{h,\bar{e}_a,e_a}^L + \Gamma_{h,\bar{e}_a,e_a}^R \right) \\
& + 6 \sum_{a=1}^3 A_0(m_{u_a}^2) m_{u_a} \left( \Gamma_{h,\bar{u}_a,u_a}^L + \Gamma_{h,\bar{u}_a,u_a}^R \right)
\end{aligned} \tag{63}$$



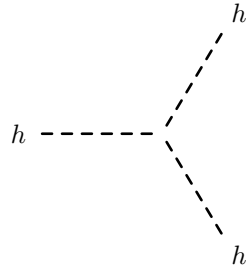
## 9 Interactions for eigenstates 'EWSB'

### 9.1 Three Scalar-Interaction



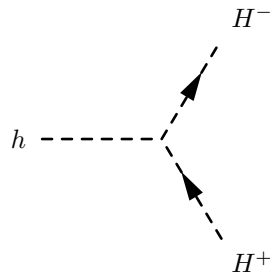
$$-i\lambda v \quad (64)$$


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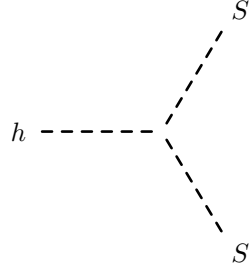
$$-3i\lambda v \quad (65)$$


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$$-i\lambda v \quad (66)$$

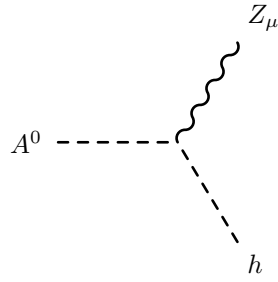

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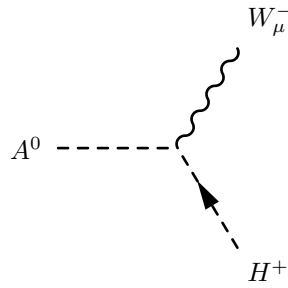

$$-2iLamSHv \quad (67)$$

## 9.2 Two Scalar-One Vector Boson-Interaction



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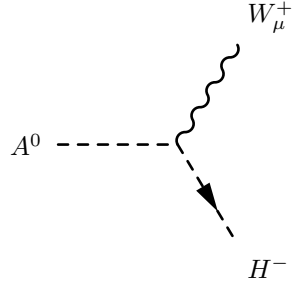

$$\frac{1}{2} \left( -g_1 \sin \Theta_W - g_2 \cos \Theta_W \right) \left( -p_\mu^h + p_\mu^{A^0} \right) \quad (68)$$



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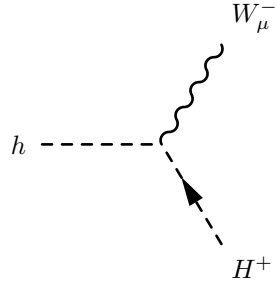

$$\frac{1}{2} g_2 \left( -p_\mu^{H^+} + p_\mu^{A^0} \right) \quad (69)$$


---



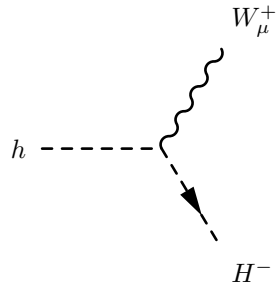
$$\frac{1}{2}g_2\left(-p_\mu^{H^-}+p_\mu^{A^0}\right) \quad (70)$$


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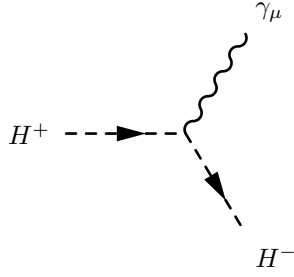
$$\frac{i}{2}g_2\left(-p_\mu^{H^+}+p_\mu^h\right) \quad (71)$$


---



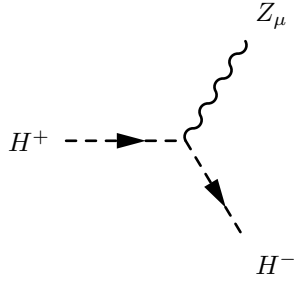
$$-\frac{i}{2}g_2\left(-p_\mu^{H^-}+p_\mu^h\right) \quad (72)$$


---



$$-\frac{i}{2}\left(g_1 \cos \Theta_W + g_2 \sin \Theta_W\right)\left(-p_\mu^{H^-} + p_\mu^{H^+}\right) \quad (73)$$

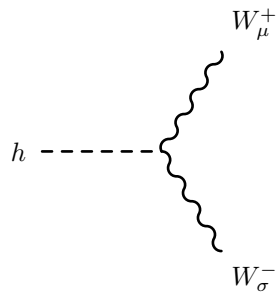

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$$-\frac{i}{2}\left(-g_1 \sin \Theta_W + g_2 \cos \Theta_W\right)\left(-p_\mu^{H^-} + p_\mu^{H^+}\right) \quad (74)$$

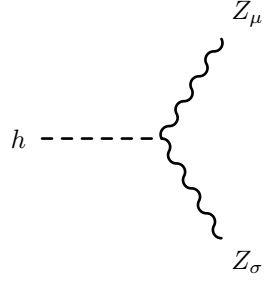

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### 9.3 One Scalar-Two Vector Boson-Interaction



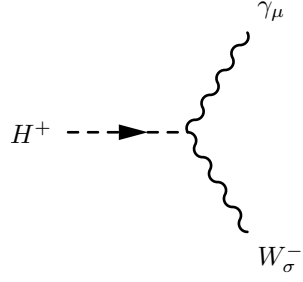
$$\frac{i}{2}g_2^2 v\left(g_{\sigma\mu}\right) \quad (75)$$


---



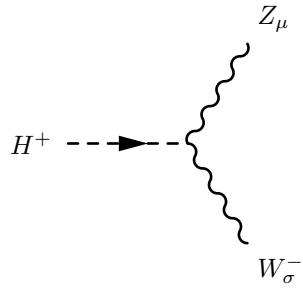
$$\frac{i}{2}v\left(g_1\sin\Theta_W+g_2\cos\Theta_W\right)^2\left(g_{\sigma\mu}\right) \quad (76)$$


---



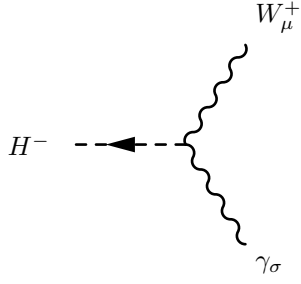
$$\frac{i}{2}g_1g_2v\cos\Theta_W\left(g_{\sigma\mu}\right) \quad (77)$$


---



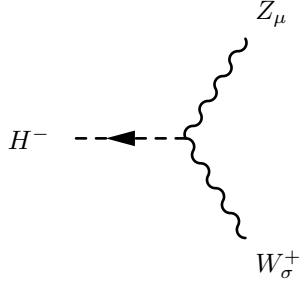
$$-\frac{i}{2}g_1g_2v\sin\Theta_W\left(g_{\sigma\mu}\right) \quad (78)$$


---



$$\frac{i}{2}g_1g_2v\cos\Theta_W\left(g_{\sigma\mu}\right) \quad (79)$$

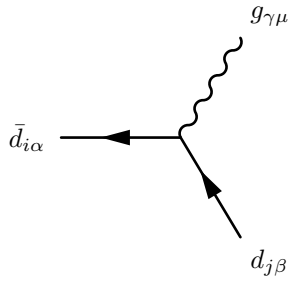

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$$-\frac{i}{2}g_1g_2v\sin\Theta_W\left(g_{\sigma\mu}\right) \quad (80)$$


---

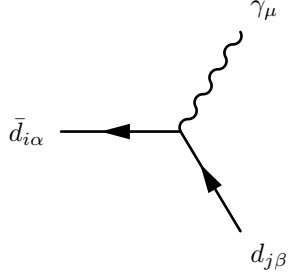
#### 9.4 Two Fermion-One Vector Boson-Interaction



$$-\frac{i}{2}g_3\delta_{ij}\lambda_{\alpha,\beta}^\gamma\left(\gamma_\mu\cdot\frac{1-\gamma_5}{2}\right) \quad (81)$$

$$+\frac{i}{2}g_3\delta_{ij}\lambda_{\alpha,\beta}^\gamma\left(\gamma_\mu\cdot\frac{1+\gamma_5}{2}\right) \quad (82)$$

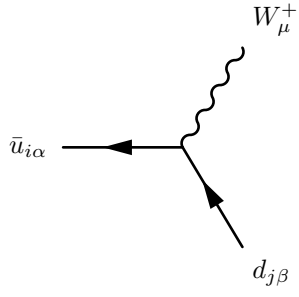

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$$-\frac{i}{6}\delta_{\alpha\beta}\delta_{ij}\left(-3g_2\sin\Theta_W+g_1\cos\Theta_W\right)\left(\gamma_\mu\cdot\frac{1-\gamma_5}{2}\right) \quad (83)$$

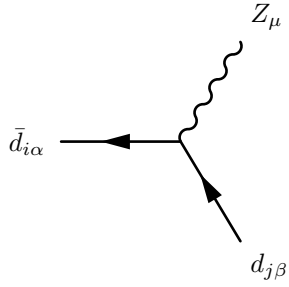
$$+\frac{i}{3}g_1\cos\Theta_W\delta_{\alpha\beta}\delta_{ij}\left(\gamma_\mu\cdot\frac{1+\gamma_5}{2}\right) \quad (84)$$


---



$$-i\frac{1}{\sqrt{2}}g_2\delta_{\alpha\beta}\sum_{a=1}^3U_{L,ja}^{d,*}U_{L,ia}^u\left(\gamma_\mu\cdot\frac{1-\gamma_5}{2}\right) \quad (85)$$

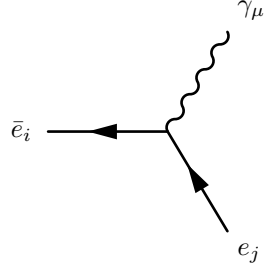

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$$\frac{i}{6}\delta_{\alpha\beta}\delta_{ij}\left(3g_2\cos\Theta_W+g_1\sin\Theta_W\right)\left(\gamma_\mu\cdot\frac{1-\gamma_5}{2}\right) \quad (86)$$

$$+\frac{i}{3}g_1\delta_{\alpha\beta}\delta_{ij}\sin\Theta_W\left(\gamma_\mu\cdot\frac{1+\gamma_5}{2}\right) \quad (87)$$

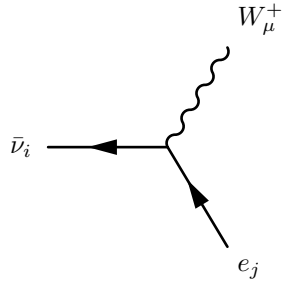

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$$\frac{i}{2}\delta_{ij}\left(g_1\cos\Theta_W+g_2\sin\Theta_W\right)\left(\gamma_\mu\cdot\frac{1-\gamma_5}{2}\right) \quad (88)$$

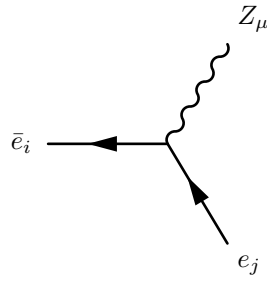
$$+ig_1\cos\Theta_W\delta_{ij}\left(\gamma_\mu\cdot\frac{1+\gamma_5}{2}\right) \quad (89)$$


---



$$-i\frac{1}{\sqrt{2}}g_2U_{L,ji}^{e,*}\Theta_{i,3}\left(\gamma_\mu\cdot\frac{1-\gamma_5}{2}\right) \quad (90)$$


---

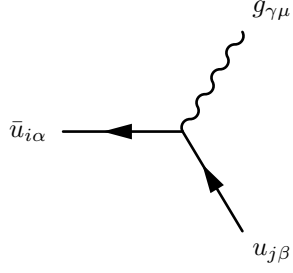


$$\frac{i}{2}\delta_{ij}\left(-g_1\sin\Theta_W+g_2\cos\Theta_W\right)\left(\gamma_\mu\cdot\frac{1-\gamma_5}{2}\right) \quad (91)$$

$$+ -ig_1\delta_{ij}\sin\Theta_W\left(\gamma_\mu\cdot\frac{1+\gamma_5}{2}\right) \quad (92)$$


---

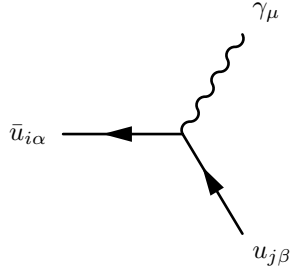




$$-\frac{i}{2}g_3\delta_{ij}\lambda_{\alpha,\beta}^\gamma\left(\gamma_\mu\cdot\frac{1-\gamma_5}{2}\right) \quad (93)$$

$$+\frac{i}{2}g_3\delta_{ij}\lambda_{\alpha,\beta}^\gamma\left(\gamma_\mu\cdot\frac{1+\gamma_5}{2}\right) \quad (94)$$

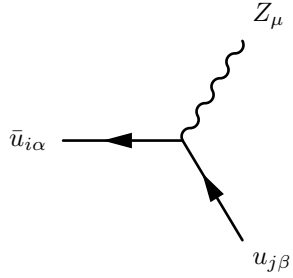

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$$-\frac{i}{6}\delta_{\alpha\beta}\delta_{ij}\left(3g_2\sin\Theta_W+g_1\cos\Theta_W\right)\left(\gamma_\mu\cdot\frac{1-\gamma_5}{2}\right) \quad (95)$$

$$+\frac{2i}{3}g_1\cos\Theta_W\delta_{\alpha\beta}\delta_{ij}\left(\gamma_\mu\cdot\frac{1+\gamma_5}{2}\right) \quad (96)$$

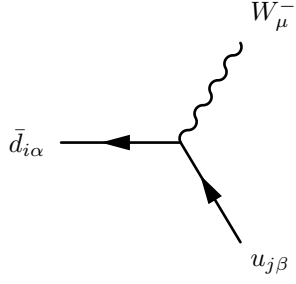

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$$-\frac{i}{6}\delta_{\alpha\beta}\delta_{ij}\left(3g_2\cos\Theta_W-g_1\sin\Theta_W\right)\left(\gamma_\mu\cdot\frac{1-\gamma_5}{2}\right) \quad (97)$$

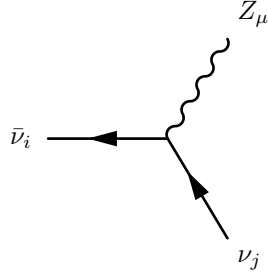
$$+\frac{2i}{3}g_1\delta_{\alpha\beta}\delta_{ij}\sin\Theta_W\left(\gamma_\mu\cdot\frac{1+\gamma_5}{2}\right) \quad (98)$$


---



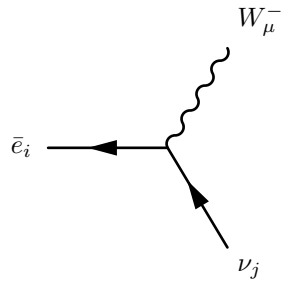
$$-i \frac{1}{\sqrt{2}} g_2 \delta_{\alpha\beta} \sum_{a=1}^3 U_{L,ja}^{u,*} U_{L,ia}^d \left( \gamma_\mu \cdot \frac{1 - \gamma_5}{2} \right) \quad (99)$$


---



$$-\frac{i}{2} \delta_{ij} \left( g_1 \sin \Theta_W + g_2 \cos \Theta_W \right) \left( \gamma_\mu \cdot \frac{1 - \gamma_5}{2} \right) \quad (100)$$

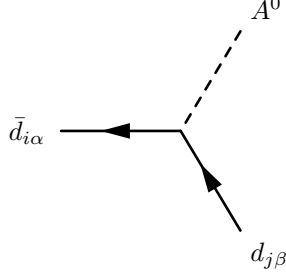

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$$-i \frac{1}{\sqrt{2}} g_2 \Theta_{j,3} U_{L,ij}^e \left( \gamma_\mu \cdot \frac{1 - \gamma_5}{2} \right) \quad (101)$$


---

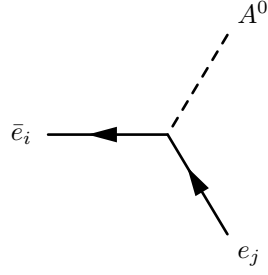
## 9.5 Two Fermion-One Scalar Boson-Interaction



$$- \frac{1}{\sqrt{2}} \delta_{\alpha\beta} \sum_{b=1}^3 U_{L,jb}^{d,*} \sum_{a=1}^3 U_{R,ia}^{d,*} Y_{d,ab} \left( \frac{1-\gamma_5}{2} \right) \quad (102)$$

$$+ \frac{1}{\sqrt{2}} \delta_{\alpha\beta} \sum_{b=1}^3 \sum_{a=1}^3 Y_{d,ab}^* U_{R,ja}^d U_{L,ib}^d \left( \frac{1+\gamma_5}{2} \right) \quad (103)$$

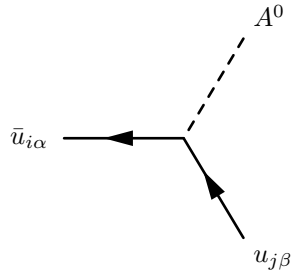

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$$- \frac{1}{\sqrt{2}} \sum_{b=1}^3 U_{L,jb}^{e,*} \sum_{a=1}^3 U_{R,ia}^{e,*} Y_{e,ab} \left( \frac{1-\gamma_5}{2} \right) \quad (104)$$

$$+ \frac{1}{\sqrt{2}} \sum_{b=1}^3 \sum_{a=1}^3 Y_{e,ab}^* U_{R,ja}^e U_{L,ib}^e \left( \frac{1+\gamma_5}{2} \right) \quad (105)$$

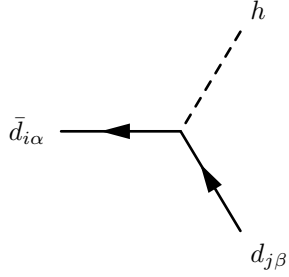

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$$- \frac{1}{\sqrt{2}} \delta_{\alpha\beta} \sum_{b=1}^3 U_{L,jb}^{u,*} \sum_{a=1}^3 U_{R,ia}^{u,*} Y_{u,ab} \left( \frac{1-\gamma_5}{2} \right) \quad (106)$$

$$+ \frac{1}{\sqrt{2}} \delta_{\alpha\beta} \sum_{b=1}^3 \sum_{a=1}^3 Y_{u,ab}^* U_{R,ja}^u U_{L,ib}^u \left( \frac{1+\gamma_5}{2} \right) \quad (107)$$

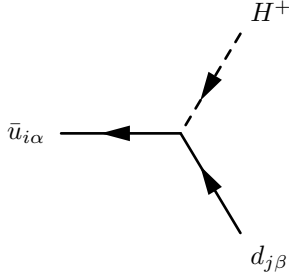

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$$- i \frac{1}{\sqrt{2}} \delta_{\alpha\beta} \sum_{b=1}^3 U_{L,jb}^{d,*} \sum_{a=1}^3 U_{R,ia}^{d,*} Y_{d,ab} \left( \frac{1-\gamma_5}{2} \right) \quad (108)$$

$$+ -i \frac{1}{\sqrt{2}} \delta_{\alpha\beta} \sum_{b=1}^3 \sum_{a=1}^3 Y_{d,ab}^* U_{R,ja}^d U_{L,ib}^d \left( \frac{1+\gamma_5}{2} \right) \quad (109)$$

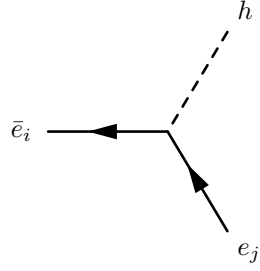

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$$- i \delta_{\alpha\beta} \sum_{b=1}^3 U_{L,jb}^{d,*} \sum_{a=1}^3 U_{R,ia}^{u,*} Y_{u,ab} \left( \frac{1-\gamma_5}{2} \right) \quad (110)$$

$$+ -i \delta_{\alpha\beta} \sum_{b=1}^3 \sum_{a=1}^3 Y_{d,ab}^* U_{R,ja}^d U_{L,ib}^u \left( \frac{1+\gamma_5}{2} \right) \quad (111)$$

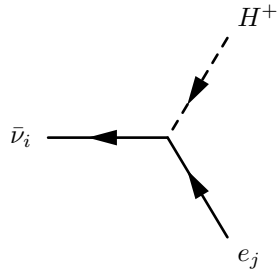

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$$-i \frac{1}{\sqrt{2}} \sum_{b=1}^3 U_{L,jb}^{e,*} \sum_{a=1}^3 U_{R,ia}^{e,*} Y_{e,ab} \left( \frac{1-\gamma_5}{2} \right) \quad (112)$$

$$+ -i \frac{1}{\sqrt{2}} \sum_{b=1}^3 \sum_{a=1}^3 Y_{e,ab}^* U_{R,ja}^e U_{L,ib}^e \left( \frac{1+\gamma_5}{2} \right) \quad (113)$$

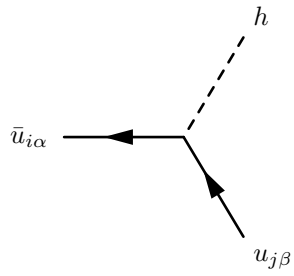

---



$$(114)$$

$$+ -i \sum_{a=1}^3 Y_{e,ai}^* U_{R,ja}^e \left( \frac{1+\gamma_5}{2} \right) \quad (115)$$

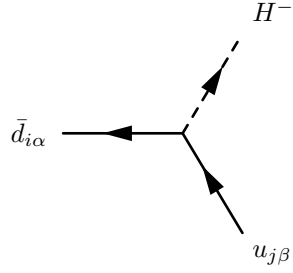

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$$i \frac{1}{\sqrt{2}} \delta_{\alpha\beta} \sum_{b=1}^3 U_{L,jb}^{u,*} \sum_{a=1}^3 U_{R,ia}^{u,*} Y_{u,ab} \left( \frac{1-\gamma_5}{2} \right) \quad (116)$$

$$+ i \frac{1}{\sqrt{2}} \delta_{\alpha\beta} \sum_{b=1}^3 \sum_{a=1}^3 Y_{u,ab}^* U_{R,ja}^u U_{L,ib}^u \left( \frac{1+\gamma_5}{2} \right) \quad (117)$$

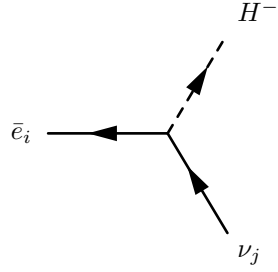

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$$- i \delta_{\alpha\beta} \sum_{b=1}^3 U_{L,jb}^{u,*} \sum_{a=1}^3 U_{R,ia}^{d,*} Y_{d,ab} \left( \frac{1-\gamma_5}{2} \right) \quad (118)$$

$$+ -i \delta_{\alpha\beta} \sum_{b=1}^3 \sum_{a=1}^3 Y_{u,ab}^* U_{R,ja}^u U_{L,ib}^d \left( \frac{1+\gamma_5}{2} \right) \quad (119)$$

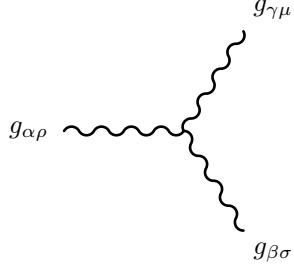

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$$- i \sum_{a=1}^3 U_{R,ia}^{e,*} Y_{e,aj} \left( \frac{1-\gamma_5}{2} \right) \quad (120)$$

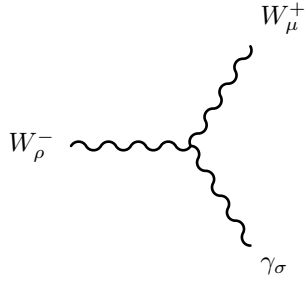

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## 9.6 Three Vector Boson-Interaction



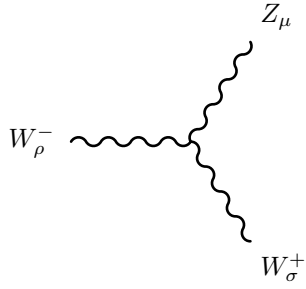
$$g_3 f_{\alpha,\beta,\gamma} \left( g_{\rho\mu} \left( -p_\sigma^{g_{\gamma\mu}} + p_\sigma^{g_{\alpha\rho}} \right) + g_{\rho\sigma} \left( -p_\mu^{g_{\alpha\rho}} + p_\mu^{g_{\beta\sigma}} \right) + g_{\sigma\mu} \left( -p_\rho^{g_{\beta\sigma}} + p_\rho^{g_{\gamma\mu}} \right) \right) \quad (121)$$


---



$$-ig_2 \sin \Theta_W \left( g_{\rho\mu} \left( -p_\sigma^{W_\mu^+} + p_\sigma^{W_\rho^-} \right) + g_{\rho\sigma} \left( -p_\mu^{W_\rho^-} + p_\mu^{\gamma_\sigma} \right) + g_{\sigma\mu} \left( -p_\rho^{\gamma_\sigma} + p_\rho^{W_\mu^+} \right) \right) \quad (122)$$

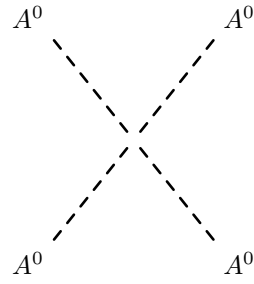

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$$ig_2 \cos \Theta_W \left( g_{\rho\mu} \left( -p_\sigma^{Z_\mu} + p_\sigma^{W_\rho^-} \right) + g_{\rho\sigma} \left( -p_\mu^{W_\rho^-} + p_\mu^{W_\sigma^+} \right) + g_{\sigma\mu} \left( -p_\rho^{W_\sigma^+} + p_\rho^{Z_\mu} \right) \right) \quad (123)$$

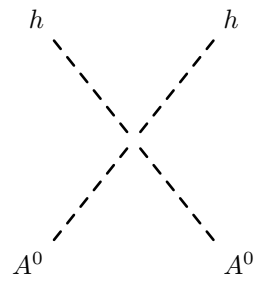

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## 9.7 Four Scalar-Interaction



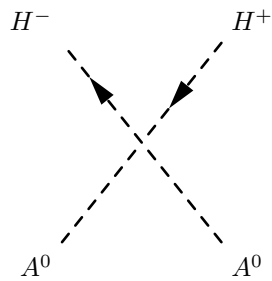
$$-3i\lambda \quad (124)$$


---



$$-i\lambda \quad (125)$$

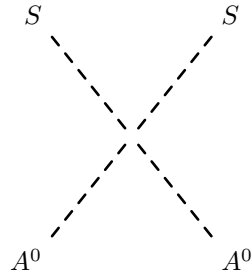

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$$-i\lambda \quad (126)$$

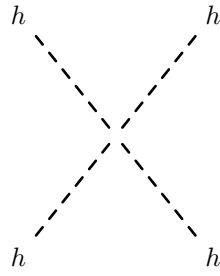

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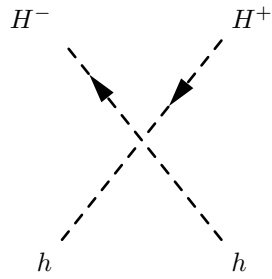
$$-2iLamSH \quad (127)$$


---



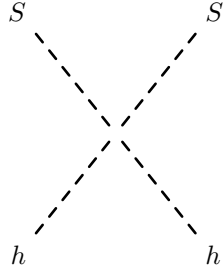
$$-3i\lambda \quad (128)$$


---



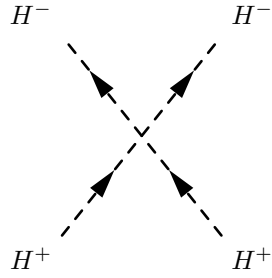
$$-i\lambda \quad (129)$$


---



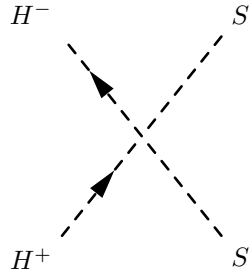
$$-2iLamSH \quad (130)$$


---



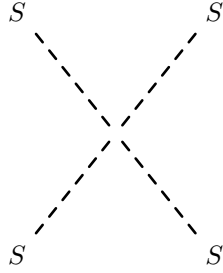
$$-2i\lambda \quad (131)$$


---



$$-2iLamSH \quad (132)$$

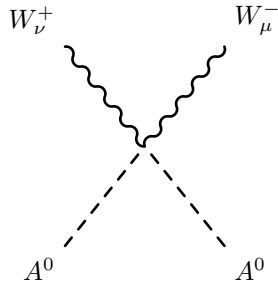

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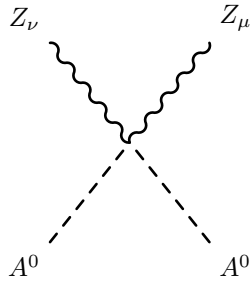

$$-12iLamS \quad (133)$$

## 9.8 Two Scalar-Two Vector Boson-Interaction



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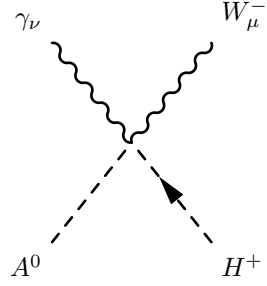

$$\frac{i}{2}g_2^2(g_{\mu\nu}) \quad (134)$$



---

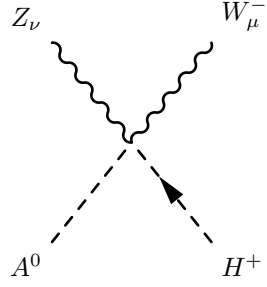

$$\frac{i}{2}\left(g_1 \sin \Theta_W + g_2 \cos \Theta_W\right)^2(g_{\mu\nu}) \quad (135)$$


---



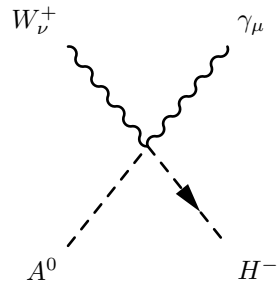
$$\frac{1}{2}g_1g_2\cos\Theta_W\left(g_{\mu\nu}\right) \quad (136)$$


---



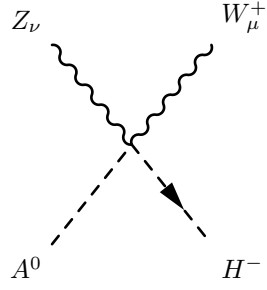
$$-\frac{1}{2}g_1g_2\sin\Theta_W\left(g_{\mu\nu}\right) \quad (137)$$


---



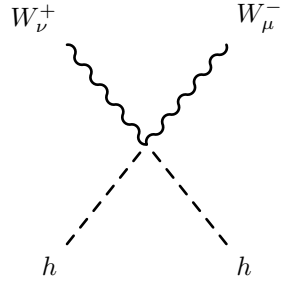
$$-\frac{1}{2}g_1g_2\cos\Theta_W\left(g_{\mu\nu}\right) \quad (138)$$


---



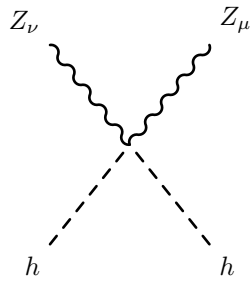
$$\frac{1}{2}g_1g_2\sin\Theta_W\left(g_{\mu\nu}\right) \quad (139)$$


---



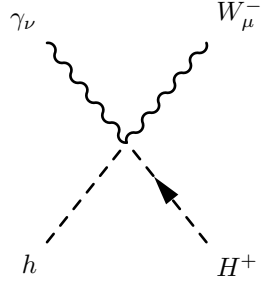
$$\frac{i}{2}g_2^2\left(g_{\mu\nu}\right) \quad (140)$$


---



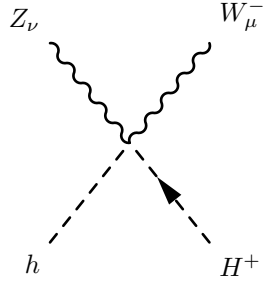
$$\frac{i}{2}\left(g_1\sin\Theta_W+g_2\cos\Theta_W\right)^2\left(g_{\mu\nu}\right) \quad (141)$$


---



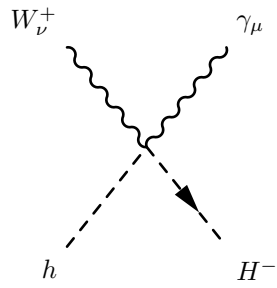
$$\frac{i}{2} g_1 g_2 \cos \Theta_W (g_{\mu\nu}) \quad (142)$$


---



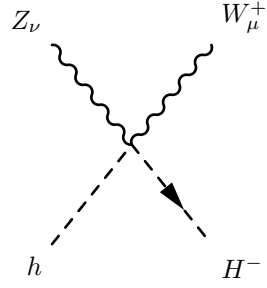
$$-\frac{i}{2} g_1 g_2 \sin \Theta_W (g_{\mu\nu}) \quad (143)$$


---



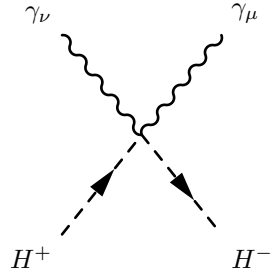
$$\frac{i}{2} g_1 g_2 \cos \Theta_W (g_{\mu\nu}) \quad (144)$$


---



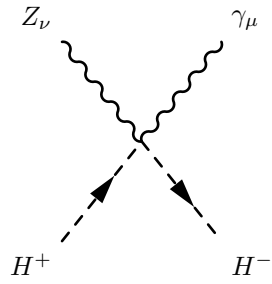
$$-\frac{i}{2}g_1g_2\sin\Theta_W\left(g_{\mu\nu}\right) \quad (145)$$


---



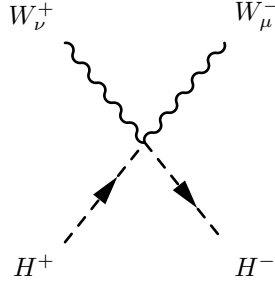
$$\frac{i}{2}\left(g_1\cos\Theta_W+g_2\sin\Theta_W\right)^2\left(g_{\mu\nu}\right) \quad (146)$$


---



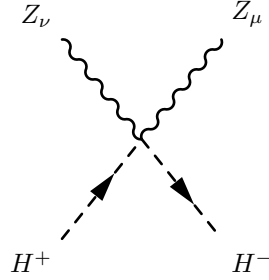
$$-\frac{i}{4}\left(-2g_1g_2\cos2\Theta_W+\left(-g_2^2+g_1^2\right)\sin2\Theta_W\right)\left(g_{\mu\nu}\right) \quad (147)$$


---



$$\frac{i}{2}g_2^2(g_{\mu\nu}) \quad (148)$$

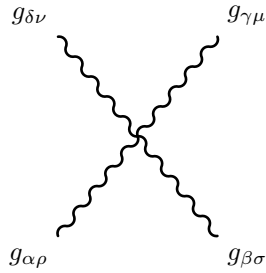

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$$\frac{i}{2}\left(-g_1\sin\Theta_W + g_2\cos\Theta_W\right)^2(g_{\mu\nu}) \quad (149)$$


---

## 9.9 Four Vector Boson-Interaction



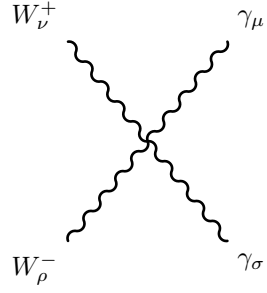
$$-ig_3^2\left(\sum_{a=1}^8 f_{\alpha,\delta,a}f_{\beta,\gamma,a} + \sum_{a=1}^8 f_{\alpha,\gamma,a}f_{\beta,\delta,a}\right)(g_{\rho\sigma}g_{\mu\nu}) \quad (150)$$

$$+ ig_3^2\left(-\sum_{a=1}^8 f_{\alpha,\beta,a}f_{\gamma,\delta,a} + \sum_{a=1}^8 f_{\alpha,\delta,a}f_{\beta,\gamma,a}\right)(g_{\rho\mu}g_{\sigma\nu}) \quad (151)$$



$$+ ig_3^2 \left( \sum_{a=1}^8 f_{\alpha,\gamma,a} f_{\beta,\delta,a} + \sum_{a=1}^8 f_{\alpha,\beta,a} f_{\gamma,\delta,a} \right) (g_{\rho\nu} g_{\sigma\mu}) \quad (152)$$


---

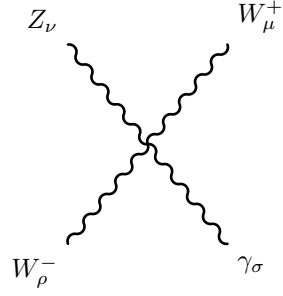


$$ig_2^2 \sin \Theta_W^2 (g_{\rho\sigma} g_{\mu\nu}) \quad (153)$$

$$+ ig_2^2 \sin \Theta_W^2 (g_{\rho\mu} g_{\sigma\nu}) \quad (154)$$

$$+ -2ig_2^2 \sin \Theta_W^2 (g_{\rho\nu} g_{\sigma\mu}) \quad (155)$$


---

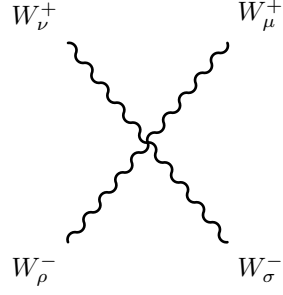


$$ig_2^2 \cos \Theta_W \sin \Theta_W (g_{\rho\sigma} g_{\mu\nu}) \quad (156)$$

$$+ -ig_2^2 \sin 2\Theta_W (g_{\rho\mu} g_{\sigma\nu}) \quad (157)$$

$$+ ig_2^2 \cos \Theta_W \sin \Theta_W (g_{\rho\nu} g_{\sigma\mu}) \quad (158)$$

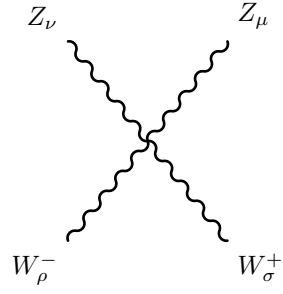

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$$2ig_2^2(g_{\rho\sigma}g_{\mu\nu}) \quad (159)$$

$$+ -ig_2^2(g_{\rho\mu}g_{\sigma\nu}) \quad (160)$$

$$+ -ig_2^2(g_{\rho\nu}g_{\sigma\mu}) \quad (161)$$

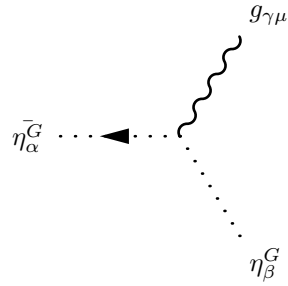


$$- 2ig_2^2 \cos \Theta_W^2(g_{\rho\sigma}g_{\mu\nu}) \quad (162)$$

$$+ ig_2^2 \cos \Theta_W^2(g_{\rho\mu}g_{\sigma\nu}) \quad (163)$$

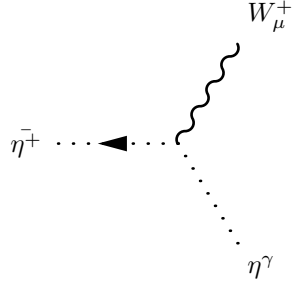
$$+ ig_2^2 \cos \Theta_W^2(g_{\rho\nu}g_{\sigma\mu}) \quad (164)$$

## 9.10 Two Ghosts-One Vector Boson-Interaction



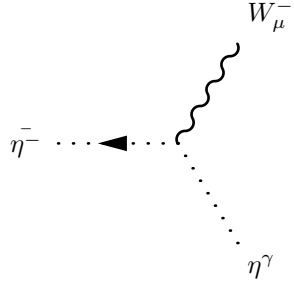
$$g_3 f_{\alpha,\beta,\gamma} \left( p_{\mu}^{\eta_{\beta}^G} \right) \quad (165)$$


---



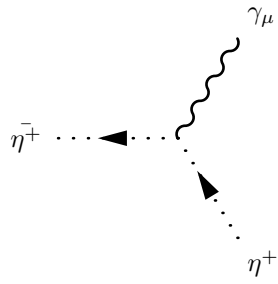
$$-ig_2 \sin \Theta_W \left( p_{\mu}^{\eta^{\gamma}} \right) \quad (166)$$


---



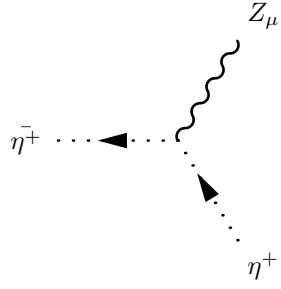
$$ig_2 \sin \Theta_W \left( p_{\mu}^{\eta^{\gamma}} \right) \quad (167)$$


---



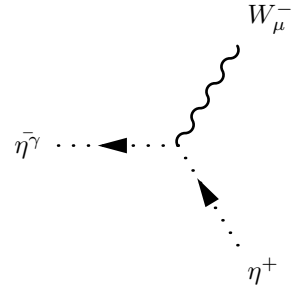
$$ig_2 \sin \Theta_W \left( p_{\mu}^{\eta^+} \right) \quad (168)$$


---



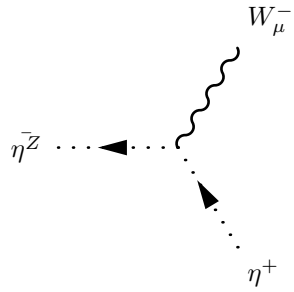
$$ig_2 \cos \Theta_W (p_\mu^{\eta^+}) \quad (169)$$


---



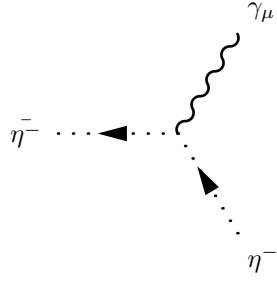
$$-ig_2 \sin \Theta_W (p_\mu^{\eta^+}) \quad (170)$$


---



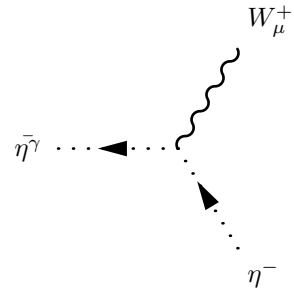
$$-ig_2 \cos \Theta_W (p_\mu^{\eta^+}) \quad (171)$$


---



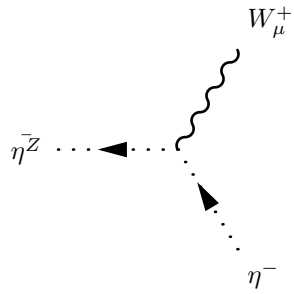
$$-ig_2 \sin \Theta_W (p_\mu^{\eta^-}) \quad (172)$$


---



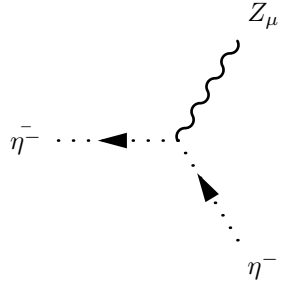
$$ig_2 \sin \Theta_W (p_\mu^{\eta^-}) \quad (173)$$


---



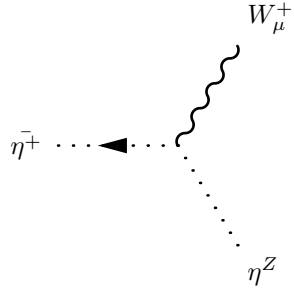
$$ig_2 \cos \Theta_W (p_\mu^{\eta^-}) \quad (174)$$


---



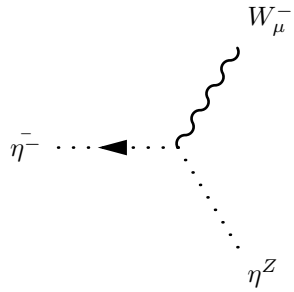
$$-ig_2 \cos \Theta_W \left( p_\mu^{\eta^-} \right) \quad (175)$$


---



$$-ig_2 \cos \Theta_W \left( p_\mu^{\eta^Z} \right) \quad (176)$$

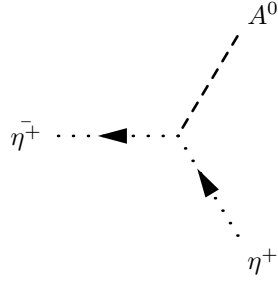

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$$ig_2 \cos \Theta_W \left( p_\mu^{\eta^Z} \right) \quad (177)$$

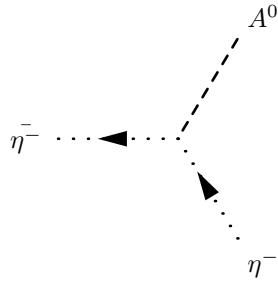

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### 9.11 Two Ghosts-One Scalar-Interaction



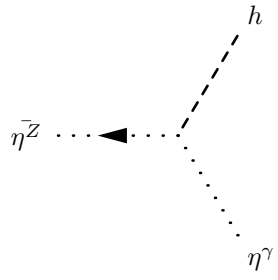
$$\frac{1}{4}g_2^2 v \xi_{W^+} \quad (178)$$


---



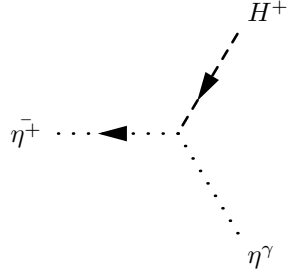
$$-\frac{1}{4}g_2^2 v \xi_{W^+} \quad (179)$$


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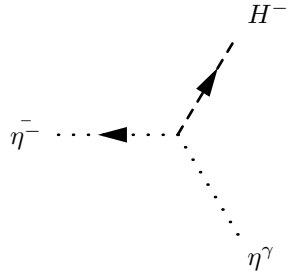
$$\frac{i}{8}v\xi_Z \left( 2g_1g_2 \cos 2\Theta_W + \left( -g_2^2 + g_1^2 \right) \sin 2\Theta_W \right) \quad (180)$$


---



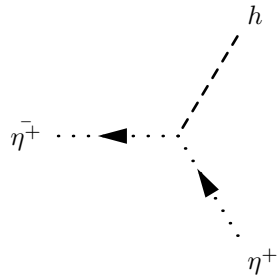
$$-\frac{i}{4}g_2v\xi_{W^+}\left(g_1\cos\Theta_W+g_2\sin\Theta_W\right) \quad (181)$$


---



$$-\frac{i}{4}g_2v\xi_{W^+}\left(g_1\cos\Theta_W+g_2\sin\Theta_W\right) \quad (182)$$

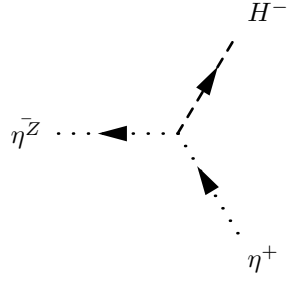

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$$-\frac{i}{4}g_2^2v\xi_{W^+} \quad (183)$$

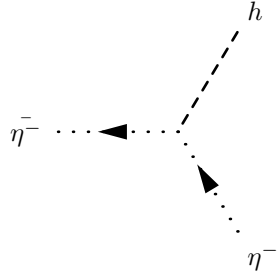

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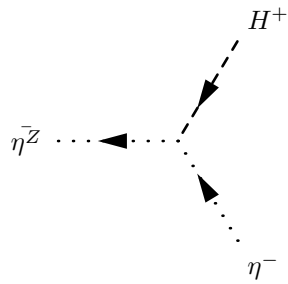
$$\frac{i}{4}g_2v\xi_Z\left(g_1\sin\Theta_W+g_2\cos\Theta_W\right) \quad (184)$$


---



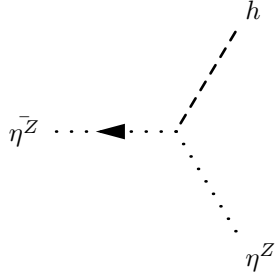
$$-\frac{i}{4}g_2^2v\xi_{W^+} \quad (185)$$


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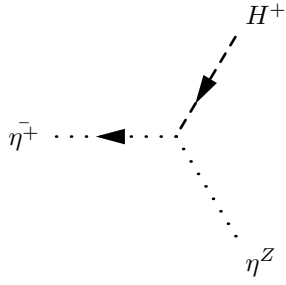
$$\frac{i}{4}g_2v\xi_Z\left(g_1\sin\Theta_W+g_2\cos\Theta_W\right) \quad (186)$$


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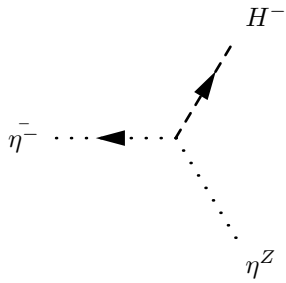
$$-\frac{i}{4}v\xi_Z\left(g_1\sin\Theta_W+g_2\cos\Theta_W\right)^2 \quad (187)$$


---



$$-\frac{i}{4}g_2v\xi_{W^+}\left(-g_1\sin\Theta_W+g_2\cos\Theta_W\right) \quad (188)$$


---



$$-\frac{i}{4}g_2v\xi_{W^+}\left(-g_1\sin\Theta_W+g_2\cos\Theta_W\right) \quad (189)$$


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## 10 Clebsch-Gordan Coefficients